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Draw in the bisectors of the angles and call Α. mistitte ## # the points of intersection P, Q, R, S. Since AK CL and BM HD the quadrilateral PQRS is a parallelogram. Since $m \angle ABP = m \angle BAP = 45^{\circ}$, $m \angle BPA = mQPS = 90^{\circ}$, so PQRS is a rectangle. Finally, $\triangle ABK \cong \triangle CDL \cong \triangle MAB \cong \triangle HCD$ and $\triangle HQK \cong \triangle MSL$, QR = RS = SP = PQ, so PQRS is a square.

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Institute % 19. Let 3x, 4x, and 5x be the measures of the 3 remaining exterior angles. Since the D. sum of the exterior angles of a polygon is 360° , 75+105+3x+4x+5x=360, $180 + 12x = 360 \implies x = 15$, so the smallest angle has measure $3 \cdot 15 = 45^{\circ}$.

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rectangular solid as shown. Then $(\sqrt{153}x)^2 + (4x)^2 = BC^2 \Rightarrow BC = 13x$. Also 39 = 13x, x = 3, so the longest dimensional dimensional dimension. 39 = 13x, x = 3, so the longest dimension of the

Let A, B, C be the vertices of the



Draw triangle ABE which is equilateral and 21. D. construct \overline{EP} so that $\overline{EP} \perp \overline{AB}$. The desired distance from E to CD equals x - EP. $EP = \frac{\sqrt{3}}{2}x$ and

$$x - EP = x - \frac{\sqrt{3}}{2}x = x\left(1 - \frac{\sqrt{3}}{2}\right) = x\left(\frac{2 - \sqrt{3}}{2}\right) = \frac{x}{2}\left(2 - \sqrt{3}\right)$$

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tinstitute # * formed. So $9^2 + 12^2 = OP^2 \Rightarrow OP = 15$ A right triangle with legs of lengths 9 and 12 and 22. D. hypotenuse \overline{OP} , where \overline{OP} is the radius of the sphere, is withte the the the

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The surface area of the solid consists of 6 faces of dimension 3 x 3 each with a 1 x % С. ute m W 1 square hole. The walls of the 6 holes can each be unfolded to form 1 x 4 rectangles. Thus the surface area is $6(3 \cdot 3 - 1 \cdot 1) + 6 \cdot 4 = 72$.

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The diagram shows how the octagon can be Β.

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decomposed into 4 congruent rectangles and 8 congruent triangles. Let R represent the area of a rectangle and let T region to the area of the entire octagon is $\frac{R+2T}{4R+8T} = \frac{1}{4}$.

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- 1. 近新法·资**A**. A. By the Triangle Inequality, $13-9 < k < 13+9 \Rightarrow 4 < k < 22$. For an obtuse triangle, $9^2 + 13^2 < k^2 \Rightarrow 250 < k^2 \Rightarrow k > 15.8$, so $k \in \{16, 17, 18, 19, 20, 21\}$. Also $9^2 + k^2 < k^2 \Rightarrow k^2 < 88 \Rightarrow k < 9.38$, so $k \in \{5, 6, 7, 8, 9\}$. There are 11 possible values for
 - If Ali broke the toy, then Barbara is lying by saying that Tyler broke it. So Ali Β. cannot have broken the toy. If Tyler broke it, then Ali is lying. So Tyler cannot have broken it. If Hei-Lam broke it, then both Ali and Barbara are lying. So Hie-Lam cannot have broken it, then nobody else is lying. Thus it must have been Barbara who broke it.
- Let x and y be the lengths of the sides of the two D. matitute ## isosceles triangles removed from the square, and a and b be the sides of the rectangle that remains. Then the area of the triangles removed are $\frac{1}{2}x^2, \frac{1}{2}x^2, \frac{1}{2}y^2, \text{ and } \frac{1}{2}y^2.$
 - X'S the J. Minte the to đ y So the total area removed is $x^2 + y^2 = 200$. The · 3. 8% х lengths of the sides of the rectangle are $a = \sqrt{2}x$ and Y inte d CX $b = \sqrt{2}v$. Thus the diagonal of the rectangle is $d^{2} = a^{2} + b^{2} = (\sqrt{2}x)^{2} + (\sqrt{2}y)^{2} = 2(x^{2} + y^{2}) = 2(200) = 400$. Thus $d = \sqrt{400} = 20$ Let t be the number of minutes since 3:00 when the two hands are perpendicular.
 - This time will be sometime after 3:30 so we expect t to be greater than 30. The minute hand will have moved through an angle of $\frac{t}{60} \cdot 360^\circ = (6t)^\circ$. The hour hand will have
- moved $\frac{t}{60} \cdot 30^\circ = \left(\frac{t}{2}\right)^\circ$, so the hour hand is $\left(\frac{t}{2} + 90\right)^\circ$ from 12:00. When the two hands are next perpendicular we have matime to the star of the Astitute ## # '\$ Withite the the 'S

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$$6t - \left(\frac{t}{2} + 90\right) = 90 \Rightarrow 6t - \frac{t}{2} = 180 \Rightarrow 11t = 360 \Rightarrow t - \frac{360}{11} = 32\frac{8}{11} \text{ minutes or approximately 32 minutes and 43.6 seconds.}$$

35. C. Since $\angle DAF + \angle ADF = 90^\circ = \angle DAF + \angle BAF$, we see that $\angle ADF = \angle BAF$ and thus $\triangle ADE$ is similar to $\triangle BAF$. This means that $\frac{DE}{DR} - \frac{AF}{D}$ or $\frac{5}{3} - \frac{AF}{BF}$. Similarly, $\frac{CF}{BF} - \frac{DE}{C} = \frac{5}{7}$. Therefore, $\frac{AF}{BF} + \frac{CF}{BF} - \frac{AF + CF}{BF} - \frac{AE + CE}{BF} = \frac{10}{BF} - \frac{5}{3} + \frac{5}{7} - \frac{50}{21}$, thus $BF - \frac{210}{50} = \frac{1}{5} - 4.2$
36. D. Let *O* denote the center of the circle, and let *OR* and *AB* be the radius and the chord which are perpendicular bisectors of cend other at *M*. Applying the perpendicular bisectors of cend other at *M*. Applying the perpendicular bisectors of cend other at *M*. Applying the method bisectors of cend other at *M*. Applying the method bisectors of cend other at *M*. Support the second other at *M*. Support the end of a *AB C*, while their affluxes are equal. As $(AF) - (AF) + (AF) +$

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