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MATH PRIZE FOR GIRLS Saturday, November 14, 2009

BOOKLET TEST Test Version A

DIRECTIONS

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- 加加斯林道院 2. Fill out the top of your answer sheet. Your student number is on your name tag.
 Your test version (A, B, C, or D) is above on this page
- 3. You may use pencils, pens, and erasers. You may also use the scratch paper that we provide. You may NOT use calculators, rulere provide. graph paper bool. mstinte # # 3 PE that we provide. You may NOT use calculators, rulers, protractors, compasses,
- 4. Write your final answers on the answer sheet. When a problem specifies a Institute # # '& R mythill # # 'S PL particular form for the answer, write your answer in that form. Write your Astitute # # 'S answers clearly. We will collect only the answer sheet from you.

- 1. This test contains 20 problems. You will have 150 minutes (2.5 hours) to take the test. Your score will be the number of correct answers 面射曲服務業等 militute ##
 - 2. Figures are not necessarily drawn to scale.

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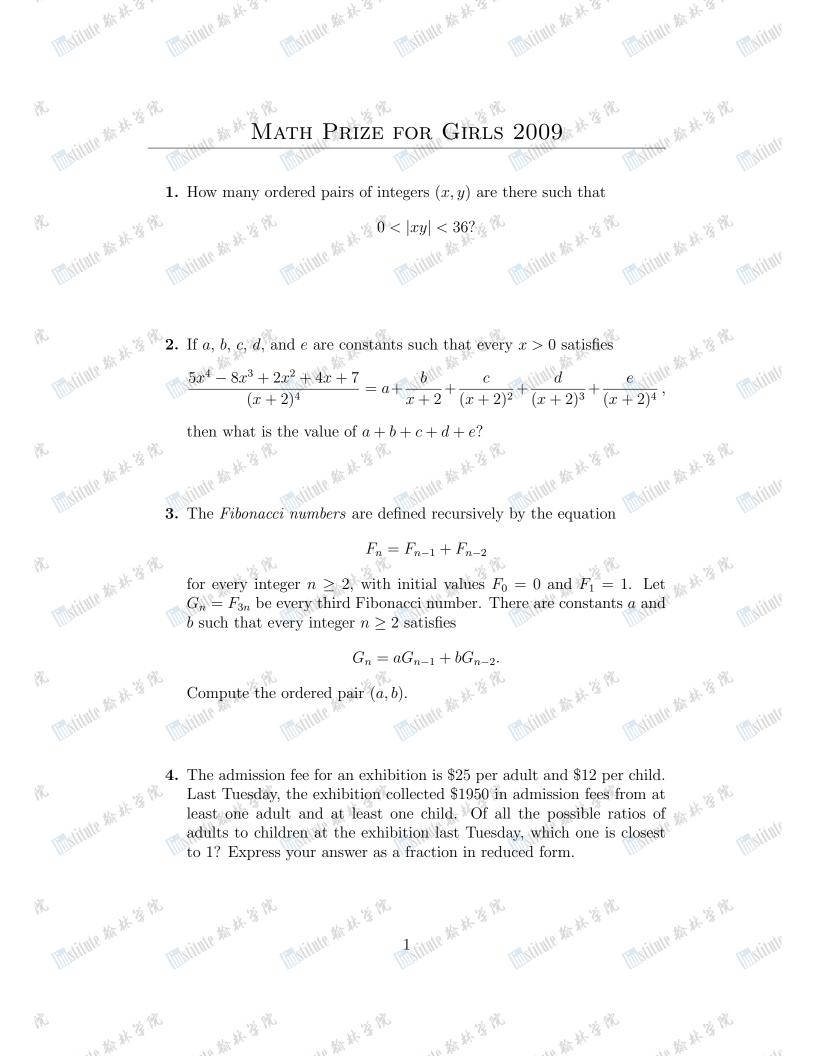
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5. The figure below shows two parallel lines, ℓ and m, that are distance 12 面动机机都样等席 而时间他都带样资源 而如此他称样姿像 Bath - manth # # * *

> A circle is tangent to line ℓ at point A. Another circle is tangent to other as shown. The distance between A and B is 13. What is the radius of each circle? Express your answer as a factor. form.

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number 1 face up. A *step* starts with a toss of the coin: if the coin comes out heads, we roll the die: otherwise (if the coin comes out heads, we roll the die: otherwise (if the coin comes of the coin comes o 6. Consider a fair coin and a fair 6-sided die. The die begins with the tails), we do nothing else in this step. After 5 such steps, what is the probability that the number 1 is face up on the die? Express your mutute # # '& R 而时间的新祥生活院 answer as a fraction in reduced form.

面对机能称并接触 加城城城 7. Compute the value of the expression

 $2009^4 - 4 \times 2007^4 + 6 \times 2005^4 - 4 \times 2003^4 + 2001^4$

面的机机都林塔张 Astitute the the the Asitute to the 'S PE Millitte # # ' K Thilling ## 'S PE Institute ## # 'S PS 8. Which point on the circle $(x - 11)^2 + (y - 13)^2 = 116$ is farthest from the point (41, 25)? Express your answer as an ordered pair. Inditute # # '& R mythte # # 'S R 面动曲线 mythte # # '& K 而如此他教祥後然

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9. The figure below is a 4×4 grid of points.

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而此此服務株等除 withthe start to the Autitute # # 18 18 Each pair of horizontally adjacent or vertically adjacent points are distance 1 apart. In the plane of this grid, how many circles of radius 1 pass through exactly two of these grid points? Withit the the the

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面对机机新林塔像 stitute # # stitute \$55 \$* 10. When the integer $(\sqrt{3}+5)^{103} - (\sqrt{3}-5)^{103}$ is divided by 9, what is the remainder?

面对机机物林塔张 柳林·凌邻 the War W 11. An arithmetic sequence consists of 200 numbers that are each at least 10 and at most 100. The sum of the numbers is 10,000. Let L be the *least* possible value of the 50th term and let G be the *greatest* possible Multille # # 'S PL mistille # # '\$ 1% value of the 50th term. What is the value of G - L? Express your 而此此微教林塔梯 multille # # 'S answer as a fraction in reduced form. stitute \$

12. Jenny places 100 pennies on a table, 30 showing heads and 70 showing mstinte # # '& R tails. She chooses 40 of the pennies at random (all different) and turns to show tails; if a chosen penny was showing tails, she turns it to show heads. At the end, what is the expected number (pennies showing heads?

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13. The figure below shows a right triangle $\triangle ABC$. myinne # # K

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The legs AB and BC each have length 4. An equilateral triangle stitute # # * * $\triangle DEF$ is inscribed in $\triangle ABC$ as shown. Point D is the midpoint of \overline{BC} . What is the area of $\triangle DEF$? Express your answer in the form $m\sqrt{3}-n$, where m and n are positive integers.

D

- 14. The three roots of the cubic $30x^3 50x^2 + 22x 1$ are distinct real Institute that the "3 PR numbers between 0 and 1. For every nonnegative integer n, let s_n be the sum of the nth powers of these three roots. What is the value of the infinite series te Kit $s_0 + s_1 + s_2 + s_3 + \dots$?
- **15.** Let $x = \sqrt[3]{\frac{4}{25}}$. There is a unique value of y such that 0 < y < x and $x^x = y^y$. What is the value of y? Express your answer in the form $\sqrt[c]{\frac{a}{b}}$, where a and b are relatively prime positive integers and c is a prime number.
- mistille # # 3 PE **16.** Let x be a real number such that the five numbers $\cos(2\pi x)$, $\cos(4\pi x)$, $\cos(8\pi x)$, $\cos(16\pi x)$, and $\cos(32\pi x)$ are all nonpositive. What is the smallest possible positive value of x? Express your answer as a fraction in reduced form. Inditute # # '& R mutute # # B Astitute ## # '\$ PR matine # # 'S R Autitute the the " the Tailute the the the

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