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Introduction

This book is designed to provide you with review and practice for algebra success! It is not intended to teach common algebra topics. Instead, it provides 501 problems so you can flex your muscles and practice a variety of mathematical and algebraic skills. *501 Algebra Questions* is designed for many audiences. It's for anyone who has ever taken a course in algebra and needs to refresh and revive forgotten skills. It can be used to supplement current instruction in a math class. Or, it can be used by teachers and tutors who need to reinforce student skills. If, at some point, you feel you need further explanation about some of the algebra topics highlighted in this book, you can find them in the LearningExpress publication *Algebra Success in 20 Minutes a Day*.

How to Use This Book

First, look at the table of contents to see the types of algebra topics covered in this book. The book is organized into 20 chapters with a variety of arithmetic, algebra, and word problems. The structure follows a common sequence of concepts introduced in basic algebra courses. You may want to follow the sequence, as each succeeding chapter builds on skills taught in previous chapters. But if

your skills are just rusty, or if you are using this book to supplement topics you are currently learning, you may want to jump around from topic to topic.

Chapters are arranged using the same method. Each chapter has an introduction describing the mathematical concepts covered in the chapter. Second, there are helpful tips on how to practice the problems in each chapter. Last, you are presented with a variety of problems that generally range from easier to more difficult problems and their answer explanations. In many books, you are given one model problem and then asked to do many problems following that model. In this book, every problem has a complete step-by-step explanation for the solutions. If you find yourself getting stuck solving a problem, you can look at the answer explanation and use it to help you understand the problem-solving process.

As you are solving problems, it is important to be as organized and sequential in your written steps as possible. The purpose of drills and practice is to make you proficient at solving problems. Like an athlete preparing for the next season or a musician warming up for a concert, you become skillful with practice. If, after completing all the problems in a section, you feel that you need more practice, do the problems over. It's not the answer that matters most—it's the process and the reasoning skills that you want to master.

You will probably want to have a calculator handy as you work through some of the sections. It's always a good idea to use it to check your calculations. If you have difficulty factoring numbers, the multiplication chart on the next page may help you. If you are unfamiliar with prime numbers, use the list on the next page so you won't waste time trying to factor numbers that can't be factored. And don't forget to keep lots of scrap paper on hand.

Make a Commitment

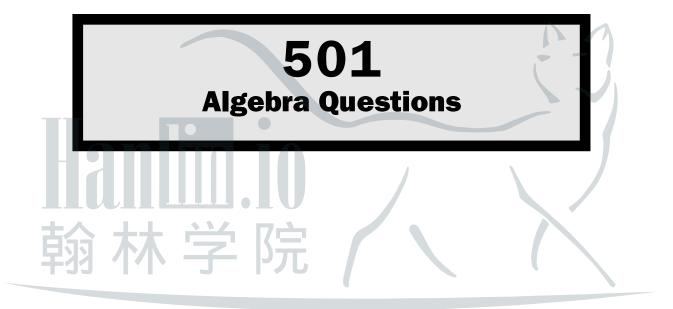
Success does not come without effort. Make the commitment to improve your algebra skills. Work for understanding. *Why* you do a math operation is as important as *how* you do it. If you truly want to be successful, make a commitment to spend the time you need to do a good job. You can do it! When you achieve algebra success, you have laid the foundation for future challenges and success. So sharpen your pencil and practice!

				М	ultipli	icatio	n Tab	le			
×	2	3	4	5	6	7	8	9	10	11	12
2	4	6	8	10	12	14	16	18	20	22	24
3	6	9	12	15	18	21	24	27	30	33	36
4	8	12	16	20	24	28	32	36	40	44	48
5	10	15	20	25	30	35	40	45	50	55	60
6	12	18	24	30	36	42	48	54	60	66	72
7	14	21	28	35	42	49	56	63	70	77	84
8	16	24	32	40	48	56	64	72	80	88	96
9	18	27	36	45	54	63	72	81	90	99	108
10	20	30	40	50	60	70	80	90	100	110	120
11	22	33	44	55	66	77	88	99	110	121	132
12	24	36	48	60	72	84	96	108	120	132	144

Commonly Used Prime Numbers

				-		-		-			
	2	3	5	7	11	13	17	19	23	29	
	31	37	41	43	47	53	59	61	67	71	_
	73	79	83	89	97	101	103	107	109	113	
	127	131	137	139	149	151	157	163	167	173	-
	179	181	191	193	197	199	211	223	227	229	
	233	239	241	251	257	263	269	271	277	281	
	283	293	307	311	313	317	331	337	347	349	
	353	359	367	373	379	383	389	397	401	409	
	419	421	431	433	439	443	449	457	461	463	
	467	479	487	491	499	503	509	521	523	541	
	547	557	563	569	571	577	587	593	599	601	
	607	613	617	619	631	641	643	647	653	659	
Ť.	661	673	677	683	691	701	709	719	727	733	$\overline{}$
	739	743	751	757	761	769	773	787	797	809	
	811	821	823	827	829	839	853	857	859	863	
	877	881	883	887	907	911	919	929	937	941	
	947	953	967	971	977	983	991	997	1,009	1,013	







Working with Integers

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For some people, it is helpful to try to simplify expressions containing signed numbers as much as possible. When you find signed numbers with addition and subtraction operations, you can simplify the task by changing all subtraction to addition. Subtracting a number is the same as adding its opposite. For example, subtracting a three is the same as adding a negative three. Or subtracting a negative 14 is the same as adding a positive 14. As you go through the step-by-step answer explanations, you will begin to see how this process of using only addition can help simplify your understanding of operations with signed numbers. As you begin to gain confidence, you may be able to eliminate some of the steps by doing them in your head and not having to write them down. After all, that's the point of practice! You work at the problems until the process becomes automatic. Then you own that process and you are ready to use it in other situations.

The **Tips for Working with Integers** section that follows gives you some simple rules to follow as you solve problems with integers. Refer to them each time you do a problem until you don't need to look at them. That's when you can consider them yours.

You will also want to review the rules for Order of Operations with numerical expressions. You can use a memory device called a *mnemonic* to help you remember a set of instructions. Try remembering the word **PEMDAS**. This nonsense word helps you remember to:

P do operations inside *Parentheses*

E evaluate terms with *Exponents*

M D do *Multiplication* and *Division* in order from left to right

A S Add and Subtract terms in order from left to right

Tips for Working with Integers

Addition

Signed numbers the same? Find the SUM and use the same sign. Signed numbers different? Find the DIFFERENCE and use the sign of the larger number. (The larger number is the one whose value without a positive or negative sign is greatest.)

Addition is commutative. That is, you can add numbers in any order and the result is the same. As an example, 3 + 5 = 5 + 3, or -2 + -1 = -1 + -2.

Subtraction

Change the operation sign to addition, change the sign of the number following the operation, then follow the rules for addition.

Multiplication/Division

Signs the same? Multiply or divide and give the result a **positive** sign. Signs different? Multiply or divide and give the result a **negative** sign.

Multiplication is commutative. You can multiply terms in any order and the result will be the same. For example: $(2 \cdot 5 \cdot 7) = (2 \cdot 7 \cdot 5) = (5 \cdot 2 \cdot 7) =$

 $(5 \cdot 7 \cdot 2)$ and so on.

Evaluate the following expressions.

- **1.** 27 + ⁻⁵
- **2.** ⁻18 + ⁻20 16
- **3.** ⁻15 ⁻7
- **4.** 33 + ⁻16
- **5.** 8 + ⁻4 12
- **6.** $38 \div ^{-}2 + 9$
- **7.** $-25 \cdot -3 + 15 \cdot -5$
- **8.** -5 · -9 · -2
- **9.** $24 \cdot 8 + 2$
- **10.** $2 \cdot {}^{-}3 \cdot {}^{-}7$
- **11.** ⁻15 + 5 + ⁻11

- **12.** $(49 \div 7) (48 \div {}^{-}4)$
- **13.** 3 + ⁻7 14 + 5
- **14.** $(5 \cdot 3) + (12 \div 4)$
- **15.** $(-18 \div 2) (6 \cdot -3)$
- **16.** 23 + (64 ÷ ⁻16)
- **17.** $2^3 (-4)^2$
- **18.** $(3-5)^3 + (18 \div 6)^2$
- **19.** $21 + (11 + -8)^3$
- **20.** $(3^2 + 6) \div (-24 \div 8)$
- **21.** A scuba diver descends 80 feet, rises 25 feet, descends 12 feet, and then rises 52 feet where he will do a safety stop for five minutes before surfacing. At what depth did he do his safety stop?
- **22.** A digital thermometer records the daily high and low temperatures. The high for the day was ⁺5° C. The low was ⁻12° C. What was the difference between the day's high and low temperatures?
- 23. A checkbook balance sheet shows an initial balance for the month of \$300. During the month, checks were written in the amounts of \$25, \$82, \$213, and \$97. Deposits were made into the account in the amounts of \$84 and \$116. What was the balance at the end of the month?
- 24. A gambler begins playing a slot machine with \$10 in quarters in her coin bucket. She plays 15 quarters before winning a jackpot of 50 quarters. She then plays 20 more quarters in the same machine before walking away. How many quarters does she now have in her coin bucket?
- **25.** A glider is towed to an altitude of 2,000 feet above the ground before being released by the tow plane. The glider loses 450 feet of altitude before finding an updraft that lifts it 1,750 feet. What is the glider's altitude now?

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

<u>Underlined</u> expressions show the original algebraic expression as an equation with the expression equal to its simplified result.

Since all the signs are negative, add the absolute value of the numbers. [13] Since the signs were negative, the result is negative1 The simplified result of the numeric expression is as follows: -1 3. Change the subtraction sign to addition by changing the sign of the number that follows it. Signs different? Subtract the absolute value of	$ \begin{array}{r} 127 - 5 = 22] \\ \underline{27 + 5} = +22 \\ 8 + -20 + (-16) \\ 8 + 20 + 16 = 54] \\ 8 + -20 + -16 = -54 \\ \underline{8 - 20 - 16} = -54 \\ \end{array} $
 changing the sign of the number that follows it1 Since all the signs are negative, add the absolute value of the numbers. [1] Since the signs were negative, the result is negative1 The simplified result of the numeric expression is as follows: -1 3. Change the subtraction sign to addition by changing the sign of the number that follows it. Signs different? Subtract the absolute value of 	8 + 20 + 16 = 54] 8 + -20 + -16 = -54
changing the sign of the number that follows it. Signs different? Subtract the absolute value of	
the numbers. Give the result the sign of the larger term. The simplified expression is as follows:	-15 + 7 [15 - 7 = 8] -15 + 7 = -8 -15 - 7 = -8
4. Signs different? Subtract the value of the numbers. Give the result the sign of the larger term.	[33 - 16 = 17] 33 + -16 = +17

5.	Change the subtraction sign to addition by changing the sign of the number that follows it.With three terms, first group like terms and add.Signs the same? Add the value of the terms and give the result the same sign.Substitute the result into the first expression.Signs different? Subtract the value of the numbers.Give the result the sign of the larger term.The simplified result of the numeric expression is as follows:	$8 + {}^{-}4 + {}^{-}12$ $8 + ({}^{-}4 + {}^{-}12)$ $[({}^{-}4 + {}^{-}12) = {}^{-}16]$ $8 + ({}^{-}16)$ [16 - 8 = 8] $8 + ({}^{-}16) = {}^{-}8$ $\underline{8 + {}^{-}4 - 12 = {}^{-}8}$
6.	First divide. Signs different? Divide and give the result the negative sign.Substitute the result into the expression.Signs different? Subtract the value of the numbers.Give the result the sign of the term with the larger value.The simplified result of the numeric expression is as follows:	$[(38 \div ^{-}2) = ^{-}19]$ $(^{-}19) + 9$ $[19 - 9 = 10]$ $(^{-}19) + 9 = ^{-}10$ $\underline{38 \div ^{-}2 + 9} = ^{-}10$
7. 33	 First perform the multiplications. Signs the same? Multiply the terms and give the result a positive sign. Signs different? Multiply the terms and give the result a negative sign. Now substitute the results into the original expression. Signs different? Subtract the value of the numbers. The simplified result of the numeric expression is as follows: 	$\begin{bmatrix} -25 \cdot -3 &= +75 \end{bmatrix}$ $\begin{bmatrix} 15 \cdot -5 &= -75 \end{bmatrix}$ (+75) + (-75) $\begin{bmatrix} 75 - 75 &= 0 \end{bmatrix}$ $-25 \cdot -3 + 15 \cdot -5 &= 0$
8.	Because all the operators are multiplication, you could group any two terms and the result would be the same. Let's group the first two terms.Signs the same? Multiply the terms and give the result a positive sign.Now substitute the result into the original expression.Signs different? Multiply the terms and give the result a negative sign.The simplified result of the numeric expression is as follows:	$(-5 \cdot -9) \cdot -2$ $[5 \cdot 9 = 45]$ $+45 \cdot -2$ $+45 \cdot -2 = -90$ $-5 \cdot -9 \cdot -2 = -90$
		$\frac{-5 \cdot -9 \cdot -2}{-9 \cdot -2} = -90$

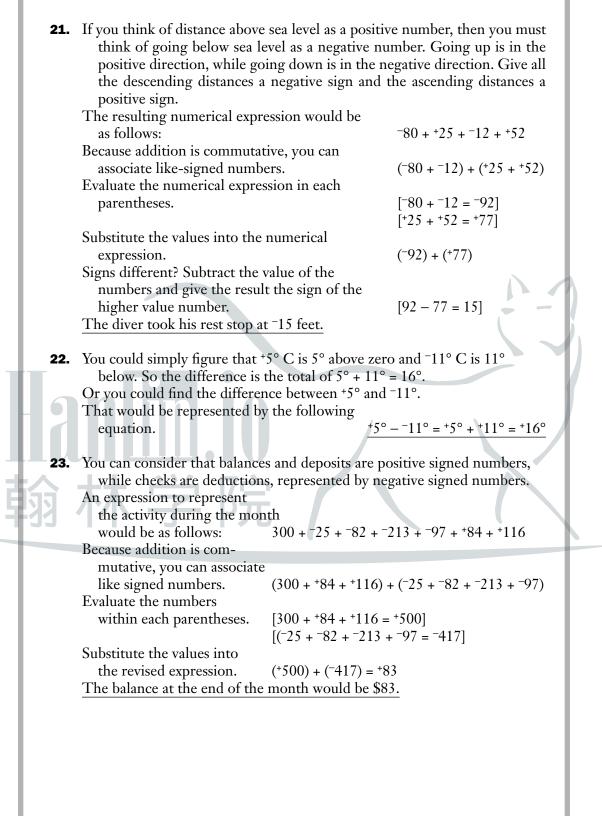
	501 Algebra Questions	
9.	Group the terms being multiplied and evaluate. Signs different? Multiply the terms and give the	
	result a negative sign.	$[24 \cdot -8 = -192]$
	Substitute.	(-192) + 2
	Signs different? Subtract the value of the terms. Give the result the sign of the term with the	
	larger value. The simplified result of the numeric expression	$(^{-192}) + 2 = ^{-190}$
	is as follows:	$\underline{24 \cdot {}^{-}8 + 2} = {}^{-}190$
10.	Because all the operators are multiplication, you could group any two terms and the result woo	uld be
	the same. Let's group the last two terms. Signs the same? Multiply the terms and give the	
	result a positive sign.	$[(-3 \cdot -7) = +21]$
	Substitute.	2 · (+21)
	Signs the same? Multiply the terms and give the result a positive sign. The simplified result of the numeric expression	$2 \cdot (+21) = +42$
	as follows:	$\underline{2 \cdot -3 \cdot -7} = +42$
11.	Because all the operators are addition, you could	
	group any two terms and the result would be	
	same. Or you could just work from left to right Signs different? Subtract the value of the number	
ШU	Give the result the sign of the term with the	[(-15, 5), -10]
	larger value. Substitute.	[(-15 + 5) = -10] (-10) + -11
	Signs the same? Add the value of the terms	(10) + 11
	and give the result the same sign.	[10 + 11 = 21]
	and give the result the same sign.	(-10) + -11 = -21
	The simplified result of the numeric expression	(10) 11 11
	is as follows:	-15 + 5 + -11 = -21
12.	First evaluate the expressions within the	
	parentheses.	$[49 \div 7 = 7]$
	Signs different? Divide and give the result	
	a negative sign.	$[48 \div ^{-}4 = ^{-}12]$
	Substitute into the original expression.	(7) - (-12)
	Change the subtraction sign to addition by changing the sign of the number that	
	follows it.	7 + +12
	Signs the same? Add the value of the terms and give the result the same sign.	7 + +12 = +19
		7 + +12 = +19 $(49 \div 7) - (48 \div -4) = +19$

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13.	Change the subtraction sign to addition by	2714 . 5
	changing the sign of the number that follows it.	
	Now perform additions from left to right. Signs different? Subtract the value of the numbers	$(3 + ^{-7}) + ^{-14} + 5$
	and give the result the sign of the higher value	
	number.	[7 - 3 = 4]
	number.	[3 + 7 = 4]
	Substitute.	$(^{-4}) + ^{-14} + 5$
	Add from left to right.	(-4 + -14) + 5
	Signs the same? Add the value of the terms and	, <i>,</i>
	give the result the same sign.	[-4 + -14 = -18]
	Substitute.	(~18) + 5
	Signs different? Subtract the value of the	
	numbers and give the result the sign of the	
	higher value number.	[18 - 5 = 13]
		(-18) + 5 = -13
	The simplified result of the numeric expression is as follows:	3 + -7 + -14 + 513
	is as follows:	$\underline{3 + -7 + -14 + 5 = -13}$
14.	First evaluate the expressions within the	
	parentheses.	$[5 \cdot 3 = 15]$
	Signs different? Divide and give the result	
6	a negative sign.	$[12 \div -4 = -3]$
	Substitute the values into the original	
	expression.	-(15) + (-3)
	Signs the same? Add the value of the terms	
	and give the result the same sign.	[15 + 3 = 18]
		$^{-}(15) + (^{-}3) = ^{-}18$
133	The simplified result of the numeric	$-(5 2) \cdot (12 - 4) - 10$
	expression is as follows:	$\frac{-(5\cdot 3) + (12 \div -4) = -18}{-18}$

15.	First evaluate the expressions within the	[/-10 2)]
	parentheses. Signs different? Divide the value of the	$[(-18 \div 2)]$
	terms and give the result a negative sign.	$[18 \div 2 = 9]$
	terms and give the result a negative sign.	$[(-18 \div 2 = -9)]$
	Signs different? Multiply the term values	
	and give the result a negative sign.	(6 · -3)
		$[6 \cdot 3 = 18]$
		$(6 \cdot {}^{-3}) = {}^{-1}8$
	Substitute the values into the original	
	expression.	(-9) – (-18)
	Change subtraction to addition and change	(0) (110)
	the sign of the term that follows.	(-9) + (+18)
	Signs different? Subtract the value of the	
	numbers and give the result the sign of the higher value number.	[18 - 0 - 0]
	lingher value humber.	[18 - 9 = 9] (-9) + (+18) = +9
	The simplified result of the numeric	())+(10)=)
	expression is as follows:	$(-18 \div 2) - (6 \cdot -3) = +9$
16.	Evaluate the expressions within the parentheses.	(64 ÷ ⁻ 16)
	Signs different? Divide and give the result	
	a negative sign.	$[64 \div 16 = 4]$
		$(64 \div -16 = -4)$
	Substitute the value into the original expression.	23 + (-4)
	Signs different? Subtract the value of the	
\mathbf{A}	numbers and give the result the sign of the	
17	higher value number.	[23 - 4 = 19]
	The simplified result of the numeric expression	23 + (-4) = +19
	is as follows:	$23 + (64 \div ^{-1}6) = ^{+19}$
		<u></u>
17.	The order of operations tells us to evaluate the	$[2^3 = 2 \cdot 2 \cdot 2 = 8]$
	terms with exponents first.	$[2^{-}=2^{-}\cdot 2^{-}\cdot 2^{-}=8]$ $[(-4)^{2}=(-4)\cdot(-4)]$
	Signs the same? Multiply the terms and give	$\left[\left(\begin{array}{c} 1 \right)^{-1} - \left(\begin{array}{c} 1 \right)^{-1} \left(\begin{array}{c} 1 \right)^{-1} \right] \right]$
	the result a positive sign.	$[4 \cdot 4 = 16]$
		$[(-4)^2 = +16]$
	Substitute the values of terms with exponents	
	into the original expression.	$2^3 - (-4)^2 = (8) - (+16)^2$
	Change subtraction to addition and change	
	the sign of the term that follows.	8 + -16
	Signs different? Subtract the value of the	
	numbers and give the result the sign of the	
	higher value number.	[16 - 8 = 8]
		8 + -16 = -8

	The simplified result of the numeric expression is as follows:	$2^3 - (-4)^2 = -8$
18.	First evaluate the expressions within the	
	parentheses. Change subtraction to addition and change	[3 – 5]
	the sign of the term that follows. Signs different? Subtract the value of the	[3 + (⁻ 5)]
	numbers and give the result the sign of the	[
	higher value number.	[5-3=2]
		$[3-5=^{-2}]$ [18 ÷ 6 = 3]
	Substitute the values of the expressions in	$\begin{bmatrix} 10 \div 0 = 5 \end{bmatrix}$
	parentheses into the original expression.	$(-2)^3 + (3)^2$
	Evaluate the terms with exponents.	$[(-2)^3 = -2 \cdot -2 \cdot -2]$
	1	$[(-2 \cdot -2) \cdot -2 = (+4) \cdot -2]$
	Signs different? Multiply the value of the	
	terms and give the result a negative sign.	$[(+4) \cdot -2 = -8]$
		$[(3)^2 = 3 \cdot 3 = 9]$
	Substitute the values into the expression.	$(^{-2})^3 + (3)^2 = ^{-8} + 9$
	Signs different? Subtract the value of the	
	numbers and give the result the sign of the higher value number.	9 - 8 = +1
	The simplified result of the numeric	y = 0 = 1
	expression is as follows:	$\frac{(3-5)^3 + (18 \div 6)^2 = +1}{}$
19.		
19.	First evaluate the expression within the parenthese Signs different? Subtract the value of the numbers	
isa -	and give the result the sign of the higher value	
	number.	[11 - 8 = 3]
		[11 + -8 = +3]
	Substitute the value into the expression.	$21 + (+3)^3$
	Evaluate the term with the exponent.	$[(+3)^3 = 3^3 = 27]$
	Substitute the value into the expression.	21 + (27) = 48
	The simplified result of the numeric expression is as follows:	$21 \cdot (11 \cdot -0)^3 = 40$
	as follows:	$\frac{21 + (11 + ^{-8})^3 = 48}{21 + (11 + ^{-8})^3 = 48}$
20.	First evaluate the expressions within the	
	parentheses.	$[3^2 + 6 = (9) + 6 = 15]$
	Signs different? Divide and give the result	
	the negative sign.	$[-24 \div 8 = -3]$
	Substitute values into the original expression.	$(15) \div (-3)$
	Signs different? Divide the value of the	$[15 \div 3 = 5]$
	terms and give the result a negative sign.	$[15 \div 5 = 5]$ $(15) \div (-3) = -5$
	The simplified result of the numeric	$(1) \neq (3) = 3$
	expression is as follows:	$(3^2 + 6) \div (-24 \div 8) = -5$



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24.	 You first figure out how many quarters she starts with. Four quarters per dollar gives you 4 · 10 = 40 quarters. You can write an expression tha represents the quarters in the bucket and the quarters added and subtracted. In chronologic order, the expression would be as follows: Change all operation signs to addition and the sign of the number that follows. Because addition is commutative, you can associate like-signed numbers. Use the rules for adding integers with like signs. Substitute into the revised expression. Signs different? Subtract the value of the numbers and give the result the sign of the number. The simplified result of the numeric expression is as follows: 	t	
25. 27 27 27		while descending is a neg-	



Working with Algebraic Expressions

This chapter contains 25 algebraic expressions; each can contain up to five variables. Remember that a variable is just a letter that represents a number in a mathematical expression. When given numerical values for the variables, you can turn an algebraic expression into a numerical one.



As you work through the problems in this chapter, you are to substitute the assigned values for the variables into the expression and evaluate the expression. You will be evaluating expressions very much like the previous numerical expressions. The answer section contains complete explanations of how to go about evaluating the expressions. Work on developing a similar style throughout, and you will have one sure way of solving these kinds of problems. As you become more familiar and comfortable with the look and feel of these expressions, you will begin to find your own shortcuts.

Read through the **Tips for Working with Algebraic Expressions** before you begin to solve the problems in this section.

Tips for Working with Algebraic Expressions

- Substitute assigned values for the variables into the expression.
- Use PEMDAS to perform operations in the proper order.
- Recall and use the Tips for Working with Integers from Chapter 1.

501 Algebra Questions
• Evaluate the following algebraic expressions when

$$a = 3$$

 $b = 5$
 $a = 6$
 $y = \frac{1}{2}$
 $z = -8$
26. $4a + z$
27. $3x + z$
28. $2ax - z$
29. $5ab + xy$
30. $4b^2 - az$
31. $7x + 2yz$
32. $bx + z + y$
33. $(b + 2)^2$
35. $2(a^2 + 2y) + b$
36. $a^3 + 24y - 3b$
37. $2x - b + az$
38. $5z^2 - 2z + 2$
39. $5xy + 2b$
40. $7x + \frac{12}{x} - z$
41. $2b^2 + y$
42. $bx(z + 3)$
43. $6y(z + y) + 3ab$
44. $2bx + (z - b)$
45. $12ab + y$
46. $y((\frac{2}{z} - 3) - 4a)$
47. $10b^3 - 4b^2$
48. $8y(a^3 - 2y)$
49. $z^2 - 4a^2y$
50. $3x^2b(5a - 3b)$

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

<u>Underlined</u> expressions show the original algebraic expression as an equation with the expression equal to its simplified result.

a = 3

b = -5

- x = 6
- $y = \frac{1}{2}$ z = -8

26.	Substitute the values for the variables into the expression Order of operations tells you to multiply first. Substitute. Signs different? Subtract the value of the numbers. Give the result the sign of the larger value. (No sign	$\begin{array}{l} . \qquad 4(3) + (^{-}8) \\ [4(3) = 12] \\ (12) + (^{-}8) \\ 12 - 8 = 4 \end{array}$	
27.	means ⁺) The value of the expression is as follows: Substitute the values for the variables into the	$\frac{^{+}4}{4a+z=^{+}4}$	
21.		2(() (0)	
	$(-2\frac{1}{4})$	$3(6) \div (-8) [3(6) = 18] (18) \div (-8) [18 \div 8 = 2\frac{2}{8} = 2\frac{1}{4}] 3x \div z = -2\frac{1}{4} \text{ or } -2.25$	
28.	Substitute the values for the variables into the expression Multiply the factors of the first term.Substitute.Change the operator to addition and the sign of the number that follows.Signs the same? Add the value of the terms and give the result the same sign.	2(3)(6) - (-8) [2(3)(6) = 36] (36) - (-8) (36) + (+8) [36 + 8 = 44]	
	result the same sign.	[50 + 8 = 7]	1

(44) $2ax-z=+44$ 19. Substitute the values for the variables into the expression. Evaluate the first term of the expression. Signs different? Multiply the terms and give the result a negative sign. Figns different? Subtract the values of the numbers. Give the result an equivalent values into the original expression. Signs different? Subtract the value of the numbers. Give the result an equivalent values into the original expression. $5(3)(5) + (6)(\frac{1}{2})$ $(5(3)(5) = 15(-5))$ $(6)(\frac{1}{2}) = 3$ $(75) + (3)$ $(75 - 3) = 72$ $(6)(\frac{1}{2}) = 3$ $(75) + (3)$ $(75 - 3) = 72$ (72) 30. Substitute the values for the variables into the expression. Now evaluate the term with the exponent. Signs different? Multiply and give the result a negative sign. Now evaluate the optivation to addition and the sign of the number that follows. $4(-5)^2 - (3)(-8)$ $(72)^2 = (5) \cdot (-5)$ $(5)(-5) = 100$ $(3)(-8)$ 31. Substitute the values for the variables into the expression. Defined value of the expression is as follows: $3(-8 = 24)$ $(100) - (-24)$ $(10) + (24) = 124$ $42^4 - a = -124$ 31. Substitute the values for the variables into the expression. Defined value of the expression is as follows: $3(-8 = 24)$ $(100) - (-24)$ 31. Substitute the values for the variables into the expression. Defined value of the expression is as follows: $1(-9) + (2\frac{1}{2})(-8)$ $(3)(-8)$ 31. Substitute the values for the variables into the expression. Defined value of the expression is as follows: $1(-9) + (2\frac{1}{2})(-8) = -5(-5)$ 31. Substitute the values into the expression. Defined value of the expression is as follows: $1(-2) + (3)$ $(2\frac{1}{2})(-8) = -5(-5)$		ovi Algobia questions	
expression. $5(3)(-5) + (6)(\frac{1}{2})$ Evaluate the first term of the expression. $[5(3)(-5) = 15(-5)]$ Signs different? Multiply the terms and give the result a negative sign. $[15(-5) = -75]$ Evaluate the second term of the expression. $[6(6)(\frac{1}{2}) = 3]$ Substitute the equivalent values into the original expression. $(-75) + (3)$ Signs different? Subtract the value of the numbers. $[75 - 3 = 72]$ Give the result the sign of the larger value. (-72) The simplified value of the expression is as follows: $5ab + xy = -72$ 30. Substitute the values for the variables into the expression. $4(-5)^2 - (3)(-8)$ PEMDAS: Evaluate the term with the exponent. $[(-5)^2 = (-5) \cdot (-5)]$ Substitute. $(-5)^2 = (-5) \cdot (-5)]$ Substitute. $[(-5)^2 = (-5) \cdot (-5)]$ Substitute. $[(-5)^2 = 100]$ Now evaluate the other term. $[(3)(-8)]$ Substitute the equivalent values into the original expression. $(100) - (-24)$ Change the operator to addition and the sign of the number that follows. $100 + +24 = 124$ 4b ² - az = 124 31. Substitute the values for the variables into the expression. $7(6) + 2(\frac{1}{2})(-8)$ PEMDAS: Multiply the terms in the expression. $(7 \cdot 6 = 42]$ $[2(\frac{1}{2})](-8) = -8]$ Substitute the equivalent values into the original expression. $(42) + (-8)$ Signs different? Divide and give the result a negative sign. $(42 + 8 = 5.25]$ (42) + (-8) = -5.25 The simplified value of the expression is		The simplified value of the expression is as follows	
expression. PEMDAS: Evaluate the term with the exponent. Signs the same? Multiply the terms and give the result a positive sign. Substitute. Now evaluate the other term. Signs different? Multiply and give the result a negative sign. Substitute the equivalent values into the original expression. Change the operator to addition and the sign of the number that follows. The simplified value of the expression is as follows: PEMDAS: Multiply the terms in the expression. Substitute the equivalent values into the original expression. Substitute the equivalent values into the expression. Substitute the equivalent values into the original expression. Substitute the equivalent values into the original expression. Signs different? Divide and give the result a negative sign. Substitute the equivalent values into the original expression. Signs different? Divide and give the result a negative sign. Substitute of the expression is Substitute the equivalent values into the original expression. Signs different? Divide and give the result a negative sign. Substitute of the expression is Substitute the equivalent values into the original expression. Signs different? Divide and give the result a negative sign. Substitute the expression is Substitute the expression is Substitute the expression is Substitute the equivalent the expression is Substitute the equivalent values into the original expression. Signs different? Divide and give the result a negative sign. Substitute the expression is Substitute	29.	 expression. Evaluate the first term of the expression. Signs different? Multiply the terms and give the result a negative sign. Evaluate the second term of the expression. Substitute the equivalent values into the original expression. Signs different? Subtract the value of the numbers Give the result the sign of the larger value. 	$[5(3)(^{-}5) = 15(^{-}5)]$ $[15(^{-}5) = ^{-}75]$ $[(6)(\frac{1}{2}) = 3]$ $(^{-}75) + (3)$ $[75 - 3 = 72]$ $(^{-}72)$
expression. $7(6) \div 2(\frac{1}{2})(-8)$ PEMDAS: Multiply the terms in the expression. $[7 \cdot 6 = 42]$ $[\{2(\frac{1}{2})\}(-8) = (1)(-8) = -8]$ Substitute the equivalent values into the original expression. $(42) \div (-8)$ Signs different? Divide and give the result a negative sign. $[42 \div 8 = 5.25]$ $(42) \div (-8) = -5.25$ The simplified value of the expression is $[42 \div 8 = -5.25]$	30.	expression. PEMDAS: Evaluate the term with the exponent. Signs the same? Multiply the terms and give the result a positive sign. Substitute. Now evaluate the other term. Signs different? Multiply and give the result a negative sign. Substitute the equivalent values into the original expression. Change the operator to addition and the sign of the number that follows.	$[(^{-5})^{2} = (^{-5}) \cdot (^{-5})]$ $[5 \cdot 5 = 25 = ^{+}25]$ $[4(^{+}25) = 100]$ $[(3)(^{-8})]$ $[3 \cdot ^{-8} = ^{-}24]$ $(100) - (^{-}24)$ $100 + ^{+}24 = 124$
	31.	expression.PEMDAS: Multiply the terms in the expression.Substitute the equivalent values into the original expression.Signs different? Divide and give the result a negative sign.The simplified value of the expression is	$[7 \cdot 6 = 42]$ [$\{2(\frac{1}{2})\}(-8) = (1)(-8) = -8$] (42) ÷ (-8) [42 ÷ 8 = 5.25] (42) ÷ (-8) = -5.25

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32.	Substitute the values for the variables into the expression.	$(-5)(6) + (-8) \div (\frac{1}{2})$
	Group terms using order of operations. PEMDAS: Multiply or divide the terms in	$(-5)(6) + \{(-8) \div (\frac{1}{2})\}$
	the expression. Signs different? Multiply and give the result	[(-5)(6)]
	a negative sign.	$[5 \cdot 6 = 30]$ [(-5)(6) = -30]
	Consider the second term.	$[(-8) \div (\frac{1}{2})]$
	Signs different? Divide and give the result a negative sign.	$[8 \div \frac{1}{2}]$
	To divide by a fraction, you multiply by the reciprocal.	$[8 \div \frac{1}{2} = 8 \cdot \frac{2}{1} = 8 \cdot 2 = 16]$
	Substitute the equivalent values into the	$[(-8) \div (\frac{1}{2}) = -16]$
	original expression. Signs the same? Add the value of the terms	(-30) + (-16)
	and give the result the same sign.	[30 + 16 = 46] (-30) + (-16) = -46
	The simplified value of the expression	
6	is as follows:	$bx + z \div y = -46$
33.	Substitute the values for the variables into the	1
	expression.	$6(\frac{1}{2}) - 2(3)(-5)$
	Evaluate the terms on either side of the	$[6(\frac{1}{2}) = 3]$
	subtraction sign.	
		$[2(3)(-5) = 2 \cdot 3 \cdot -5]$
-33	Positive times positive is positive. Positive times	
	negative is negative.	$[6 \cdot {}^{-5} = {}^{-3}0]$
	Substitute the equivalent values into the original	
	expression.	(3) - (-30)
	Change the operator to addition and the sign	
	of the number that follows.	3 - (-30) = 3 + +30
		3 + +30 = +33
	The simplified value of the expression is as follows:	$\underline{6y - 2ab} = +33$
34.	Substitute the values for the variables into the	
	expression. PEMDAS: You must add the terms inside the	$3((-5) + (-8))^2$
	parentheses first. Signs the same? Add the value of the terms and	[(-5) + (-8)]
	give the result the same sign.	[5 + 8 = 13]

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	Substitute into the original expression.Next you evaluate the term with the exponent.Signs the same? Multiply the terms and give the result a positive sign.Substitute the equivalent values into the original expression.The simplified value of the expression is as follow	$3(-13)^{2}$ $[(-13)^{2} = -13 \cdot -13]$ $[13 \cdot 13 = +169]$ s: $\frac{3(169)}{a(b+z)^{2}} = 507$
35.	 Substitute the values for the variables into the expression. Look first to evaluate the term inside the bold parentheses. The first term has an exponent. Evaluate it. Evaluate the second term. Substitute into the original numerical expression. Evaluate the first term. Substitute into the numerical expression. Signs different? Divide and give the result a negative sign. The simplified value of the expression is as follows: 	$2((3)^{2} + 2(\frac{1}{2})) \div (-5)$ $[(3)^{2} + 2(\frac{1}{2})]$ $[(3)^{2} = 3 \cdot 3 = 9]$ $[2(\frac{1}{2}) = 1]$ $[(3)^{2} + 2(\frac{1}{2}) = 9 + 1 = 10]$ $2(10) \div (-5)$ $[2(10) = 20]$ $(20) \div (-5)$ $[20 \div 5 = 4]$ $(20) \div (-5) = -4$ $\underline{2(a^{2} + 2y)} \div b = -4$
36.	 Substitute the values for the variables into the expression. Evaluate the term with the exponent. Evaluate the second term. Evaluate the third term. Signs different? Multiply and give the result a negative sign. Substitute the equivalent values into the original expression. Change the subtraction to addition and the sign of the number that follows. Signs the same? Add the value of the terms and give the result the same sign. The simplified value of the expression is as follows: 	$\frac{2(a + 2y) \div b = 4}{(3)^3 + 24(\frac{1}{2}) - 3(-5)}$ $[(3)^3 = 3 \cdot 3 \cdot 3 = 27]$ $[24(\frac{1}{2}) = 12]$ $[3(-5)]$ $[3 \cdot 5 = 15]$ $[3(-5) = -15]$ $(27) + (12) - (-15)$ $(27) + (12) + (+15)$ $27 + 12 + 15 = 54$ $\underline{a^3 + 24y - 3b = +54}$

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37.	Substitute the values for the variables into the	
	expression.	$^{-2}(6) - (^{-5}) + (3)(^{-8})$
	Evaluate first and last terms. Positive times	
	negative results in a negative.	$[-2(6) = -2 \cdot 6 = -12]$
		$[(3)(-8) = 3 \cdot -8 = -24]$
	Substitute the equivalent values into the origina	
	expression.	(-12) - (-5) + (-24)
	Change the subtraction to addition and the	$-12 \cdot (+5) \cdot -24$
	sign of the number that follows. Commutative property of addition allows	-12 + (+5) + -24
	grouping of like signs.	(-12 + -24) + (+5)
	Signs the same? Add the value of the terms	(12 + 2+) + (3)
	and give the result the same sign.	[-12 + -24 = -36]
	Substitute.	$(^{-36}) + (^{+5})$
	Signs different? Subtract and give the result	
	the sign of the higher value number.	[36 - 5 = 31]
		$(^{-3}6) + (^{+5}) = ^{-3}1$
	The simplified value of the expression is as	
	follows:	-2x - b + az = -31
38.	Substitute the values for the variables into the	
	expression.	$5(-8)^2 - 2(-8) + 2$
	PEMDAS: Evaluate the term with the exponent	
	first.	$[(-8)^2 = (-8)(-8) = +64]$
	Substitute the value into the numerical	
	expression.	5(+64) - 2(-8) + 2
	PEMDAS: Evaluate terms with multiplication	[5(+(4) 220]
55	next.	[5(+64) = 320]
-33	Substitute the values into the numerical	[2(-8) = -16]
	expression.	320 - (-16) + 2
	Change the subtraction to addition and the	520 (10) + 2
	sign of the number that follows.	320 + (+16) + 2
	Add terms from left to right. All term signs are	
	positive, a result of addition ⁺ .	320 + 16 + 2 = 338
	The simplified value of the expression is as	
	follows:	$5z^2 - 2z + 2 = 338$
39.	Substitute the values for the variables into the	
	expression.	$5(6)(\frac{1}{2}) \div 2(-5)$
	Consider the two terms on either side of	
	the division sign.	1 1
	Evaluate the first term by multiplying.	$[5 \cdot 6 \cdot \frac{1}{2} = (5 \cdot 6) \cdot \frac{1}{2} = 15]$
	Evaluate the second term.	[2(-5) = -10]

40.	Signs different? Divide and give the result a negative sign. The simplified value of the expression is as	$(15) \div (^{-}10)$ $[15 \div 10 = 1\frac{1}{2}]$ $(15) \div (^{-}10) = ^{-}1\frac{1}{2}$ $5xy \div 2b = ^{-}1\frac{1}{2} \text{ or } ^{-}1.5$
40.	 Substitute the values for the values into the expression. Evaluate the first term. Evaluate the second term. Substitute the values into the original numerical expression. Change the subtraction to addition and the sign of the number that follows. Add terms from left to right. The simplified value of the expression is as follows. 	42 + 2 + -8 42 + 2 + +8 = 52
41. 13	 Substitute the values for the variables into the expression. First, evaluate the term with the exponent. Multiply from left to right. Signs different? Multiply and give the result a negative sign. Signs the same? Multiply and give the result a positive sign. Substitute the values into the original numerical expression. Change division to multiplication and change the value to its reciprocal. The simplified value of the expression is as follows: 	$2(-5)^{2} \div \frac{1}{2}$ $[2(-5)^{2} = 2 \cdot (-5)(-5)]$ $[\{2 \cdot (-5)\} \cdot (-5)]$ $[2 \cdot (-5) = -10]$ $[(-10) \cdot (-5) = +50]$ $(+50) \div \frac{1}{2}$ $(+50) \cdot 2 = 100$ $\underline{2b^{2}} \div y = 100$
42.	 Substitute the values for the variables into the exp First, evaluate the expression inside the parenthes Signs different? Subtract and give the result the s of the higher value number. Substitute the result into the numerical expression Multiply from left to right. Negative times positir equals negative. Signs the same? Multiply and give the result a positive sign. The simplified value of the expression is as follow 	ses. $[(-8) + 3]$ ign [8 - 3 = 5] [(-8) + 3 = -5] in. $(-5)(6)(-5)$ ve $[-5 \cdot 6 = -30]$ $(-30) \cdot -5 = +150$

	43.	Substitute the values for the variables into the expression. First evaluate the expression inside the parentheses.	$6(\frac{1}{2})(-8 \div \frac{1}{2}) + 3(3)(-5)$
		Division by a fraction is the same as multiplication by its reciprocal.Substitute the result into the numerical expression.	$\begin{bmatrix} -8 \div \frac{1}{2} = -8 \cdot \frac{2}{1} = -16 \end{bmatrix}$ 6($\frac{1}{2}$)(-16) + 3(3)(-5)
		Evaluate the first term in the expression.	$[6(\frac{1}{2})(^{-1}6) = 6 \cdot \frac{1}{2} \cdot ^{-1}6]$ [3 \cdot -16 = -48]
		Evaluate the second term in the expression.	$[3(3)(^{-5}) = 3 \cdot 3 \cdot ^{-5}]$ [9 \cdot -5 = -45]
		Substitute the result into the numerical expression. Signs the same? Add the value of the terms	(-48) + (-45)
		and give the result the same sign. The simplified value of the expression is as follows:	-48 + -45 = -93 $\underline{6y(z \div y) + 3ab} = -93$
ł	44.	Substitute the values for the variables into the expression.	$2(-5)(6) \div ((-8) - (-5))$
I	- 7	First evaluate the expression inside the parentheses. Change the subtraction to addition and the	[(-85)]
ł		sign of the number that follows. Signs different? Subtract and give the result	[-8 + 5]
Ę	匑	the sign of the higher value number. Substitute the results into the numerical	[8-5=3] [-8++5=-3]
-		expression. Multiply from left to right.	$2(^{-5})(6) \div (^{-3})$ [2 \cdot -5 \cdot 6 = ^{-60}]
		Substitute the result into the numerical expression.	$(-60) \div -3$
		Signs the same? Divide and give the result	
		a positive sign.	$ \begin{bmatrix} 60 \div 3 = 20 \\ (^{-}60) \div ^{-}3 = 20 \end{bmatrix} $
		The simplified value of the expression is as follows:	$\underline{2bx} \div (z-b) = 20$

45. Substitute the values for the variables into the expression. $12(3)(-5) + (\frac{1}{2})$ Evaluate the first term. Multiply from left to right. $12(3)(-5) + (\frac{1}{2})$ Signs different? Multiply the numbers and give the result a negative sign. $136 \cdot 5 = 180$ Substitute the result into the numerical expression. $136 \cdot 5 = -180$ Division by a fraction is the same as multiplication by its reciprocal. $180 \cdot (\frac{1}{2})$ Signs different? Multiply numbers and give the result a negative sign. $180 \cdot (\frac{1}{2})$ The simplified value of the expression is as follows: $12ab \pm y = -360$ 46. Substitute the values for the variables into the expression. $12ab \pm y = -360$ 47. Substitute the values for the variables into the expression. $12ab \pm y = -360$ 48. Substitute the values for the variables into the expression. $12b \pm y = -360$ 49. Substitute the result into the numerical expression. $\frac{1}{2}(\frac{10}{2} - 3) - 4(3)$ FeMDAS: Division before subtraction. Substitute the result into the numerical expression. $\frac{1}{2}(\frac{10}{2} - 3) - 4(3)$ FeMDAS: Multiply before subtraction. Change subtraction to addition and the sign of the term that follows. $10 - 12 = 0 + -12 = -12$ Signs different? Multiply numbers and give the result a negative sign. $\frac{1}{2} \cdot 12 = 6$ The simplified value of the expression is as follows: $\frac{1}{2} \cdot 12 = 6$ Substitute the result into the numerical expression. $\frac{1}{2} \cdot 12 = 6$ Signs different? Multiply numbers and give the result a negative sign. $\frac{1}{2} \cdot 12 = 6$ Signs different? Multiply number

47. 48.	 Substitute the values for the variables into the expression. Evaluate the first term. Multiply from left to right. Evaluate the second term in the numerical expression. Multiply from left to right. Substitute the results into the numerical expression. Change subtraction to addition and the sign of the term that follows. Same signs? Add the value of the terms and give the result the same sign. The simplified value of the expression is as follows: Substitute the values for the variables into the expression. Evaluate the first term. Multiply from left to right. Evaluate the first term. Multiply from left to right. Evaluate the second term. Substitute the results into the numerical expression in the parentheses. Substitute the results into the numerical expression in the parentheses. Substitute the results into the numerical expression in the parentheses. Substitute the results into the numerical expression in the parentheses. Substitute the results into the numerical expression in the parentheses. 	$10(^{-5})^{3} - 4(^{-5})^{2}$ $[10(^{-5})^{3} = 10 \cdot ^{-5} \cdot ^{-5} \cdot ^{-5}]$ $[10 \cdot ^{-5} = (^{-5}0)]$ $[(^{-5}0) \cdot ^{-5} = ^{+2}50]$ $[^{+2}50 \cdot ^{-5} = ^{-1}, 250]$ $[4(^{-5})^{2} = 4 \cdot ^{-5} \cdot ^{-5}]$ $[4 \cdot ^{-5} = ^{-2}0]$ $[^{-2}0 \cdot ^{-5} = ^{+1}00]$ $^{-1}, 250 - ^{+1}00$ $[1, 250 + ^{-1}00$ $[1, 250 + ^{-1}00 = 1, 350]$ $10(^{-5})^{3} - 4(^{-5})^{2} = ^{-1}, 350$ $\frac{10b^{3} - 4b^{2} = ^{-1}, 350}{10(^{-5})^{3} - 4(^{-5})^{2} = ^{-1}, 350}$ $8(\frac{1}{2})((3)^{3} - 2(\frac{1}{2}))$ $((3)^{3} - 2(\frac{1}{2})) = (3^{3} - 2 \cdot \frac{1}{2})$ $[3^{3} = 3 \cdot 3 \cdot 3 = 9 \cdot 3 = 27]$ $[2 \cdot \frac{1}{2} = 1]$ $[(27) - (1)]$ $[27 - 1 = 26]$	
	expression. Multiply from left to right. The simplified value of the expression is as follows:	$8(\frac{1}{2})(26)$ [8 \cdot \frac{1}{2} = 4] [4 \cdot 26 = 104] $8y(a^3 - 2y) = 104$	

49.	Substitute the values for the variables into expression.Evaluate the first term.Signs the same? Multiply and give the resu a positive sign.Evaluate the second term.Multiply from left to right.	$\frac{(^{-}8)^2 - 4(3)^2(\frac{1}{2})}{[(^{-}8)^2 = ^{-}8 \cdot ^{-}8]}$
	Substitute the results into the numerical expression. Yes, you can just subtract. The simplified value of the expression is as follows:	$ \begin{array}{l} (64) - (18) \\ 64 - 18 = 46 \\ \underline{z^2 - 4a^2y = 46} \end{array} $
50.	 Substitute the values for the variables into the expression. PEMDAS: Evaluate the expression in the parentheses first. Change subtraction to addition and the sign of the term that follows. Substitute the result into the numerical expression. PEMDAS: Evaluate terms with exponents next. Substitute the result into the numerical expression. Multiply from left to right. Signs different? Multiply the values and give a negative sign. The simplified value of the expression is as follows: 	$3(6)^{2}(-5)(5(3) - 3(-5))$ $[(5(3) - 3(-5)) = 5 \cdot 3 - 3 \cdot -5]$ $[5 \cdot 3 - 3 \cdot -5 = 1515]$ $[15 + +15 = 30]$ $3(6)^{2}(-5)(30)$ $[(6)^{2} = 6 \cdot 6 = 36]$ $3(36)(-5)(30)$ $[3(36) = 108]$ $[(108) \cdot (-5) = -540]$ $[(-540) \cdot (30) = -16,200]$ $3(6)^{2}(-5)(5(3) - 3(-5)) = -16,200$ $\underline{3x^{2}b(5a - 3b) = -16,200}$

3

Combining Like Terms

In this chapter, you will practice simplifying algebraic expressions. As you do this, you will recognize and combine terms with variables that are alike and link them to other terms using the arithmetic operations. You should know that

- the numbers in front of the variable or variables are called coefficients.
- a coefficient is just a factor in an algebraic term, as are the variable or variables in the term.
- like terms can have different coefficients, but the configuration of the variables must be the same for the terms to be alike. For example, 3x and -4x are like terms but are different from 7ax or $2x^3$.

You can think of an algebraic term as a series of factors with numbers, and you can think of variables as factors. When the variables are given number values, you can multiply the factors of a term together to find its value, as you did in Chapter 2. When you have terms that are alike, you can add or subtract them as if they were signed numbers. You may find that combining like terms may be easier if you do addition by changing all subtraction to addition of the following term with its sign changed. This

strategy will continue to be shown in the answer explanations. But as you either know or are beginning to see, sometimes it's easier to just subtract.

You will also use the important commutative and associative properties of addition and multiplication. Another important and useful property is the distributive property. See the **Tips for Combining Like Terms**.

Tips for Combining Like Terms

Distributive Property of Multiplication

The distributive property of multiplication tells you how to multiply the terms inside a parentheses by the term outside the parentheses. Study the following general and specific examples.

 $\begin{array}{l} a(b+c) = ab + ac \\ a(b-c) = ab - ac \\ (b+c)a = ba + ca \\ 4(6+3) = 4 \cdot 6 + 4 \cdot 3 = 24 + 12 = 36 \\ (^{-5}+8)3 = ^{-5} \cdot 3 + 8 \cdot 3 = ^{-1}5 + 24 = 9 \\ 7(10+3) = 7 \cdot 10 + 7 \cdot 3 = 70 + 21 = 91 \\ 3(x+2y) = 3 \cdot x + 3 \cdot 2y = 3x + 6y \\ a(b-5d) = a \cdot b - a \cdot 5d = ab - 5ad \end{array}$

Numerical examples of the commutative properties for addition and multiplication were given in the **Tips for Working with Integers**. Now look at the following examples:

Commutative Property of Addition

a + b = b + a

This equation reminds us that terms being combined by addition can change their location (commute), but the value of the expression remains the same.

Commutative Property of Multiplication

 $x \cdot y = y \cdot x$

This equation reminds us that the order in which we multiply expressions can change without changing the value of the result.

Associative Property of Addition

(q+r) + s = q + (r+s)

This equation reminds us that when you are performing a series of additions of terms, you can associate any term with any other and the result will be the same.

Associative Property of Multiplication

 $(d \cdot e) \cdot f = d \cdot (e \cdot f)$

This equation reminds us that you can multiply three or more terms in any order without changing the value of the result.

Identity Property of Addition

n + 0 = n

Identity Property of Multiplication

 $n \cdot 1 = n$

Term Equivalents

 $x = 1 \cdot x$

For purposes of combining like terms, a variable by itself is understood to mean one of that term.

 $n = n^+$

A term without a sign in front of it is considered to be positive.

a + b = a - b = a - b

Adding a negative term is the same as subtracting a positive term. Look at the expressions on either side of the equal signs. Which one looks simpler? Of course, it's the last, a - b. Clarity is valued in mathematics. Writing expressions as simply as possible is always appreciated.

While it may not seem relevant yet, as you go through the practice exercises, you will see how each of these properties will come into play as we simplify algebraic expressions by combining like terms.

Simplify the following expressions by combining like terms.

51.
$$5a + 2a + 7a$$

52. $7a + 6b + 3a$
53. $4x + 2y - x + 3y$
54. $27 - 3m + 12 - 5m$
55. $7b + 6 + 2w - 3 + b$
56. $4(x + 2y) + 2(x + y)$
57. $3(2a + 3b) + 7(a - b)$
58. $11(4m + 5) + 3(^3m + 8)$
59. $64 + 5(n - 8) + 12n - 24$
60. $4(x + y - 4) + 6(2 - 3y)$
61. $-7(a + b) + 12a - 16b$
62. $14 + 9(2w + 7) - 2(6 - w)$
63. $8s - 3r + 5(2r - s)$
64. $6(3m - 12) - 4(9m + 8)$
65. $5(15 - 2j) + 11(7j - 3)$
66. $a(a + 4) + 3a^2 - 2a + 10$
67. $8(x - 7) + x(2 - x)$
68. $3r^2 + r(2 - r) + 6(r + 4)$
69. $2x - x(5 + y) + 3xy + 4(2x - y)$
70. $-7(c - 2d) + 21c - 3(d - 5)$
71. $5(3x - y) + x(5 + 2y) - 4(3 + x)$
72. $6(m - 3n) + 3m(n + 5) - 2n(3 - m)$
73. $9(2x - i) + 23xt + x(^{-4} + 5i)$
74. $4(2a(a + 3) + 6(4 - a)) + 5a^2$
75. $8(2a - b - 3c) + 3(2a - b) - 4(6 - b)$

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Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), {}, or [], perform operations in the innermost parentheses first and work outward.

7a + 3a + 6b

(10a) + 6b

(7a + 3a) + 6b

[(7a + 3a) = 10a]

7a + 6b + 3a = 10a + 6b

<u>Underlined</u> expressions show the simplified result.

- **51.** Use the associative property of addition.
Add like terms.(5a + 2a) + 7a
[5a + 2a = 7a]
(7a) + 7a
7a + 7a = 14a
5a + 2a + 7a = 14a**52.** Use the commutative property of addition to
- 52. Use the commutative property of addition to move like terms together.Use the associative property for addition.Add like terms.Substitute.The simplified result of the algebraic.
 - The simplified result of the algebraic expression is:

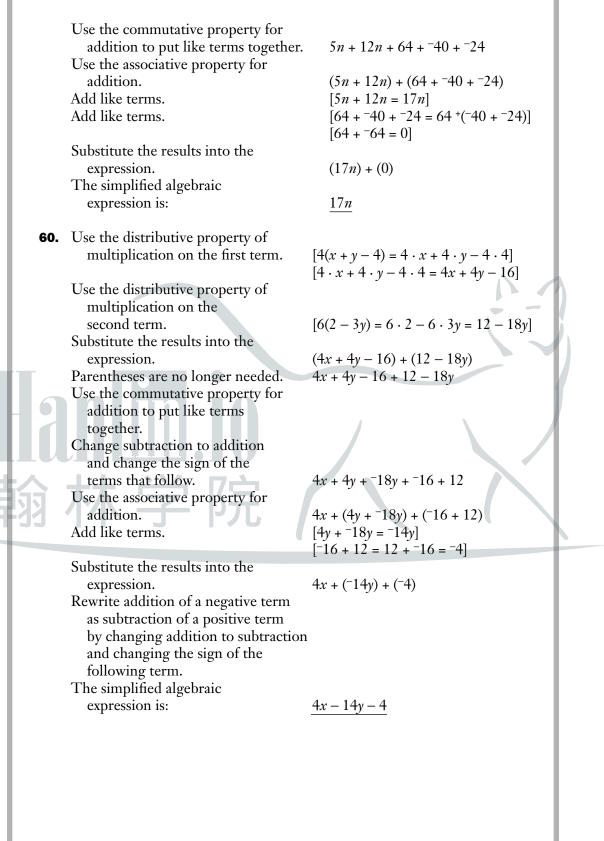
53.	Change subtraction to addition and	
	change the sign of the term	
	that follows.	4x + 2y + (-x) + 3y
	Use the commutative property of	
	addition to move like terms together.	4x + (-x) + 2y + 3y
	Use the associative property	
	for addition.	(4x + x) + (2y + 3y)
	Add like terms.	[4x + x = +3x = 3x]
		$[2\gamma + 3\gamma = 5\gamma]$
	Substitute the results into the	
	expression.	(4x + x) + (2y + 3y) = (3x) + (5y)
	The simplified algebraic	
	expression is:	4x + 2y - x + 3y = 3x + 5y
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	54.	Change subtraction to addition and change the sign of the term that follows. Use the commutative property for addition to put like terms	27 + -3m + 12 + -5m	
L		together.	27 + 12 + -3m + -5m	
		Use the associative property	(27, 12) (-2, -5,)	
		for addition.	(27 + 12) + (-3m + -5m)	
		Add like terms.	$\begin{bmatrix} 27 + 12 = 39 \end{bmatrix}$ $\begin{bmatrix} -3m + -5m = -8m \end{bmatrix}$	
L		Substitute the results into the	$\begin{bmatrix} 5m + 5m - 6m \end{bmatrix}$	
		expression.	(27 + 12) + (-3m + -5m) = (39) + (-8m)	
l		Rewrite addition of a negative term as subtraction of a positive term by changing addition to		
		subtraction and changing the		
L		sign of the following term.	39 - 8m = 39 - 8m	
		The simplified algebraic	27 2	
L		expression is:	$\frac{27 - 3m + 12 - 5m = 39 - 8m}{2}$	
h	55.	Change subtraction to addition and	hange subtraction to addition and change the	
H		sign of the term that follows.	7h + 6 + 2w + (-3) + h	
L		Use the commutative property for a		
H		to put like terms together.	7h + h + 2w + 6 + -3	
Ш		Use the associative property for add	ition. $(7b + b) + 2w + (6 + -3)$	
Ľ		Add like terms.	[(7b+b)=8b]	
Ŀ.	\wedge		$[(6 + ^{-3}) = 3]$	
k		Substitute the result into the express		
	JJ (The simplified algebraic expression	is: $\frac{8b+2w+3}{2w+3}$	
ŀ	56.	Use the distributive property of mul	tiplication	
L		on the first expression.	$[4(x+2y) = 4 \cdot x + 4 \cdot 2y]$	
L		1	[4x + 8y]	
		Use the distributive property of mul	2 24	
		on the second expression.	$[2(x+y) = 2 \cdot x + 2 \cdot y]$	
			[2x+2y]	
		Substitute the results into the expres		
		Use the commutative property of ad		
		to put like terms together.	4x + 2x + 8y + 2y	
		Use the associative property for add		
		Add like terms.	$\begin{bmatrix} 4x + 2x = 6x \end{bmatrix}$	
		Substitute the regults into the owner	[8y + 2y = 10y]	
		Substitute the results into the express The simplified algebraic expression		
L				

57.	Use the distributive property of multiplica	ntion
	on the first term.	$[3(2a + 3b) = 3 \cdot 2a + 3 \cdot 3b]$
		[6a+9b]
	Use the distributive property of	
	multiplication on the second term.	$[7(a-b) = 7 \cdot a - 7 \cdot b]$
		[7a - 7b]
	Substitute the results into the expression.	(6a + 9b) + (7a - 7b)
		6a + 9b + 7a - 7b
	Change subtraction to addition and change	e
	the sign of the term that follows.	6a + 9b + 7a + (-7b)
	Use the commutative property for additio	n
	to put like terms together.	6a + 7a + 9b + (-7b)
	Use the associative property for addition.	(6a + 7a) + (9b + -7b)
	Add like terms.	[6a + 7a = 13a]
	Signs different? Subtract the value of	
	the terms.	[9b + -7b = 2b]
	Substitute the result into the expression.	(13a) + (2b) -
	The simplified algebraic expression is:	$\frac{13a+2b}{2}$
58.	Use the distributive property of	
	multiplication on the first term.	$[11(4m+5) = 11 \cdot 4m + 11 \cdot 5]$
	multiplication on the first term.	[44m + 55]
	Use the distributive property of	
	multiplication on the second term.	$[3(^{-}3m + 8) = 3 \cdot ^{-}3m + 3 \cdot 8]$
	r	[-9m + 24]
	Substitute the result into the expression.	(44m + 55) + (-9m + 24)
		44m + 55 + -9m + 24
I TT	Use the commutative property for	
F33	addition to put like terms together.	44m + -9m + 55 + 24
	Use the associative property for	
	addition.	(44m + -9m) + (55 + 24)
	Add like terms.	$[44m + {}^{-}9m = 35m]$
		[55 + 24 = 79]
	Substitute the result into the expression.	(35m) + (79)
	The simplified algebraic expression is:	35m + 79
59	Use the distributive property of	
		$[5(n-8) = 5 \cdot n - 5 \cdot 8]$
	*	[5n - 40]
	Substitute the result into the	
		64 + (5n - 40) + 12n - 24
	*	64 + 5n - 40 + 12n - 24
	Change subtraction to addition	
	and change the sign of the term	
		64 + 5n + 40 + 12n + 24



61.	 Use the distributive property of multiplication on the first term. Substitute the results into the expression. Parentheses are no longer needed. Use the commutative property for addition to put like terms together. Change subtraction to addition and change the sign of the terms that follow. Use the associative property for addition. Add like terms. Substitute the results into the expression. Adding a negative term is the same as subtracting a positive term. 	on $\begin{bmatrix} -7(a+b) = -7 \cdot a + -7 \cdot b \\ (-7a + -7b) + 12a - 16b \\ -7a + -7b + 12a - 16b \\ 12a + -7a + -7b - 16b \\ 12a + -7a + -7b + -16b \\ (12a + -7a) + (-7b + -16b) \\ [12a + -7a = 5a] \\ [-7b + -16b = -23b] \\ (5a) + (-23b) \\ \underline{5a - 23b} \end{bmatrix}$
62.	Change subtraction to addition and change the sign of the terms that follow. Use the distributive property of multiplication on the second term.	$[9(2w + 7) = 9 \cdot 2w + 9 \cdot 7]$
多	 Use the distributive property of multiplication on the third term. Notice the result of multiplication for opposite and like-signed terms. Substitute the results into the original expression. Parentheses are no longer needed. Use the commutative property of addition to put like terms together. Use the associative property for addition. Add like terms. Add from left to right. Substitute the results into the expression. Parentheses are no longer needed. 	$[9 \cdot 2w + 9 \cdot 7 = 18w + 63]$ $[-2(6 + -w) = -2 \cdot 6 + -2 \cdot -w]$ $[-2 \cdot 6 + -2 \cdot -w = -12 + +2w]$ 14 + (18w + 63) + (-12 + +2w) 14 + 18w + 63 + -12 + +2w 18w + +2w + 14 + 63 + -12 (18w + +2w) + (14 + 63 + -12) [18w + +2w = 20w] [14 + 63 + -12 = 77 + -12 = 65] (20w) + (65) 20w + 65

63.	 Change subtraction to addition and change the sign of the terms that follow. Use the distributive property of multiplication on the third term. Substitute the results into the expression. Parentheses are no longer needed. Use the commutative property of addition to put like terms together. Use the associative property for addition. Add like terms. Substitute the results into the expression. Parentheses are no longer needed. 	$8s + -3r + 5(2r + -s)$ $[5(2r + -s) = 5 \cdot 2r + 5 \cdot -s]$ $[5 \cdot 2r + 5 \cdot -s = 10r + -5s]$ $8s + -3r + (10r + -5s)$ $8s + -3r + 10r + -5s$ $8s + -5s + 10r + -3r$ $(8s + -5s) + (10r + -3r)$ $[8s + -5s = 3s]$ $[10r + -3r = 7r]$ $(3s) + (7r)$ $3s + 7r$
64.	 Change subtraction to addition and change the sign of the terms that follow. Use the distributive property of multiplication on the first term. Use the distributive property of multiplication on the second term. Substitute the results into the expression. Parentheses are no longer needed. Use the commutative property of addition to put like terms together. Use the associative property for addition. Add terms using the rules for terms with different signs. Add terms using the rules for terms with the same signs. Substitute the results into the expression. Parentheses are no longer needed. Add terms using the rules for terms with different signs. Add terms using the rules for terms with the same signs. Substitute the results into the expression. Parentheses are no longer needed. Addition a negative term is the same as subtracting a positive term. Use the commutative property of addition. Change addition to subtraction and change the sign of the term that follows. Either of the last two expressions is correct, but the second is the simpler: 	

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	65.	Change subtraction to addition and	
		change the sign of the terms that follow.	5(15 + 2j) + 11(7j + 3)
		Use the distributive property of	
		multiplication on the first term.	$[5(15 + ^{-}2j) = 5 \cdot 15 + 5 \cdot ^{-}2j]$
			$[5 \cdot 15 + 5 \cdot {}^{-2}j = 75 + {}^{-1}0j]$
		Use the distributive property of	
1		multiplication on the second term.	$[11(7j + {}^{-3}) = 11 \cdot 7j + 11 \cdot {}^{-3}]$
1			$[11 \cdot 7j + 11 \cdot ^{-3} = 77j + ^{-3}3]$
1		Substitute the results into the	
1		expression.	(75 + -10j) + (77j + -33)
		Parentheses are no longer needed.	75 + -10j + 77j + -33
		Use the commutative property of	
		addition to put like terms together.	77j + -10j + 75 + -33
		Use the associative property for	
		addition.	$(77j + ^{-1}0j) + (75 + ^{-3}3)$
		Add terms using the rules for terms	
		with different signs.	$[77j + ^{-1}0j = ^{+}67j]$
		Add terms using the rules for terms	[7522 + 42]
		with different signs.	[75 + -33 = +42]
ł		Substitute the results into the	(67:) (12)
l		expression. Parentheses are no longer needed.	(67j) + (42) 67i + 42
l		r arentheses are no longer needed.	67j + 42
l	66	Change subtraction to addition and change	
l		the sign of the terms that follow.	$a(a + 4) + 3a^2 + -2a + 10$
Į		Use the distributive property of	
d		multiplication on the first term.	$[a(a+4) = a \cdot a + a \cdot 4]$
ļ	6.	Use the commutative property for	
Į		multiplication for the second term.	$[a \cdot a + a \cdot 4 = a^2 + 4a]$
1	33	Substitute the results into the expression.	$(a^2 + 4a) + 3a^2 + -2a + 10$
1		Parentheses are no longer needed.	$a^2 + 4a + 3a^2 + -2a + 10$
		Use the commutative property of addition	
		to put like terms together.	$a^2 + 3a^2 + 4a + -2a + 10$
		Use the associative property for addition.	$(a^2 + 3a^2) + (4a + -2a) + 10$
		Add the first term using the rules for	
		terms with the same signs.	$[a^2 + 3a^2 = 4a^2]$
		Add the second term using the rules for	
		terms with different signs.	[4a + 2a = 2a]
		Substitute the results into the expression.	$(4a^2) + (2a) + 10$
		Parentheses are no longer needed.	$\frac{4a^2+2a+10}{2}$
		Parentheses are no longer needed.	$\frac{4a^2 + 2a + 10}{4a^2 + 2a + 10}$

67.	Change subtraction to addition and change		
	the sign of the terms that follow.	8(x + 7) + x(2 + x)	
	Use the distributive property of	· · · · · · · · · · · · · · · · · · ·	
	multiplication on the first term.	$[8(x + ^{-7}) = 8 \cdot x + 8 \cdot ^{-7}]$	
		$[8 \cdot x + 8 \cdot ^{-7} = 8x + ^{-56}]$	
	Use the distributive property of		
	multiplication on the second term.	$[x(2 + x) = x \cdot 2 + x \cdot x]$	
	multiplication on the second term.	$[x \cdot 2 + x \cdot -x = 2x + -x^2]$	
	Substitute the regults into the every	$[x \cdot 2 + x \cdot x = 2x + x]$ (8x + -56) + 2x + -x ²	
	Substitute the results into the expression.	(3x + 56) + 2x + x $8x + 56 + 2x + x^2$	
	Parentheses are no longer needed.	$3x + 30 + 2x + x^{-1}$	
	Use the commutative property of addition	9 - 2 - 5(-2)	
	to put like terms together.	$8x + 2x + 56 + x^2$	
	Use the associative property for addition.	$(8x + 2x) + {}^{-5}6 + {}^{-}x^2$	
	Add terms in parentheses using the rules	(10) π (2)	
	for terms with the same signs.	$(10x) + {}^{-56} + {}^{-}x^2$	
	Change addition to subtraction and change	$10x - (+56) + -x^2$	
	the sign of the term that follows.	$10x - (+56) + -x^2$	
	Use the commutative property of addition		
	to put the terms in exponential order.	$\frac{-x^2 + 10x - 56}{-x^2 + 10x - 56}$	
68.	Change subtraction to addition and change		
	the sign of the terms that follow.	$3r^2 + r(2 + r) + 6(r + 4)$	
	Use the distributive property of		
	multiplication on the second term.	$[r(2 + -r) = r \cdot 2 + r \cdot -r]$ [r \cdot 2 + r \cdot -r = 2r + -r^2]	
		$[r \cdot 2 + r \cdot \overline{r} = 2r + \overline{r^2}]$	
	Use the distributive property of		
	multiplication on the third term.	$[6(r+4) = 6 \cdot r + 6 \cdot 4]$	
22		$[6 \cdot r + 6 \cdot 4 = 6r + 24]$	
11	Substitute the results into the expression.	$3r^2 + (2r + r^2) + (6r + 24)$	
	Remove the parentheses.	$3r^2 + 2r + r^2 + 6r + 24$	
	Use the commutative property of addition		
	to put like terms together.	$3r^2 + r^2 + 2r + 6r + 24$	
	Use the associative property for addition.	$(3r^2 + r^2) + (2r + 6r) + 24$	
	Add the first term using the rules for		
	terms with different signs.	$[3r^2 + r^2 = 2r^2]$	
	Add the second term using the rules for		
	terms with the same signs.	[2r + 6r = 8r]	
	Substitute the results into the expression.	$(2r^2) + (8r) + 24$	
	Remove the parentheses.	$2r^2 + 8r + 24$	

60	Change subtraction to addition and	
09.	Change subtraction to addition and the sign of the terms that follow.	2x + x(5 + y) + 3xy + 4(2x + y)
	Use the distributive property of	$2x + x(3 + y) + 3xy + \tau(2x + y)$
	multiplication on the second term.	$[-x(5 + y) = -x \cdot 5 + -x \cdot y]$
	Use the rules for multiplying	$[x(y+y) = x \cdot y + x \cdot y]$
	signed terms.	$\begin{bmatrix} -x \cdot 5 + -x \cdot y &= -5x + -xy \end{bmatrix}$
	Use the distributive property of	$\begin{bmatrix} x \cdot y + x \cdot y = yx + xy \end{bmatrix}$
	multiplication on the fourth term.	$[4(2x + -y) = 4 \cdot 2x + 4 \cdot -y]$
	Use the rules for multiplying	$\left[1(2x+y)-1(2x+1)y\right]$
	signed terms.	$[4 \cdot 2x + 4 \cdot y = 8x + 4y]$
	Substitute the results into the	$\begin{bmatrix} 1 & 2x \\ 1 & 1 \end{bmatrix} = \begin{bmatrix} 0x \\ 1 & 1 \end{bmatrix}$
	expression.	2x + (-5x + -xy) + 3xy + (8x + -4y)
	Remove the parentheses.	2x + (5x + xy) + 5xy + (5x + 1y) 2x + 5x + xy + 3xy + 8x + 4y
	Use the associative and commutative	201 201 001 001 000
	properties for addition.	(2x + 5x + 8x) + (xy + 3xy) + (4y)
	Add the first set of terms using the	
	rules for terms with different signs.	[2x + 5x + 8x = 5x]
	Add the second set of terms using the	[]
	rules for terms with different signs.	[-xy + 3xy = 2xy]
	Substitute the results into the	
	expression.	(-5x) + (2xy) + (-4y)
	Remove the parentheses.	5x + 2xy - 4y
70.	Change subtraction to addition and the	
	sign of the terms that follow.	-7(c + -2d) + 21c + -3(d + -5)
	Use the distributive property of	
	multiplication on the first term.	$[^{-7}(c + ^{-2}d) = ^{-7} \cdot c + ^{-7} \cdot ^{-2}d]$
	Use the rules for multiplying	
	signed terms.	$[^{-7} \cdot c + ^{-7} \cdot ^{-2}d = ^{-7}c + ^{+1}4d]$
	Use the distributive property of	
	multiplication on the third term.	$[^{-3}(d + ^{-5}) = ^{-3} \cdot d + ^{-3} \cdot ^{-5}]$
	Use the rules for multiplying	
	signed terms.	$[-3 \cdot d + -3 \cdot -5 = -3d + +15]$
	Substitute the results into the	
	last expression.	(-7c + +14d) + 21c + (-3d + +15)
	Remove the parentheses.	-7c + +14d + 21c + -3d + +15
	Use the commutative property of	
	addition to move terms together.	$21c + ^{-7}c + ^{+1}4d + ^{-3}d + ^{+1}5$
	Use the associative property for	(21 + -7) + (+1) + -2 + +15
	addition.	(21c + -7c) + (+14d + -3d) + +15
	Combine like terms using addition	(14.) + $(11.d)$ + 15
	rules for signed numbers.	(14c) + (11d) + 15 14c + 11d + 15
	Remove the parentheses.	$\frac{17l + 11l + 13}{17l}$

$$\begin{aligned} + &-5x + 8x = 5x] \\ y + &3xy = 2xy] \\ x) + &(2xy) + (^{-}4y) \\ &+ &2xy - 4y \\ \hline &-7(c + ^{-}2d) + 21c + ^{-}3(d + ^{-}5) \\ &[^{-}7(c + ^{-}2d) = ^{-}7 \cdot c + ^{-}7 \cdot ^{-}2d] \\ &[^{-}7(c + ^{-}2d) = ^{-}7 \cdot c + ^{-}7 \cdot ^{-}2d] \\ &[^{-}7(c + ^{-}2d) = ^{-}7c + ^{+}14d] \\ &[^{-}3(d + ^{-}5) = ^{-}3 \cdot d + ^{-}3 \cdot ^{-}5] \\ &[^{-}3 \cdot d + ^{-}3 \cdot ^{-}5 = ^{-}3d + ^{+}15] \end{aligned}$$

71. Change subtraction to addition and the sign of the terms that follow. Use the distributive property of multiplication on the first term. Use the rules for multiplying signed terms. Use the distributive property of multiplication on the second term. Use the rules for multiplying signed terms. Use the distributive property of multiplication on the third term. Use the rules for multiplying signed terms. Substitute the results into the original expression. Remove the parentheses. Use the commutative property of addition to move like terms together. Use the associative property for addition. Combine like terms using addition rules for signed numbers. Adding a negative term is the same as subtracting a positive term. Remove the parentheses.

5(3x + -y) + x(5 + 2y) + -4(3 + x) $[5(3x + -y) = 5 \cdot 3x + 5 \cdot -y]$ $[5 \cdot 3x + 5 \cdot -y = 15x + -5y]$ $[x(5 + 2y) = x \cdot 5 + x \cdot 2y]$ $[x \cdot 5 + x \cdot 2y = 5x + 2xy]$ $[-4(3 + x) = -4 \cdot 3 + -4 \cdot x]$ $[-4 \cdot 3 + -4 \cdot x = -12 + -4x]$ (15x + -5y) + (5x + 2xy) + (-12 + -4x) 15x + -5y + 5x + 2xy + -12 + -4x (15x + 5x + -4x) + -5y + 2xy + -12 (16x) + -5y + 2xy - (+12) (16x) - (+5y) + 2xy - (+12)16x - 5y + 2xy - 12

- **72.** Change subtraction to addition and the sign of the terms that follow. Use the distributive property of multiplication on the first term. Use the rules for multiplying signed terms. Use the distributive property of multiplication on the second term. Use the rules for multiplying signed terms. Use the distributive property of multiplication on the third term. Use the rules for multiplying signed terms. Substitute the results into the original expression. Remove the parentheses. Use the commutative property of addition to move like terms together. Use the associative property for addition. Combine like terms using addition rules for signed numbers. Adding a negative term is the same as subtracting a positive term.
- 73. Change subtraction to addition and the sign of the terms that follow.
 Use the distributive property of multiplication on the first term.
 Use the rules for multiplying signed terms.
 Use the distributive property of multiplication on the third term.
 Use the rules for multiplying signed terms.
 Substitute the results into the expression.
 Remove the parentheses.

 $6(m + {}^{-}3n) + 3m(n + 5) + {}^{-}2n(3 + {}^{-}m)$ $[6(m + {}^{-}3n) = 6 \cdot m + 6 \cdot {}^{-}3n]$ $[6 \cdot m + 6 \cdot {}^{-}3n = 6m + {}^{-}18n]$ $[3m(n + 5) = 3m \cdot n + 3m \cdot 5]$ $[3m \cdot n + 3m \cdot 5 = 3mn + 15m]$ $[{}^{-}2n(3 + {}^{-}m) = {}^{-}2n \cdot 3 + {}^{-}2n \cdot {}^{-}m]$ $[{}^{-}2n \cdot 3 + {}^{-}2n \cdot {}^{-}m = {}^{-}6n + {}^{+}2mn]$

 $(6m + {}^{-1}8n) + (3mn + 15m) + ({}^{-}6n + {}^{+}2mn)$ $6m + {}^{-1}8n + 3mn + 15m + {}^{-}6n + {}^{+}2mn$

$$(6m + 15m) + (3mn + 2mn) + (-6n + -18n)$$

$$(21m) + (5mn) + (-24n)$$

21m + 5mn - 24n

9(2x + -t) + 23xt + x(-4 + 5t) $[9(2x + -t) = 9 \cdot 2x + 9 \cdot -t]$ $[9 \cdot 2x + 9 \cdot -t = 18x + -9t]$ $[x(-4 + 5t) = x \cdot -4 + x \cdot 5t]$ $[x \cdot -4 + x \cdot 5t = -4x + 5xt]$ (18x + -9t) + 23xt + (-4x + 5xt) 18x + -9t + 23xt + -4x + 5xt

	Use the commutative property of addition to move like terms together.	$18x + {}^{-}\!4x + {}^{-}\!18t + 23xt + 5xt$
	Use the associative property for addition.	(18x + -4x) + -9t + (23xt + 5xt)
	Combine like terms using addition	
	rules for signed numbers. Adding a negative term is the same as	$(14x) + {}^{-9}t + (28xt)$
	subtracting a positive term.	$14x - {}^{+}9t + 28xt$
		$\frac{14x - 9t + 28xt}{14x - 9t + 28xt}$
74.	Change subtraction to addition and the sign	
	of the terms that follow.	$4\{2a(a+3)+6(4+a)\}+5a^2$
	Simplify the term inside the outer parentheses first.	[2a(a+3)+6(4+a)]
	Use the distributive property of	
	multiplication on the first term. Use the rules for multiplying signed terms.	$[2a(a + 3) = 2a \cdot a + 2a \cdot 3]$ [2a \cdot a + 2a \cdot 3 = 2a ² + 6a]
	Use the distributive property of	$[2u \cdot u + 2u \cdot 3 = 2u + 6u]$
	multiplication on the second term.	$[6(4 + -a) = 6 \cdot 4 + 6 \cdot -a]$
	Use the rules for multiplying signed terms. Substitute the results into the expression.	$[6 \cdot 4 + 6 \cdot a = 24 + 6a]$ [(2a ² + 6a) + (24 + 6a)]
	Remove the parentheses.	$[2a^{2} + 6a + 24 + -6a]$
6	Use the commutative property of addition.	$[2a^2 + 6a + -6a + 24]$
	Use the associative property for addition. Combine like terms using addition rules	$[2a^2 + (6a + {}^{-}6a) + 24]$
	for signed numbers.	$[2a^2 + (0) + 24]$
$\mathbf{\nabla}$	Use the identity property of addition.	$[2a^2 + 24]$
	Substitute the results into the expression. Use the distributive property of	$4\{2a^2 + 24\} + 5a^2$
	multiplication on the first term.	$[4 \cdot 2a^2 + 4 \cdot 24]$
	Substitute into the companying	$[8a^2 + 96]$
	Substitute into the expression. Remove the parentheses.	$(8a^2 + 96) + 5a^2 8a^2 + 96 + 5a^2$
	Use the commutative property of addition.	$8a^2 + 5a^2 + 96$
	Use the associative property for addition.	$(8a^2 + 5a^2) + 96$
	Add like terms.	$13a^2 + 96$

75.	Change subtraction to addition and the sign of the terms that follow	9(2a+-b+-
	that follow. Use the distributive property of multiplication on the	8(2a + b + b)
	first term. Use the rules for multiplying	[8(2a + b +
	signed terms.	$[8 \cdot 2a + 8 \cdot$
	Use the distributive property of multiplication on the	
	second term. Use the rules for multiplying	[3(2a + b) =
	signed terms. Use the distributive property	$[3\cdot 2a+3\cdot$
	of multiplication on the	
	third term. Use the rules for multiplying	[-4(6 + -b) =
	signed terms. Substitute the results into	$[-4 \cdot 6 + -4 \cdot$
	the expression.	(16a + -8b +
	Remove the parentheses.	16a + -8b +
1	Use the commutative property of addition to move	
	like terms together. Use the associative property	16 <i>a</i> + 6 <i>a</i> + ⁻
	for addition.	(16a + 6a) +
	Combine like terms using addition rules for	
	signed numbers.	(22a) + (-7b)
	Adding a negative term	
	is the same as subtracting a	
	positive term.	$\frac{22a-7b-2}{2}$

(-3c) + 3(2a + b) + (-4(6 + b)) $(-3c) = 8 \cdot 2a + 8 \cdot (-b) + 8 \cdot (-3c)$ $b^{-}b + 8 \cdot {}^{-}3c = 16a + {}^{-}8b + {}^{-}24c$ $= 3 \cdot 2a + 3 \cdot b]$ -b = 6a + -3b] $= -4 \cdot 6 + -4 \cdot -b$] $\cdot b = 24 + 4b$ (-24c) + (6a + -3b) + (-24 + +4b)-24c + 6a + -3b + -24 + +4b-8b + -3b + +4b + -24c + -24+(-8b+-3b++4b)+-24c+-24b) + $^{-}24c$ + $^{-}24$

24*c* – 24

Solving Basic Equations

4

Solving equations is not very different from working with numerical or algebraic expressions. An equation is a mathematical statement where two expressions are set equal to each other. Using logic and mathematical operations, you can manipulate the equation to find a solution. Simply put, that is what you have done when you have the variable on one side of the equal sign and a number on the other. The answer explanations will show and identify all the steps you will need to solve basic equations. There will be different solutions to similar problems to show a variety of methods for solving equations. But they all rely on the same rules. Look over the **Tips for Solving Basic Equations** before you begin this chapter's questions.

Tips for Solving Basic Equations

- If a number is being added to or subtracted from a term on one side of an equation, you can eliminate that number by performing the inverse operation.
- The inverse of addition is subtraction. The inverse of subtraction is addition. If you add or subtract an amount from one side of the equation, you must do the same to the other side to maintain the equality.

- The inverse of multiplication is division. If a variable is being multiplied by a coefficient, you can eliminate the coefficient by dividing both sides of the equation by that coefficient, leaving you with just one of the variables. If *a* is a number ≠ 0, then *ax* ÷ *a* = *x*.
- The inverse of division is multiplication. If a number is dividing a variable, you can multiply the term by the number, leaving you with one of the variables. If *b* is a number $\neq 0$, then $b(\frac{y}{b}) = y$.
- You can perform any operation to a term in an equation. Just remember that you must do it to both sides. When you have the variable isolated on one side of the equation, the value on the other side is your solution.

76. *a* + 21 = 32

- **77.** x 25 = 32**78.** y + 17 = -12
- **79.** b 15 = 71

81. s - -4 = -1**82.** $a + 1\frac{3}{4} = 6\frac{1}{4}$

83. $b - \frac{5}{2} = -\frac{2}{3}$

84. $c - 4(\frac{1}{2} - 5) = 20$

85. m + 2(5 - 24) = -76

80. 12 - c = -9

87. 4x = -20**88.** -3y = 18

86. 2a = 24

- **89.** 27*b* = 9
- **90.** 45r = -30
- **91.** 0.2*c* = 5.8
- **92.** $\frac{x}{7} = 16$
- **93.** $\frac{y}{-4} = -12$
- **94.** $\frac{2}{3}a = 54$
- **95.** $\frac{8}{5}b = -56$

- **96.** Jack paid \$21,000 for his new car. This was $\frac{7}{8}$ the suggested selling price of the car. What was the suggested selling price of the car?
- **97.** After putting 324 teddy bears into packing crates, there were 54 crates filled with bears. If each crate contained the same number of bears, how many bears were in each packing crate?
- **98.** Only 3% of turtle hatchlings will live to become breeding adults. How many turtles must have been born if the current number of breeding adults is 1,200?
- **99.** This year, a farmer planted 300 acres of corn. This was 1.5 times as many acres as he planted last year. How many acres did he plant this year?
- **100.** A business executive received a \$6,000 bonus check from her company at the end of the year. This was 5% of her annual salary. How much was her annual salary before receiving the bonus?

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Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

<u>Underlined</u> equations show the simplified result.

Subtract 21 from both sides of the equation.Associate like terms.Perform the numerical operation in the parentheses.Zero is the identity element for addition.	a + (21 - 21) = (32 - 21) $a + (0) = (11)$ $a = 11$
Add 25 to each side of the equation.Use the commutative property for addition.Associate like terms.Perform the numerical operation in the parentheses.Zero is the identity element for addition.	25 + x - 25 = 32 + 25 x + 25 - 25 = 32 + 25 x + (25 - 25) = (32 + 25) x + (0) = (57) x = 57
Associate like terms.	y + 17 - 17 = -12 - 17 y + (17 - 17) = (-12 - 17)
change the sign of the term that follows. Apply the rules for operating with signed numbers. Zero is the identity element for addition.	$y + (17 + ^{-}17) = (^{-}12 + ^{-}17)$ $y + (0) = ^{-}29$ $y = ^{-}29$
Change subtraction to addition and change the sign of the term that follows.Add +15 to each side of the equation.Associate like terms.Apply the rules for operating with signed numbers.Zero is the identity element for addition.	$b + {}^{-1}5 = 71$ $b + {}^{-1}5 + {}^{+1}5 = 71 + {}^{+1}5$ $b + ({}^{-1}5 + 15) = (71 + 15)$ b + (0) = 86 b = 86
	 Perform the numerical operation in the parentheses. Zero is the identity element for addition. Add 25 to each side of the equation. Use the commutative property for addition. Associate like terms. Perform the numerical operation in the parentheses. Zero is the identity element for addition. Subtract 17 from both sides of the equation. Associate like terms. Change subtraction to addition and change the sign of the term that follows. Apply the rules for operating with signed numbers. Zero is the identity element for addition. Change subtraction to addition and change the sign of the term that follows. Apply the rules for operating with signed numbers. Add *15 to each side of the equation. Associate like terms. Apply the rules for operating with signed numbers.

Change subtraction to addition and change the sign of the term that follows. Add ⁺ <i>c</i> to each side of the equation. Associate like terms.	$12 + {}^{-}c = {}^{-}9$ $12 + {}^{-}c + {}^{+}c = {}^{-}9 + {}^{+}c$ $12 + ({}^{-}c + {}^{+}c) = {}^{-}9 + {}^{+}c$ $12 + (0) = {}^{-}9 + c$ $12 - {}^{-}0$
Add +9 to each side of the equation.Associate like terms.Apply the rules for operating with signed numbers.Zero is the identity element for addition.	12 = -9 + c +9 + 12 = +9 + -9 + c (+9 + 12) = (+9 + -9) + c (21) = (0) + c <u>21 = c</u>
Change subtraction to addition and change the sign of the term that follows. Add ⁻⁴ to each side of the equation. Associate like terms. Apply the rules for operating with signed numbers. Subtracting zero is the same as adding zero.	$s + {}^{+}4 = {}^{-}1$ $s + {}^{+}4 + {}^{-}4 = {}^{-}1 + {}^{-}4$ $s + ({}^{+}4 + {}^{-}4) = {}^{-}1 + {}^{-}4$ $s + (0) = ({}^{-}5)$ $\underline{s = {}^{-}5}$
 Add ⁻¹³/₄ to each side of the equation. Associate like terms. Apply the rules for operating with signed numbers. Zero is the identity element for addition. 	$a + 1\frac{3}{4} + -1\frac{3}{4} = 6\frac{1}{4} + -1\frac{3}{4}$ $a + (1\frac{3}{4} + -1\frac{3}{4}) = 6\frac{1}{4} + -1\frac{3}{4}$ $a + (0) = 4\frac{1}{2}$ $\underline{a = 4\frac{1}{2}}$
 Change subtraction to addition and change the sign of the term that follows. Subtract -⁵/₂ from both sides of the equation. Associate like terms. Change subtraction to addition and change the sign of the term that follows. Apply the rules for operating with signed numbers. Change the improper fraction to a mixed number. 	$b + \frac{-5}{2} = -\frac{2}{3}$ $b + \frac{-5}{2} - \frac{-5}{2} = -\frac{2}{3} - \frac{-5}{2}$ $b + (-\frac{5}{2} - \frac{-5}{2}) = -\frac{2}{3} - \frac{-5}{2}$ $b + (-\frac{5}{2} + \frac{+5}{2}) = -\frac{2}{3} + \frac{+5}{2}$ $b + (0) = \frac{11}{6}$ $\underline{b} = 1\frac{5}{6}$
	 the sign of the term that follows. Add *c to each side of the equation. Associate like terms. Apply to each side of the equation. Associate like terms. Apply the rules for operating with signed numbers. Zero is the identity element for addition. Change subtraction to addition and change the sign of the term that follows. Add ⁻⁴ to each side of the equation. Associate like terms. Apply the rules for operating with signed numbers. Add ⁻⁴ to each side of the equation. Associate like terms. Apply the rules for operating with signed numbers. Subtracting zero is the same as adding zero. Add ⁻¹³/₄ to each side of the equation. Associate like terms. Apply the rules for operating with signed numbers. Zero is the identity element for addition. Change subtraction to addition and change the sign of the term that follows. Subtract ⁻⁵/₂ from both sides of the equation. Associate like terms. Change subtraction to addition and change the sign of the term that follows. Subtract ⁻⁵/₂ from both sides of the equation. Associate like terms. Change subtraction to addition and change the sign of the term that follows. Apply the rules for operating with signed numbers.

	oor Algebra Questions	
84.	Change subtraction to addition and change the sign of the term that follows. $c + -4(\frac{1}{2} + -5) = 20$ Use the distributive property of multiplication. $c + (-4 \cdot \frac{1}{2} + -4 \cdot -5) = 20$ Perform the operation in parentheses. $c + (-4 \cdot \frac{1}{2} + -4 \cdot -5) = 20$ Apply the rules for operating with signed numbers. $c + (18) = 20$ Subtract 18 from both sides of the equation. $c + 18 - 18 = 20 - 18$ Associate like terms. $c + (18 - 18) = 20 - 18$ Perform the operation in parentheses. $c + 0 = 2$ Zero is the identity element for addition. $c = 2$	
85.	Use the distributive property of multiplication. $m + (2 \cdot 5 - 2 \cdot 24) = -76$ The order of operations is to multiply first. $m + (10 - 48) = -76$ Add +38 to each side of the equation. $m + -38 + +38 = -76 + +38$ Associate like terms. $m + (-38 + +38) = -76 + +38$ Apply the rules for operating with signed numbers. $m + (0) = -38$ $m = -38$	
86.	Divide both sides of the equation by 2. $2a \div 2 = 24 \div 2$	
87.	Apply the rules for operating with signed numbers. $a = 24 \div 2$ Another method is as follows: $\frac{a = 12}{\frac{2a}{2} = \frac{24}{2}}$ Divide both sides of the equation by 4. $4x \div 4 = -20 \div 4$	
匑	Apply the rules for operating with signed numbers. Another look for this solution method is as follows: $\frac{x = -20 \div 4}{\frac{4x}{4} = -\frac{20}{4}}$ $\frac{x = -5}{\frac{4x}{4} = -\frac{20}{4}}$	
88.	Divide both sides of the equation by -3. $\frac{-3\gamma}{-3} = \frac{18}{-3}$	
	Apply the rules for operating with signed numbers. $y = \frac{18}{-3}$ y = -6	
89.	Divide both sides of the equation by 27. $\frac{27b}{27} = \frac{9}{27}$ $b = \frac{9}{27}$	
	Reduce fractions to their simplest form. $b = \frac{1}{3}$	
90.	Divide both sides of the equation by 45. $\frac{45r}{45} = \frac{-30}{45}$ $r = \frac{-30}{45}$	
	Reduce fractions to their simplest form (common factor of 15). $\frac{r = \frac{-2}{3}}{r = \frac{-2}{3}}$	

91. Divide both sides of the equation by 0.2. $\frac{0.2e}{0.2} = \frac{5.8}{0.2}$ $c = \frac{5.8}{0.2}$ $c = \frac{5.8}{0.2}$ $c = \frac{5.8}{0.2}$ $c = \frac{5.8}{0.2}$ $c = \frac{5.8}{0.2}$ 92. Multiply both sides of the equation by 7. Multiply. $7(\frac{5}{5}) = 7(16)$ $x = 7(16)$ $x = 112$ 93. Multiply both sides of the equation by $^-4$. positive sign. $7(\frac{5}{2}) = 7(16)$ $x = 112$ 94. Divide both sides of the equation by $\frac{2}{3}$. Divide both sides of the equation by $\frac{2}{3}$. Dividing by a fraction is the same as multiplying by its reciprocal. $y = *48 = 48$ 95. Divide both sides of the equation by $\frac{8}{5}$. Dividing by a fraction is the same as multiplying by its reciprocal. $\frac{8}{5}b + \frac{8}{5} = -56 + \frac{8}{5}$ $b = -56 + \frac{8}{5}$ $b = -56 + \frac{8}{5}$ 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{2}{5}$ of the suggested price $= $21,000$. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. $\frac{7}{8x} + \frac{7}{8} = 21,000 + \frac{7}{8}$ $x = 21,000 + \frac{7}{8}$ $x = 21,000 + \frac{7}{8}$
Divide. Divide. Divide. Divide both sides of the equation by 7. Multiply both sides of the equation by 7. Multiply. 92. Multiply both sides of the equation by 7. Multiply. 93. Multiply both sides of the equation by 74. Signs the same? Multiply and give the result a positive sign. 94. Divide both sides of the equation by $\frac{2}{3}$. Dividing by a fraction is the same as multiplying by its reciprocal. 95. Divide both sides of the equation by $\frac{8}{5}$. Dividing by a fraction is the same as multiplying by its reciprocal. There are several ways to multiply fractions and whole numbers. Here's one. 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price $= \$21,000$. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price $= \$21,000$. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price $= \$21,000$. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. 97. $\frac{7}{8}x = \$21,000 + \frac{7}{8}$ $x = 21,000 + \frac{7}{8}$ $x = 21,000 + \frac{7}{8}$ $x = 21,000 + \frac{7}{8}$
Multiply. $x = 7(16)$ $x = 112$ 93. Multiply both sides of the equation by $^{-4}$. $x = 112$ 93. Multiply both sides of the equation by $^{-4}$. $x = 112$ $y = ^{-4} \cdot ^{-12}$ $y = ^{-4} \cdot ^{-12}$ $y = ^{-4} \cdot ^{-12}$ 94. Divide both sides of the equation by $\frac{2}{3}$. $y = ^{+48} = 48$ 94. Divide both sides of the equation by $\frac{2}{3}$. $y = ^{+48} = 48$ 95. Divide both sides of the equation by $\frac{8}{5}$. $\frac{2}{3}a \div \frac{2}{3} = 54 \div \frac{2}{3}$ $a = 54 \div \frac{2}{3}$ 95. Divide both sides of the equation by $\frac{8}{5}$. $\frac{8}{5}b \div \frac{8}{5} = ^{-56} \div \frac{8}{5}$ $b = ^{-56} \div \frac{8}{5}$ 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price = $\$21,000$. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. $\frac{7}{8x} = \$21,000$ $\frac{7}{8x} = 21,000 \div \frac{7}{8}$ $x = 21,000 \div \frac{7}{8}$
Multiply. $x = 112$ 93. Multiply both sides of the equation by $^-4$. Signs the same? Multiply and give the result a positive sign. $^-4 \cdot \frac{y}{4} = ^-4 \cdot ^{-12} y = ^$
Signs the same? Multiply and give the result a positive sign. 94. Divide both sides of the equation by $\frac{2}{3}$. Dividing by a fraction is the same as multiplying by its reciprocal. 95. Divide both sides of the equation by $\frac{8}{5}$. Dividing by a fraction is the same as multiplying by its reciprocal. There are several ways to multiply fractions and whole numbers. Here's one. 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price = \$21,000. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price = \$21,000. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. 97. 10. 10. 10. 10. 10. 10. 10. 10
Signs the same? Multiply and give the result a positive sign. 94. Divide both sides of the equation by $\frac{2}{3}$. Dividing by a fraction is the same as multiplying by its reciprocal. 95. Divide both sides of the equation by $\frac{8}{5}$. Dividing by a fraction is the same as multiplying by its reciprocal. There are several ways to multiply fractions and whole numbers. Here's one. 96. Let x = the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price = \$21,000. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. 78x = $\frac{7}{8} = 21,000 + \frac{7}{8}$ $x = 21,000 + \frac{8}{7}$
Dividing by a fraction is the same as multiplying by its reciprocal. $a = 54 \cdot \frac{3}{2}$ $a = 81$ 95. Divide both sides of the equation by $\frac{8}{5}$. Dividing by a fraction is the same as multiplying by its reciprocal. There are several ways to multiply fractions and whole numbers. Here's one. $a = 54 \cdot \frac{3}{2}$ $a = 81$ 96. Let x = the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price = \$21,000. So your equation is: Dividing by a fraction is the same as multiplying by its reciprocal. $\frac{7}{8}x = $21,000 \div \frac{7}{8}$ $x = 21,000 \div \frac{7}{8}$ $x = 21,000 \cdot \frac{8}{7}$
Dividing by a fraction is the same as multiplying by its reciprocal. $a = 54 \cdot \frac{3}{2}$ $a = 81$ 95. Divide both sides of the equation by $\frac{8}{5}$. Dividing by a fraction is the same as multiplying by its reciprocal. There are several ways to multiply fractions and whole numbers. Here's one. $a = 54 \cdot \frac{3}{2}$ $a = 81$ 95. Dividing by a fraction is the same as multiplying by its reciprocal. There are several ways to multiply fractions and whole numbers. Here's one. $a = 56 \cdot \frac{8}{5}$ $b = -56 \cdot \frac{5}{8}$ $b = \frac{-56}{1} \cdot \frac{5}{8}$ $b = \frac{-280}{8}$ $b = -35$ 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price = \$21,000. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. $\frac{7}{8}x = $21,000 \div \frac{7}{8}$ $x = 21,000 \div \frac{7}{8}$ $x = 21,000 \cdot \frac{8}{7}$
Dividing by a fraction is the same as multiplying by its reciprocal. There are several ways to multiply fractions and whole numbers. Here's one. 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price = \$21,000. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. Dividing by a fraction is the same as multiplying by its reciprocal. Dividing by a fraction is the same as multiplying by its reciprocal. Dividing by a fraction is the same as multiplying by its reciprocal. Dividing by a fraction is the same as multiplying by its reciprocal. Divide both sides of the same as multiplying
Dividing by a fraction is the same as multiplying by its reciprocal. There are several ways to multiply fractions and whole numbers. Here's one. 96. Let $x =$ the suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price = \$21,000. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. 96. Let $x = the$ suggested selling price of the car. The first and second sentences tell you that $\frac{7}{8}$ of the suggested price = \$21,000. So your equation is: Divide both sides of the equation by $\frac{7}{8}$. Dividing by a fraction is the same as multiplying by its reciprocal. 97. $x = 21,000 \div \frac{7}{8}$ $x = 21,000 \div \frac{7}{8}$
first and second sentences tell you that $\frac{7}{8}$ of the suggested price = \$21,000. So your equation is: $\frac{7}{8}x = $21,000$ Divide both sides of the equation by $\frac{7}{8}$. $\frac{7}{8}x \div \frac{7}{8} = 21,000 \div \frac{7}{8}$ Dividing by a fraction is the same as multiplying by its reciprocal. $x = 21,000 \div \frac{7}{8}$
suggested price = \$21,000. So your equation is: $\frac{7}{8}x = $21,000$ Divide both sides of the equation by $\frac{7}{8}$. $\frac{7}{8}x \div \frac{7}{8} = 21,000 \div \frac{7}{8}$ Dividing by a fraction is the same as multiplying by its reciprocal. $x = 21,000 \div \frac{7}{8}$
Dividing by a fraction is the same as multiplying by its reciprocal. $x = 21,000 \div \frac{7}{8}$ $x = 21,000 \cdot \frac{8}{7}$
x = \$24,000

97.	Let <i>b</i> = the number of bears in each packing cr. The first sentence tells you that the number packing crates times the number of bears in is equal to the total number of bears. Your	of
	equation is: Divide both sides of the equation by 54.	54b = 324 $54b \div 54 = 324 \div 54$ $b = 324 \div 54$
	Divide.	b = 6
98.	Let <i>t</i> = the number of turtle hatchlings born. The first sentence tells you that only 3% survive to adulthood. Three percent of the turtles born is 1,200. Your equation will be: The numerical equivalent of 3% is 0.03, so the equation becomes Divide both sides of the equation by 0.03.	(3%) <i>t</i> = 1,200 0.03 <i>t</i> = 1,200. 0.03 <i>t</i> ÷ 0.03 = 1,200 ÷ 0.03
		$t = 1,200 \div 0.03$ —
	Divide.	t = 40,000
1	 Let <i>c</i> = the number of acres he planted last year 1.5 times <i>c</i> is 300. Divide both sides of the equation by 1.5. Divide. Let <i>d</i> = her annual salary. Five percent of her salary equals her yearly bonus. Your equation will be: The numerical equivalent of 5% is 	r. $ \begin{array}{r} 1.5c = 300 \\ 1.5c \div 1.5 = 300 \div 1.5 \\ c = 300 \div 1.5 \\ \underline{c = 200} \end{array} $ (5%) $d = \$6,000$
	0.05, so the equation becomes Divide both sides of the equation by 0.05.	$\begin{array}{l} 0.05d = 6,000.\\ 0.05d \div 0.05 = 6,000 \div 0.05 \end{array}$
	Divide.	$d = 6,000 \div 0.05$ d = \$120,000

5

Solving Multi-Step Equations

Solving multi-step equations simply combines the work you have done in the previous chapters. The solution techniques for the two types of basic equations you worked on in Chapter 4 are both utilized in the equations in this chapter.

Tips for Solving Multi-Step Equations

- There are at least two ways to show multiplication. You may be used to seeing multiplication shown with an × like this: 5 × 3 = 15. In equations, this becomes confusing. In algebra, the convention is to show multiplication with either a · like this: 5 · 3 = 15, or with parentheses like this: 5(3) = 15. Both conventions will be used in the answers, so you should get used to either one.
- Similarly, division can be shown using the standard division symbol ÷, as in 10 ÷ 2 = 5. Or it can be shown using a fraction bar like this: 10 ÷ 2 = ¹⁰/₂ = 5. Use and get used to both.
- Check your answers before looking at the answer solutions. Just substitute the value you find for the variable and work

each side of the equation as if it were a numerical expression. If the quantities you find are equal, your solution is correct.

- Dividing by a fraction is the same as multiplying by its reciprocal. For example, $9 \div \frac{2}{3} = 9(\frac{3}{2})$.
- To write an equation for a word problem, let the unknown quantity be equal to the variable. Then write the equation based on the information stated in the problem.

Find the solutions to the following equations.

101. 4x + 7 = 10**102.** 13x + 21 = 60**103.** 3x - 8 = 16**104.** 5x - 6 = -26**105.** $\frac{x}{3} + 4 = 10$ **106.** $\frac{x}{7} - 5 = 1$ **107.** 39 = 3a - 9**108.** 4 = 4a + 20**109.** 10a + 5 = 7**110.** 0.3a + 0.25 = 1**111.** $\frac{2}{3}m + 8 = 20$ **112.** $9 = \frac{3}{4}m - 3$ **113.** 41 - 2m = 65**114.** 4m - 14 = 50**115.** $\frac{2m}{5} + 16 = 24$ **116.** 7m - 6 = -2.5**117.** 10s - 6 = 0**118.** $\frac{s}{4} + 2.7 = 3$ **119.** 8s - 7 = 41**120.** -55 = 25 - s

Solve the following word problems by letting a variable equal the unknown quantity, making an equation from the information given, and then solving the equation.

- **121.** A farmer is raising a hog that weighed 20 lbs. when he bought it. He expects it to gain 12 pounds per month. He will sell it when it weighs 200 lbs. How many months will it be before he will sell the animal?
- **122.** Mary earns \$1.50 less than twice Bill's hourly wage. Mary earns \$12.50 per hour. What is Bill's hourly wage?
- **123.** At year's end, a share of stock in Axon Corporation was worth \$37. This was \$8 less than three times its value at the beginning of the year. What was the price of a share of Axon stock at the beginning of the year?
- **124.** Jennifer earned \$4,000 more than 1.5 times her former salary by changing jobs. She earned \$64,000 at her new job. What was her salary at her previous employment?
- **125.** Twenty-five more girls than $\frac{2}{3}$ the number of boys participate in interscholastic sports at a local high school. If the number of girls participating is 105, how many boys participate?

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

Underlined equations show the simplified result.

101. Subtract 7 from both sides of the equation. Associate like terms. Perform numerical operations. Zero is the identity element for addition. Divide both sides of the equation by 4. $4x + 7 - 7 = 11 - 7$ $4x + (7 - 7) = (11 - 7)$ $4x + (0) = (4)$ $4x = 4$ $4x \div 4 = 4 \div 4$ $x = 1$ 102. Subtract 21 from both sides of the equation. Associate like terms. Perform numerical operations. Zero is the identity element for addition. Divide both sides of the equation by 13. $13x + 21 - 21 = 60 - 21$ $13x + (21 - 21) = (60 - 21)$ $13x + (0) = (39)$ $13x = 39$ 103. Add 8 to each side of the equation. Change subtraction to addition and change $3x - 8 + 8 = 16 + 8$
103. Add 8 to each side of the equation. $\frac{x=3}{3x-8+8} = 16+8$
103. Add 8 to each side of the equation. $3x - 8 + 8 = 16 + 8$
the sign of the term that follows. $3x + {}^{-8} + 8 = 16 + 8$ Associate like terms. $3x + ({}^{-8} + 8) = 16 + 8$
Perform numerical operations. $3x + (0) = 24$ Zero is the identity element for addition. $3x = 24$ Divide both sides of the equation by 3. $3x \div 3 = 24 \div 3$ $x = 8$
104. Add 6 to each side of the equation. Change subtraction to addition and change the sign of the term that follows. $5x - 6 + 6 = -26 + 6$ Associate like terms. $5x + -6 + 6 = -26 + 6$ Associate like terms. $5x + (-6 + 6) = -26 + 6$ Perform numerical operations. $5x + (-6 + 6) = -26 + 6$ Zero is the identity element for addition. $5x = -20$ Divide both sides of the equation by 5. $5x \div 5 = -20 \div 5$ $x = -4$

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105.	Subtract 4 from both sides of the equation.	$\frac{x}{3} + 4 - 4 = 10 - 4$
	Associate like terms.	$\frac{x}{3} + (4 - 4) = 10 - 4$
	Perform numerical operations.	$\frac{x}{3} + (0) = 6$
	Zero is the identity element for addition.	$\frac{x}{3} = 6$
	Multiply both sides of the equation by 3.	$3(\frac{x}{3}) = 3(6)$
	r y	$\frac{x=18}{2}$
106.	1	$\frac{x}{7} - 5 + 5 = 1 + 5$
	Change subtraction to addition and change the sign of the term that follows.	$\frac{x}{7}$ + ⁻⁵ + 5 = 1 + 5
	Associate like terms.	$\frac{x}{7} + (-5 + 5) = 1 + 5$
	Perform numerical operations.	$\frac{x}{7} + (0) = 6$
	Zero is the identity element for addition.	$\frac{x}{7} = 6$
	Multiply both sides of the equation by 7.	$7(\frac{x}{7}) = 7(6)$
		$\underline{x = 42}$
107.	Add 9 to each side of the equation.	39 + 9 = 3a - 9 + 9
	Change subtraction to addition and change	
6	the sign of the term that follows.	39 + 9 = 3a + (-9 + 9) 39 + 9 = 3a + (-9 + 9)
	Associate like terms. Perform numerical operations.	39 + 9 = 3a + (-9 + 9) 48 = 3a + (0)
	Zero is the identity element for addition.	48 = 3a
	Divide both sides of the equation by 3.	$48 \div 3 = 3a \div 3$
Δ		$\underline{16} = a$
		1 20 1 20 20
108.	Subtract 20 from both sides of the equation. Associate like terms.	4 - 20 = 4a + 20 - 20 4 - 20 = 4a + (20 - 20)
	Perform numerical operations.	-16 = 4a + (0)
	Zero is the identity element for addition.	$^{-16} = 4a$
	Divide both sides of the equation by 4.	$\frac{-16}{4} = \frac{4a}{4}$
		$^{-4} = a^{+}$
109.	1	10a + 5 - 5 = 7 - 5
	Associate like terms.	10a + (5 - 5) = 7 - 5
	Perform numerical operations.	10a + (0) = 2
	Zero is the identity element for addition.	10a = 2
	Divide both sides of the equation by 10.	$\frac{10a}{10} = \frac{2}{10}$ $a = 0.2 \text{ or } \frac{1}{5}$

	110.	Subtract 0.25 from both sides of the	
		equation.	0.3a + 0.25 - 0.25 = 1 - 0.25
		Associate like terms.	0.3a + (0.25 - 0.25) = 1 - 0.25
		Perform numerical operations. Zero is the identity element for addition.	0.3a + (0) = 0.75 0.3a = 0.75
		•	$\frac{0.3a}{0.3} = \frac{0.75}{0.3}$
		Divide both sides of the equation by 0.3.	
		Simplify the result.	$\underline{a=2.5}$
	111.	Subtract 8 from both sides of the equation.	$\frac{2}{3}m + 8 - 8 = 20 - 8$
		Associate like terms.	$\frac{2}{3}m + (8 - 8) = 20 - 8$
		Perform numerical operations.	$\frac{2}{3}m + (0) = 12$
		Zero is the identity element for addition.	$\frac{2}{3}m = 12$
		Multiply both sides of the equation by	3 7 . 3
		the reciprocal of $\frac{2}{3}$.	$\frac{3}{2}(\frac{2}{3}m) = \frac{3}{2}(12)$
			$\underline{m=18}$
	112.	Add 3 to both sides of the equation.	$9 + 3 = \frac{3}{4}m - 3 + 3$
		Change subtraction to addition and change	
ł		the sign of the term that follows.	$9 + 3 = \frac{3}{4}m + \frac{-3}{3} + 3$
I		Associate like terms.	$9 + 3 = \frac{3}{4}m + (-3 + 3)$
I		Perform numerical operations.	$12 = \frac{3}{4}m + (0)$
I		Zero is the identity element for addition.	$12 = \frac{3}{4}m$
Ţ		Multiply both sides of the equation by	
3		the reciprocal of $\frac{3}{4}$.	$\frac{4}{3}(12) = \frac{4}{3}(\frac{3}{4}m)$
ų	55		16 = m
3	53		
1	113.	Subtract 41 from both sides of the equation.	
		Associate like terms.	(41 - 41) - 2m = 65 - 41
		Perform numerical operations.	(0) - 2m = 24
		Zero is the identity element for addition.	$^{-2}m = 24$
		You can change the subtraction to addition and the sign of the term following to its	
		opposite, which in this case is ^{-2}m .	-2m = 24
		Divide both sides of the equation by -2 .	$\frac{-2m}{-2} = \frac{24}{-2}$
		Use the rules for operating with	-22
		signed numbers.	m = -12
	114.	Add 14 to each side of the equation.	4m - 14 + 14 = 50 + 14
		Change subtraction to addition and change	4m + -14 + 14 = 50 + 14
		the sign of the term that follows. Associate like terms.	4m + -14 + 14 = 50 + 14 4m + (-14 + 14) = 50 + 14
			4m + (-14 + 14) = 50 + 14

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	Perform numerical operations. Zero is the identity element for addition.	4m + (0) = 64 4m = 64
	Divide both sides of the equation by 4.	$\frac{4m}{4} = \frac{64}{4}$ $\underline{m = 16}$
115.	This equation presents a slightly different look The variable in the numerator has a coefficie There are two methods for solving.	
	Subtract 16 from both sides of the equation.	$\frac{2m}{5}$ + 16 - 16 = 24 - 16
	Associate like terms.	$\frac{2m}{5}$ + (16 – 16) = 24 – 16
	Perform numerical operations.	$\frac{2m}{5} + (0) = 8$
	Zero is the identity element for addition.	$\frac{2m}{5} = 8$
	Multiply both sides of the equation by 5. Use rules for multiplying whole numbers	$5(\frac{2m}{5}) = 5(8)$
	and fractions.	$\frac{5}{1}(\frac{2m}{5}) = 40$
		$\frac{5 \cdot 2m}{1 \cdot 5} = 40$
		$\frac{10m}{5} = 40$
		2m = 40
	Divide both sides by 2.	$\frac{2m}{2} = \frac{40}{2}$
	Divide both sides by 2.	m = 20
ШU	Or you can recognize that	$\frac{2m}{5} = \left(\frac{2}{5}\right)m.$
	Then you would multiply by the reciprocal	
	of the coefficient.	$\frac{5}{2}(\frac{2}{5})m = (\frac{5}{2})8$
-33		$\underline{m=20}$
116.	Add 6 to each side of the equation.	7m - 6 + 6 = -2.5 + 6
	Change subtraction to addition and change	7 (2 5 (
	the sign of the term that follows. Associate like terms.	7m + -6 + 6 = -2.5 + 6 7m + (-6 + 6) = -2.5 + 6
	Perform numerical operations.	7m + (0) = 3.5
	Divide both sides of the equation by 7.	$\frac{7m}{7} = \frac{3.5}{7}$
		m = 0.5
117.	Add 6 to each side of the equation. Change subtraction to addition and change	10s - 6 + 6 = 0 + 6
	the sign of the term that follows.	10s + -6 + 6 = 0 + 6
	Associate like terms. Perform numerical operations.	10s + (-6 + 6) = 0 + 6 10s + (0) = 6
	Divide both sides of the equation by 10.	$\frac{10s + (0) = 0}{10} = \frac{6}{10}$
	Express the answer in the simplest form.	10 = 10 $s = \frac{3}{5} = 0.6$

118.	Subtract 2.7 from both sides of the constinu	
	Subtract 2.7 from both sides of the equation.	$\frac{s}{4} + 2.7 - 2.7 = 3 - 2.7$
	Associate like terms.	$\frac{s}{4}$ + (2.7 – 2.7) = 3 – 2.7
	Perform numerical operations.	$\frac{s}{4} + (0) = 0.3$
	Multiply both sides of the equation by 4.	$4(\frac{s}{4}) = 4(0.3)$
		s = 1.2
119.	Add 7 to each side of the equation.	8s - 7 + 7 = 41 + 7
	Change subtraction to addition and change the sign of the term that follows.	$8s + ^{-7} + 7 = 41 + 7$
	Associate like terms.	8s + (-7 + 7) = 41 + 7
	Perform numerical operations.	8s + (0) = 48
	Divide both sides of the equation by 8.	$\frac{8s}{8} = \frac{48}{8}$
	Express the answer in simplest form.	s = 6
120.	Subtract 25 from both sides of the equation.	-55 - 25 = 25 - 25 - s
	Change subtraction to addition and change the sign of the term that follows.	-55 + -25 = 25 + -25 + -s
	Associate like terms.	(-55 + -25) = (25 + -25) + -s
	Perform numerical operations.	-80 = (0) + -s
	Zero is the identity element for addition.	-80 = -s
	You are to solve for <i>s</i> , but the term remaining $\frac{1}{2}$	
	is $\neg s$. If you multiply both sides by $\neg 1$, you will be left with a $\neg s$ or just <i>s</i> .	-1(-80) = -1(-s)
	Use the rules for operating with signed	1(00) = 1(0)
	numbers.	$\underline{80 = s}$
121.	Let $x =$ the number of months. The number	
	of months (<i>x</i>), times 12 (pounds per month) plus the starting weight (20), will be equal t	
	200 pounds. An equation that represents	
	these words would be	12x + 20 = 200.
	Subtract 20 from both sides of the equation.	12x + 20 - 20 = 200 - 20
	Associate like terms. Perform numerical operations.	12x + (20 - 20) = 200 - 20 $12x + (0) = 180$
	*	$\frac{12x}{12} = \frac{180}{12}$
	Divide both sides of the equation by 12.	$\frac{12}{12} = \frac{12}{12}$ x = 15
	The farmer would have to wait 15 months bef	
	Let x = Bill's hourly wage. Then $2x$ less	
122.		
122.	\$1.50 is equal to Mary's hourly wage.	
122.	The equation representing the last	
122.	The equation representing the last statement would be 2:	$\begin{aligned} x - 1.50 &= 12.50. \\ x - 1.50 &= 12.50 \\ + 1.50 &= 12.50 \\ + 1.50 \end{aligned}$

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	Perform numerical operations. Divide both sides of the equation by 2 Bill's hourly wage is \$7.00 per hour.	2x = 14.00 $\frac{2x}{2} = \frac{14.00}{2}$ x = 7.00
123.	Let <i>x</i> = the share price at the beginnin The statements tell us that if we muprice at the beginning of the year by subtract \$8, it will equal \$37. An equipresents this amount is Add 8 to both sides of the equation. Perform numerical operations. Divide both sides of the equation by 3	Iltiply the share y 3 and then uation that $3x - 8 = 37.$ $3x - 8 + 8 = 37 + 8$ $3x = 45$ $\frac{3x}{3} = \frac{45}{3}$ $x = 15$
	One share of Axon costs \$15 at the be	ginning of the year.
124.	Let x = her previous salary. The statements tell us that \$64,000 is equal to 1.5 times x plus \$4,000. An algebraic equation to represent this statement is Subtract 4,000 from both sides	54,000 = 1.5x + 4,000.
	of the equation. 6 Perform numerical operations. 6 Divide both sides of the	54,000 - 4,000 = 1.5x + 4,000 - 4,000 50,000 = 1.5x $\frac{50,000}{1.5} = \frac{1.5x}{1.5}$
R	Jennifer's former salary was \$40,000 p	10,000 = x er year.
125.	Let x = the number of boys who particle interscholastic sports. The question that $\frac{2}{3}$ the number of boys plus 25 is to the number of girls who participate equation that represents this statem	cipate in a tells us s equal ate. An
	Subtract 25 from both sides of the equ	nation. $\frac{2}{3}x + 25 - 25 = 105 - 25$
	Perform numerical operations.	$\frac{2}{3}x = 80$
	Multiply by the reciprocal of $\frac{2}{3}$.	$\frac{\frac{3}{2}(\frac{2}{3}x) = \frac{3}{2}(80)}{x = 120}$
	The number of boys who participate i	

6

Solving Equations with Variables on Both Sides of an Equation

If you have been solving the problems in this book with some success, you will move easily into this chapter. Work through the questions carefully, and refer to the answer explanations as you try and solve the equations by yourself. Then check your answers with the solutions provided. If your sequence of steps is not identical to the solution shown, but you are getting the correct answers, that's all right. There is often more than one way to find a solution. And it demonstrates your mastery of the processes involved in doing algebra.

Tips for Solving Equations with Variables on Both Sides of the Equation

Use the distributive property of multiplication to expand and separate terms. Notice that what follows are variations on the basic distributive property.

a(b - c) = ab - ac-1(b + c) = -b - c -1(b - c) = -b + c -(b - c) = -b + c

The object is to isolate the variable on one side of the equation. When the variable stands alone on one side of the equation, you have found the solution. There are two instances that sometimes occur when solving equations. In the instance where you have eliminated the variable altogether from the equation and end up with two values that do not equal each other—such as 5 = 7, which we know is not true—there is said to be no solution for the equation. Stated another way, the solution is the null set—that is, a set containing no elements. In another instance, you find that the solution seems to be the variable, or some number, is equal to itself. In that instance, any value can make the equation true; therefore, there are an infinite number of solutions.

As you begin to practice solving the following equations, remember that you can add, subtract, multiply, and divide variables on both sides of an equation just as you did with numerical values.

Find the solutions for the following equations.

126. 11x + 7 = 3x - 9**127.** 3x - 23 = 54 - 4x**128.** 5x + 3 + 6x = 10x + 9 - x**129.** 10x + 27 - 5x - 46 = 32 + 3x - 19**130.** 20x - 5 - 5x = 11x + 49**131.** 0.4 + 3x - 0.25 = 1.15 - 2x**132.** 2x + 17 - 1.2x = 10 - 0.2x + 11**133.** 2 + 6x - 0.2 = 5x + 2.1**134.** 1.3 + 5x - 0.1 = -1.2 - 3x**135.** 3x + 12 - 0.8x = 3.4 - 0.8x - 9.4**136.** 7(x+2) + 1 = 3(x+14) - 4x**137.** 4(4x + 3) = 6x - 28**138.** 13 - 8(x - 2) = 7(x + 4) + 46**139.** 13x + 3(3 - x) = -3(4 + 3x) - 2x**140.** 2(2x + 19) - 9x = 9(13 - x) + 21**141.** 12x - 4(x - 1) = 2(x - 2) + 16

142. $2x + 1\frac{4}{5}x = 1 + 3x$ **143.** $\frac{5}{2}(x-2) + 3x = 3(x+2) - 10$ **144.** $6(\frac{1}{2}x + \frac{1}{2}) = 3(x+1)$ **145.** 0.7(0.2x - 1) = 0.3(3 - 0.2x) **146.** 10(x+2) + 7(1-x) = 3(x+9) **147.** 4(9-x) = 2x - 6(x+6) **148.** 5(2x+3) - 9 = 14(x+1) **149.** 7(x-10) + 110 = 4(x-25) + 7x**150.** 0.8(x+20) - 4.5 = 0.7(5+x) - 0.9x

501 Algebra Questions

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Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), {}, or [], perform operations in the innermost parentheses first and work outward.

<u>Underlined</u> equations show the simplified result.

	0 11	equations show the simplified result	
1	126.	Subtract 7 from both sides of the equation.Simplify.Identity property of 0 for addition.Subtract 3<i>x</i> from both sides of the equation.Simplify.	11x + 7 - 7 = 3x - 9 - 7 11x + (0) = 3x - 16 11x = 3x - 16 11x - 3x = 3x - 3x - 16 8x = -16
		 Divide both sides of the equation by 8. Simplify. Solution. Let's check the answer. Substitute ⁻² for x in the original equation. Simplify. 	$\frac{8x}{8} = \frac{-16}{8}$ $1x = -2$ $x = -2$ $11(-2) + 7 = 3(-2) - 9$ $-22 + 7 = -6 - 9$
14		The result is a true statement, so this answer is	-15 = -15
		The result is a true statement, so this answer is	a confect solution.
19	127.	Add 23 to both sides of the equation. Simplify by combining like terms.	3x - 23 + 23 = 54 + 23 - 4x 3x + 0 = 77 - 4x
		Identity property of 0 for addition.	3x = 77 - 4x
		Now add 4x to both sides.	3x + 4x = 77 - 4x + 4x
		Simplify.	7x = 77
		Divide both sides of the equation by 7.	$\frac{7x}{7} = \frac{77}{7}$
		Simplify.	$x_{1}^{7} - x_{2}^{7}$

128.	Use the commutative property	of addition with	5 (2 10 0
	like terms. Combine like terms on each sid	a af tha	5x + 6x + 3 = 10x - x + 9
	equation.	e of the	11x + 3 = 9x + 9
	Subtract 3 from both sides.		11x + 3 - 3 = 9x + 9 - 3
	Simplify.		11x = 9x + 6
	Now subtract $9x$ from both side	es of the	
	equation.		11x - 9x = 9x - 9x + 6
	Simplify.		2x = 6
	Divide both sides by 2.		$\frac{2x}{2} = \frac{6}{2}$
	Simplify.		x=3
129.	Use the commutative property		
	of addition with like terms.	10x - 5x + 27 -	46 = 3x + 32 - 19
	Combine like terms on each		
	side of the equation.	5x - 19 = 3x + 1	3
	Add 19 to both sides of the	5 10 10 3	10 13
	equation.	5x + 19 - 19 = 3	x + 19 + 13
	Combine like terms on each	5x = 3x + 32	
	side of the equation. Subtract 3x from both sides	3x = 3x + 32	
	of the equation to isolate the		
	variable on one side of the		
	equation.	5x - 3x = 3x - 3	x + 32
	Simplify.	2x = 32	
	Divide both sides of the		
\wedge	equation by 2.	$\frac{2x}{2} = \frac{32}{2}$	
	Simplify.	x = 16	
33	Let's check this answer.		
	Substitute 16 for x in the		
	original equation.	10(16) + 27 - 5(16) - 46 = 32 + 3(16) - 19
	Simplify by multiplying		
	factors.	(160) + 27 - (80)) - 46 = 32 + (48) - 19
	Parentheses are not needed.		
	Add and subtract from left		00 10
	to right.	187 - 80 - 46 =	80 - 19
		107 - 46 = 61	
		61 = 61	dian in a mark
	The previous statement is true;	therefore, the sol	ution is correct.

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130.	Use the commutative property to move	
	like terms.	20x - 3x - 11 = 9x + 43
	Combine like terms on each side of	
	the equation.	17x - 11 = 9x + 43
	Add 11 to both sides of the equation.	17x + 11 - 11 = 9x + 43 + 11
	Simplify.	17x = 9x + 54
	Subtract $9x$ from both sides of the	17 0 0 51
	equation.	17x - 9x = 9x - 9x + 54
	Simplify.	8x = 54
	Divide both sides of the equation by 8.	$\frac{8x}{8} = \frac{54}{8}$
	Simplify the expression.	x = 6.75
131.	Use the commutative property to	
	move like terms.	3x + 0.4 - 0.25 = 1.15 - 2x
	Combine like terms on each side of	
	the equation.	3x + 0.15 = 1.15 - 2x
	Subtract 0.15 from both sides of	
	the equation.	3x + 0.15 - 0.15 = 1.15 - 0.15 - 2x
	Combine like terms on each side	2.1.1(0) 1 2.1
	of the equation. Identity property of addition.	3x + (0) = 1 - 2x 3x = 1 - 2x
	Add $2x$ to both sides of the	5x = 1 - 2x
	equation.	3x + 2x = 1 - 2x + 2x
	Simplify.	5x + 2x + 1 = 2x + 2x $5x = 1$
	Divide both sides of the equation	
	by 5.	$\frac{5x}{5} = \frac{1}{5}$
	Simplify the expression.	$x = \frac{1}{5}$
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132.	Use the commutative property with	
	like terms.	2x - 1.2x + 17 = 10 + 11 - 0.2x
	Combine like terms on each side of	
	the equation.	0.8x + 17 = 21 - 0.2x
	Subtract 17 from both sides of	
	the equation.	0.8x + 17 - 17 = 21 - 17 - 0.2x
	Combine like terms on each side of	0.8
	the equation. Add 0.2π to both sides of the equation	0.8x = 4 - 0.2x 0.8x + 0.2x = 4 - 0.2x + 0.2x
	Add $0.2x$ to both sides of the equation. Combine like terms on each side of	0.0x + 0.2x = 7 - 0.2x + 0.2x
	the equation.	1x = 4
	Identity property of multiplication.	x = 4
	recently property of multipleadon.	<u></u>

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133.	Use the commutative property with like terms.	6x + 2 - 0.2 = 5x + 2.1	
	Combine like terms and simplify the expression. Subtract 1.8 from both sides of the	6x + 1.8 = 5x + 2.1	
	equation. Combine like terms and simplify the	6x + 1.8 - 1.8 = 5x + 2.1 - 1.8	
	expression. Subtract $5x$ from both sides of the equat	6x = 5x + 0.3 ion. $6x - 5x = 5x - 5x + 0.3$	
	Combine like terms on each side of the equation.	x = 0.3	
	Let's try this a slightly different way. Instead of adding 1.8, try subtracting 2.		
	from both sides of the equation. Combine like terms on each side of the	6x + 1.8 - 2.1 = 5x + 2.1 - 2.1	
	equation. Now subtract 6x from both sides of the	6x - 0.3 = 5x	
	equation. Combine like terms on each side of the equation.	6x - 6x - 0.3 = 5x - 6x -0.3 = -x	
T	Now divide both sides by the coefficient the variable x , which is -1 .		
- 9	Dividing like signs results in a positive. Simplify.	0.3 = x	
LU	The answer will be the same. As long as manipulate an equation many ways and s		
134.	Use the commutative property with like terms.	3x + 0.4 - 0.25 = 1.15 - 2x	
	Associate like terms on each side of the equation.	3x + (0.4 - 0.25) = 1.15 - 2x	
	Simplify the expression.	3x + (0.15) = 1.15 - 2x	
	Remove the parentheses.	3x + 0.15 = 1.15 - 2x	
	Add $2x$ to both sides of the equation.	3x + 2x + 0.15 = 1.15 + 2x - 2x	
	Associate like terms.	(3x + 2x) + 0.15 = 1.15 + (2x - 2x)	
	Simplify the expression. Subtract 0.15 from both sides of	5x + 0.15 = 1.15	
	the equation. Combine like terms on each side	5x + 0.15 - 0.15 = 1.15 - 0.15	
	of the equation.	5x + 0 = 1	
	Identity property of addition.	5x + 0 = 1 $5x = 1$	
	Divide both sides of the equation by 5.	$\frac{5x}{5} = \frac{1}{5}$	
	Simplify the expression.	5 - 5 x = 0.2	

135.	 Use the commutative property with like terms. Associate like terms on each side of the equation. Simplify the expression. Subtract 12 from both sides of the equation. Associate like terms on each side of the equation. Simplify the expression. Identity property of addition. Add 0.8x to both sides of the equation. Combine like terms on each side of the equation. Divide both sides of the equation by 3. Simplify the expression. 	3x - 0.8x + 12 = 3.4 - 9.4 - 0.8x (3x - 0.8x) + 12 = (3.4 - 9.4) - 0.8x 2.2x + 12 = -6 - 0.8x 2.2x + 12 - 12 = -6 - 12 - 0.8x 2.2x + (12 - 12) = (-6 - 12) - 0.8x 2.2x + (0) = (-18) - 0.8x 2.2x = -18 - 0.8x 2.2x + 0.8x = -18 + 0.8x - 0.8x 3x = -18 $\frac{3x}{3} = \frac{-18}{3}$ x = -6
	 Use the distributive property of multiplication. Simplify the expression. Use the commutative property with like terms. Combine like terms on each side of the equation. Subtract 15 from both sides of the equation. Combine like terms on each side of the equation. Add <i>x</i> to both sides of the equation. Combine like terms on each side of the equation. Divide both sides of the equation by 8. Simplify the expression. 	7(x) + 7(2) + 1 = 3(x) + 3(14) - 4x 7x + 14 + 1 = 3x + 42 - 4x 7x + 14 + 1 = 3x - 4x + 42 7x + 15 = -1x + 42 7x + 15 - 15 = -1x + 42 - 15 7x = -1x + 27 7x + x = x + -1x + 27 8x = 27 $\frac{8x}{8} = \frac{27}{8}$ $x = 3\frac{3}{8}$

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137.	Use the distributive property of	
	multiplication.	4(4x) + 4(3) = 6x - 28
	Simplify the expression.	16x + 12 = 6x - 28
	Subtract 12 from both sides of the	
	equation.	16x + 12 - 12 = 6x - 28 - 12
	Combine like terms on each side of the	
	equation.	16x = 6x - 40
	Subtract 6x from both sides of the	
	equation.	16x - 6x = 6x - 6x - 40
	Simplify the expression.	10x = -40
	Divide both sides of the equation by 10	0. $\frac{10x}{10} = \frac{-40}{10}$
	Simplify the expression.	x = -4
	Simplify the expression.	
138.	Use the distributive property of	
	multiplication.	$13 - 8(x) - 8(^{-}2) = 7(x) + 7(4) + 46$
	Simplify the expression.	13 - 8x + 16 = 7x + 28 + 46
	Use the commutative property with	
	like terms.	13 + 16 - 8x = 7x + 28 + 46
	Combine like terms on each side of	
	the equation.	29 - 8x = 7x + 74
	Add $8x$ to both sides of the equation.	29 + 8x - 8x = 8x + 7x + 74
6	Combine like terms on each side of	
	the equation.	29 = 15x + 74
	Subtract 74 from both sides of the	
	equation.	29 - 74 = 15x + 74 - 74
~	Combine like terms on each side	
1.7	of the equation.	-45 = 15x
	Divide both sides of the equation	-45 15x
	by 15. J	$\frac{-45}{15} = \frac{15x}{15}$
	Simplify the expression.	$\overline{-3} = x$
139.	Use the distributive property of	
	multiplication.	13x + 3(3) - 3(x) = -3(4) - 3(3x) - 2x
	Simplify the expression.	13x + 9 - 3x = -12 - 9x - 2x
	Use the commutative property	
		9 + 13x - 3x = -12 - 9x - 2x
	Combine like terms on each side	/ 100 00 12 /0 20
		9 + 10x = -12 - 11x
	Add $11x$ to both sides of the	
		9 + 10x + 11x = -12 - 11x + 11x
	Combine like terms on each side	
		9 + 21x = -12
	Subtract 9 from both sides of the	
		9 - 9 + 21x = -12 - 9

	_		
	Combine like terms on each side of the equation. Divide both sides of the equation by 21. Simplify the expression.	21x = -21 $\frac{21x}{21} = \frac{-21}{21}$ x = -1	
140.	Use the distributive property of multiplication. Simplify the expression. Use the commutative property with like terms. Combine like terms on each side of the equation. Subtract 38 from both sides	2(2x) + 2(19) - 9x = 9(13) - 9(x) + 21 4x + 38 - 9x = 117 - 9x + 21 38 + 4x - 9x = 117 + 21 - 9x 38 - 5x = 138 - 9x	
	of the equation. Combine like terms on each side of the equation. Add 9x to both sides of the	38 - 38 - 5x = 138 - 38 - 9x -5x = 100 - 9x	
r.	equation. Combine like terms on each side of the equation.	-5x + 9x = 100 - 9x + 9x 4x = 100	
	Divide both sides of the equation by 4. Simplify the expression. Now let's check the answer by substituting the solution into	$\frac{\frac{4x}{4} = \frac{100}{4}}{\frac{x = 25}}$	
羽	the original equation. Simplify the expression. Use order of operations.	2(2(25) + 19) - 9(25) = 9(13 - (25)) + 21 $2(50 + 19) - 225 = 9(^{-1}2) + 21$ $2(69) - 225 = ^{-1}08 + 21$ $138 - 225 = ^{-8}7$	
		-87 = -87	
	The solution is someost		

The solution is correct.

141.	Use the distributive property of multiplication. Simplify the expression.	$12x - 4(x) - 4(^{-}1) = 2(x) + 2(^{-}2) + 16$ 12x - 4x + 4 = 2x - 4 + 16
	Combine like terms on each side of the equation. Subtract 4 from both sides of the	8x + 4 = 2x + 12
	equation. Simplify the expression.	8x + 4 - 4 = 2x + 12 - 4 $8x = 2x + 8$
	Subtract 2<i>x</i> from both sides of the equation.Simplify the expression.Divide both sides of the equation	8x - 2x = 2x - 2x + 8 $6x = 8$
	by 6.	$\frac{6x}{6} = \frac{8}{6}$
	Simplify the expression. Reduce fractions to simplest	$x = \frac{4}{3}$
	terms. Now let's check the answer by	$\underline{x=1\frac{1}{3}}$
	substituting the solution into the original equation. Operate inside the parentheses	$12(\frac{4}{3}) - 4((\frac{4}{3}) - 1) = 2((\frac{4}{3}) - 2) + 16$
	first. Change whole numbers to fractional equivalents.	
		$12(\frac{4}{3}) - 4(\frac{4}{3} - \frac{3}{3}) = 2(\frac{4}{3} - \frac{6}{3}) + 16$ $12(\frac{4}{3}) - 4(\frac{1}{3}) = 2(\frac{-2}{3}) + 16$
	Multiply.	$\frac{48}{3} - \frac{4}{3} = -\frac{4}{3} + 16$
E	Add $\frac{4}{3}$ to both sides of the equation. Simplify the expression. A true statement, so this solution is co	$\frac{48}{3} + \frac{4}{3} - \frac{4}{3} = \frac{4}{3} - \frac{4}{3} + 16$ 16 = 16 percet.
142.	Simplify the equation by adding like t	terms. $3\frac{4}{5}x = 1 + 3x$
	Subtract $3x$ from both sides of the eq Combine like terms on each side of the	5
	equation. Divide both sides of the equation by -	$\frac{4}{5}x = 1$
	Remember that division by a fracti same as multiplication by the recip of the fraction. You can multiply by	rocal
	Simplify the expression.	$\frac{x = \frac{5}{4}}{}$
143.		$(1) - \frac{5}{2}(2) + 3x = 3(x) + 3(2) - 10$
	Simplify the expression. $\frac{5}{2}x$	-5 + 3x = 3x + 6 - 10

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	Use the commutative property with like terms. A simple way to avoid having to operate with fractions is to multiply the equation by a factor that will eliminate the denominator. In this case, that would be a 2.	$\frac{5}{2}x + 3x - 5 = 3x + 6 - 10$ $2(\frac{5}{2}x + 3x - 5) = 2(3x + 6 - 10)$
	Use the distributive property. Simplify the expressions. Combine like terms on each	$2(\frac{5}{2}x) + 2(3x) - 2(5) = 2(3x) + 2(6) - 2(10)$ 5x + 6x - 10 = 6x + 12 - 20
	side of the equation. Add 10 to both sides of the equation.	11x - 10 = 6x - 8 $11x - 10 + 10 = 6x - 8 + 10$
	Simplify the expression. Subtract 6x from both sides of the equation.	11x = 6x + 2 11x - 6x = 6x - 6x + 2
	Combine like terms on each side of the equation. Divide both sides of the equation by 5.	$5x = 2$ $\frac{5x}{5} = \frac{2}{5}$
	Simplify the expression.	$\frac{x=\frac{2}{5}}{5}$
144. 分	Use the distributive property on Simplify the expression. Subtract 3 from both sides of the Simplify the expression. Divide both sides of the equation Simplify the expression. There are an infinite number of a	equation. a by 3. $3x + 3 = 3x + 3$ $3x + 3 - 3 = 3x + 3 - 3$ $3x = 3x$ $\frac{3x}{3} = \frac{3x}{3}$ $x = x$
145.	both sides. Simplify the expressions.	0.7(0.2x) - 0.7(1) = 0.3(3) - 0.3(0.2x) 0.14x - 0.7 = 0.9 - 0.06x
	Add 0.06 <i>x</i> to both sides of the equation. Combine like terms on each	0.14x + 0.06x - 0.7 = 0.9 - 0.6x + 0.06x
	side of the equation. Add 0.7 to both sides of the	0.2x - 0.7 = 0.9
	equation. Combine like terms on each side of the equation.	0.2x - 0.7 + 0.7 = 0.9 + 0.7 0.2x = 1.6
	Divide both sides of the equation by 0.2.	$\frac{0.2x}{0.2} = \frac{1.6}{0.2}$
	Simplify the expression.	x = 8

	146.	Use the distributive property of		
		multiplication.	10(x) + 10(2) + 7(1) - 7(x) = 3(x) + 3(9)	
		Simplify the expression.	10x + 20 + 7 - 7x = 3x + 27	
		Use the commutative property		
		with like terms.	10x - 7x + 20 + 7 = 3x + 27	
		Combine like terms on each		
		side of the equation.	3x + 27 = 3x + 27	
		Look familiar? Subtract 27		
		from both sides.	3x + 27 - 27 = 3x + 27 - 27	
		Simplify the expression.	3x = 3x	
		Divide both sides of the		
		equation by 3.	x = x	
		The solutions for this equation are i	nfinite.	
	147.	Use the distributive property of		
		multiplication.	4(9) - 4(x) = 2x - 6(x) - 6(6)	
		Simplify the expressions.	36 - 4x = 2x - 6x - 36	
		Combine like terms.	36 - 4x = -4x - 36),
		Add $4x$ to both sides of the equation	36 + 4x - 4x = 4x - 4x - 36	
	_	Combine like terms on each side of		
		the equation.	36 = -36	
		This is not true. There is no solutio	· ·	
		saying this is to say that the solution	for this equation is the null set.	
	140	Use the distributive property of		
-	140.	Use the distributive property of multiplication.	5(2x) + 5(3) - 9 = 14(x) + 14	
		Simplify the expressions.	$\frac{3(2x) + 3(3) - 7 - 11(x) + 11}{10x + 15 - 9 = 14x + 14}$	
E	i an	Combine like terms.	10x + 15 = 7 = 11x + 11 10x + 6 = 14x + 14	
ㅋ		Subtract $9x$ from both sides of the	104 10 - 114 11	
	33	equation.	10x - 10x + 6 = 14x - 10x + 14	
		Combine like terms on each side of		
		the equation.	6 = 4x + 14	
		Subtract 14 from both sides of the		
		equation.	6 - 14 = 4x + 14 - 14	
		Combine like terms on each side of		
		the equation.	$^{-8} = 4x$	
		Divide both sides of the equation by	$74. \qquad \frac{-8}{4} = \frac{4x}{4}$	
		Simplify the expression.	-2 = x	

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	149.	Use the distributive property of	of	7() $7(10)$, 110 $4()$	1(25) . 7.	
		multiplication.		7(x) - 7(10) + 110 = 4(x) - 4x	• •	
		Simplify the expressions. Combine like terms on each si	de	7x - 70 + 110 = 4x - 100 +	<i>1 x</i>	
		of the equation.	ue	7x + 40 = 11x - 100		
		Subtract 40 from both sides of	:	74 + 10 - 114 100		
		the equation.		7x + 40 - 40 = 11x - 100 - 40	40	
		Combine like terms on each si	de			
		of the equation.		7x = 11x - 140		
		Subtract $11x$ from both sides of	of			
		the equation.		7x - 11x = 11x - 11x - 140		
		Combine like terms on each si	de			
		of the equation.		-4x = -140		
		Divide both sides of the equation	ion	-4x -140		
		by -4.		$\frac{-4x}{-4} = \frac{-140}{-4}$		
		Simplify the expressions.		$\underline{x=35}$		
	150	You should look for opportuni	ties to s	implify		
	1001	your work. In this equation,				
		terms are in decimal form. I				
		the equation by 10, it might		1.7		
		make it easier for you.	10[0.8	(x+20)-4.5] = 10[0.7(5+x)]	(x) - 0.9x]	
		Use the distributive property				
		of multiplication.	10[0.8	(x + 20)] - 10[4.5]		
				= 10[0.7(5+x)]	-10[0.9x]	
Л		Simplify the expressions.	8(x + 2)	10) - 45 = 7(5 + x) - 9x		
귀		Use the distributive	9()	8(20) - 45 = 7(5) + 7(x) - 9x		
5		property again. Simplify the expressions.		6(20) - 43 = 7(3) + 7(x) - 9x 60 - 45 = 35 + 7x - 9x		
З	133	Combine like terms on	0x + 10	50 - 75 = 55 + 7x - 9x		
-		each side of the equation.	8x + 1	15 = 35 - 2x		
		Subtract 115 from both				
		sides of the equation.	8x + 1	15 - 115 = 35 - 115 - 2x		
		Combine like terms on each				
		side of the equation.	8x = -8	30 - 2x		
		Add $2x$ to both sides of				
		the equation.	8x + 2x	x = -80 - 2x + 2x		
		Combine like terms on each	10	-00		
		side of the equation. Divide both sides of the	10x = -	00		
		equation by 10.	$\frac{10x}{10} = -$	80		
		Simplify the expression.	x = -8	10		
		r ,				

Using Formulas to Solve Equations

Chances are you have been asked to use formulas to solve problems in math, science, social studies, or technology. Algebra is a useful skill to know when faced with problems in these areas. In this chapter, you will have the chance to solve word problems that could pop up in any one of these subject areas. These word problems require you to find an unknown value in a formula. You will be using your algebra problem-solving skills in every problem.

Tips for Using Formulas to Solve Equations

Given a formula with several variables, you will generally be given values for all but one. Then you will be asked to solve the equation for the missing variable. It can be helpful to list each variable with its given value. Put a question mark next to the equal sign in place of the value for the unknown variable.

Keep in mind the rules for order of operations.

Select from these formulas the appropriate one to solve the following word problems:

<u>Volume of a rectangular solid</u>: V = lwh where l =length, w =width, h =height

<u>Distance formula:</u> D = rt where r = rate, t = time

<u>Simple interest</u>: I = prt where p = principal, r = interest rate, t = time in years<u>Area of a trapezoid</u>: $A = \frac{1}{2}b(b_1 + b_2)$ where $b = height and b_1$ and b_2 are the bases

<u>Fahrenheit/Celsius equivalence:</u> $C = \frac{5}{9}(F - 32)$

<u>Volume of a cylinder</u>: $V = \pi r^2 h$ (let $\pi = 3.14$) where r = radius and h = height <u>Surface area of a cylinder</u>: $S = 2\pi r(r + h)$ where r = radius of the base, h = height of cylinder (let $\pi = 3.14$)

- **151.** Find the volume of a rectangular solid whose length is 12 cm, width is 8 cm, and height is 3 cm.
- **152.** A rectangular container has a volume of 98 ft³. If the length of the box is 7 ft, and its width is 3.5 ft, what is its height?
- **153.** An airplane flies at an average velocity of 350 miles per hour. A flight from Miami to Aruba takes 3.5 hours. How far is it from Miami to Aruba?
- **154.** A bicycle tour group planned to travel 68 miles between two New England towns. How long would the trip take if they averaged 17 miles per hour for the trip?
- **155.** A hiking group wanted to travel along a chapter of the Appalachian Trail for 4 days. They planned to hike 6 hours per day and wanted to complete a trail chapter that was 60 miles long. What rate of speed would they have to average to complete the trail chapter as planned?
- **156.** At an interest rate of 6%, how much interest would \$12,000 earn over 2 years?
- **157.** Over a three-year period, the total interest paid on a \$4,500 loan was \$1,620. What was the interest rate?
- **158.** In order to earn \$1,000 in interest over 2 years at an annual rate of 4%, how much principal must be put into a savings account?
- **159.** How long will it take for a \$3,000 savings account to double its value at a simple interest rate of 10%?
- **160.** What is the area of a trapezoid whose height is 8 cm and whose bases are 14 cm and 18 cm?
- 161. What would be the height of a trapezoidal building if, at its base, it measured 80 feet, its roofline measured 40 feet, and the surface area of one side was 7,200 ft²?
- **162.** A trapezoid with an area of 240 square inches has a height of 12 inches. What are the lengths of the bases, if the lower base is three times the length of the upper?

- **163.** You plan to visit a tropical island where the average daytime temperature is 40° Celsius. What would that temperature be on the Fahrenheit scale?
- **164.** Jeff won't play golf if the temperature falls below 50° Fahrenheit. He is going to a country where the temperature is reported in Celsius. What would Jeff's low temperature limit be in that country? (Round your answer to the nearest degree.)
- **165.** A steel drum has a base with a radius of 2 feet and a height of 4 feet. What is its volume in cubic feet?
- **166.** Find the radius of a cylinder whose volume is 339.12 cubic centimeters and whose height is 12 centimeters.
- **167.** The volume of a cylindrical aquarium tank is 13,565 cubic feet. If its radius is 12 feet, what is its height to the nearest foot?
- **168.** The radius of the base of a cylinder is 20 cm. The height of the cylinder is 40 cm. What is its surface area?
- **169.** What is the height of a cylinder whose surface area is 282.6 square inches and whose radius is 3 inches?

170. A cylinder has a surface area of 2,512 square feet. The height of the cylinder is three times the radius of the base of the cylinder. Find the radius and the height of the cylinder.

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Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

V = lwbV = ?

l = 12 cmw = 8 cm

The simplified result is <u>underlined</u>.

151. Write the applicable formula. List the values for the variables.

		b = 3 cm
	Substitute the values into the formula.	V = (12)(8)(3)
	Simplify the expression.	V = 288
	Include the units.	$V = 288 \text{ cm}^3$
	include the units.	<u>v = 200 cm</u>
450	White the community frame.	V = lwh
152.	Write the appropriate formula.	
	List the values for the variables.	<i>V</i> = 98
\frown		l = 7
		w = 3.5
JJ	יויוי דד יויוי	b = ?
	Substitute the values into the formula.	98 = (7)(3.5)b
	Simplify the expression.	98 = 24.5 <i>b</i>
	Divide both sides of the equation by 24.5.	$\frac{98}{24.5} = \frac{24.5h}{24.5}$
		24.5 - 24.5 4 = b
	Simplify the expression.	
	Include the units.	b = 4 feet
450		Dt
153.	Write the applicable formula.	D = rt
	List the values for the variables.	D = ?
		r = 350
		<i>t</i> = 3.5
	Substitute the values for the variables.	D = (350)(3.5)
	Simplify the expression.	D = 1,225
	Include the units.	D = 1,225 miles

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154.	Write the applicable formula. List the values for the variables.	D = rt $D = 68$ $r = 17$
	Substitute the values for the variables. Simplify the expression.	t = ? 68 = (17)t 68 = 17t
	Divide both sides of the equation by 17. Simplify the expression. Include the units.	$\frac{68}{17} = \frac{17t}{17}$ 4 = t 4 hours = t
155.	Write the applicable formula. List the values for the variables.	D = rt $D = 60$ $r = ?$
	Calculate the total number of hours.	$4 \text{ days} \cdot \frac{6 \text{ hrs}}{\text{day}} = 24 \text{ hrs}$ $t = 24$
	Substitute the given values into the formula. Simplify the expression.	60 = r(24) 60 = 24r
	Divide both sides of the equation by 18. Simplify the expression.	$\frac{60}{24} = \frac{24r}{24} \\ 2.5 = r$
_	Include the units.	2.5 miles per hour = r
156.	Write the applicable formula. List the values for the variables.	I = prt I = ? p = 12,000 r = 6% t = 2
家	Substitute the given values into the formula. Simplify the expression. Include the units.	I = (12,000)(0.06)(2) I = 1,440 I = \$1,440
157.		I = prt
	List the values for the variables. Substitute the given values into the formula. Simplify the expression.	I = 1,620 p = 4,500 r = ? t = 3 1,620 = (4,500)r(3) 1,620 = 13,500r $\frac{1620}{13500} = \frac{13,500r}{13,500}$
	Divide both sides of the equation by 13,500. Simplify the expression. Express as a percent.	13500 = 13,500 0.12 = r 12% = r
158.	Write the applicable formula. List the values for the variables.	I = prt I = 1,000 p = ? r = 4% t = 2

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	Substitute the given values into the formula. Simplify the expression. Divide both sides of the equation by 0.08. Simplify the expression. Include the units.	1,000 = p(0.04)(2) 1,000 = 0.08p $\frac{1,000}{0.08} = \frac{0.08p}{0.08}$ 12,500 = p $\frac{\$12,500 = p}{\$12,500 = p}$
159.	Write the applicable formula. To double its value, the account would have to earn \$3,000 in interest. List the values for the variables.	I = prt I = 3,000 p = 3,000 r = 10% t = ?
	Substitute the given values into the formula. Simplify the expression. Divide both sides of the equation by 300. Simplify the expression. Include the units.	3,000 = (3,000)(0.10)t 3,000 = 300t $\frac{3,000}{300} = \frac{300t}{300}$ 10 = t 10 years = t
160.	Write the applicable formula. List the values for the variables.	$A = \frac{1}{2}b(b_1 + b_2) A = ? b_1 = 14 b_2 = 18 b = 8$
刻	Substitute the given values into the formula. Simplify the expression. Include the units.	$A = \frac{1}{2} \cdot 8 \cdot (14 + 18)$ $A = \frac{1}{2} \cdot 8 \cdot 32$ $A = \frac{1}{2} \cdot 256$ $A = 128$ $\underline{A} = 128 \text{ cm}^2$
161.	Write the applicable formula. List the values for the variables.	$A = \frac{1}{2}b(b_1 + b_2) A = 7,200 b_1 = 40 b_2 = 80 b = ?$
	Substitute the given values into the formula. Simplify the expression.	$7,200 = \frac{1}{2} \cdot h \cdot (40 + 80)$ $7,200 = \frac{1}{2} \cdot h \cdot 120$ 7,200 = 60 h
	Divide both sides of the equation by 60. Simplify the expression. Include the units.	$\frac{7,200}{60} = \frac{60h}{60}$ 120 = h 120 ft = h

	501 Algebra Questio	ons
162.	Write the applicable formula. List the values for the variables.	$A = \frac{1}{2}b(b_1 + b_2)$ A = 240 $b_1 = x$ $b_2 = 3x$
	Substitute the given values into the formula.	b = 12 240 = $\frac{1}{2} \cdot 12 \cdot (x + 3x)$
	Simplify the expression.	$240 = \frac{1}{2} \cdot 12 \cdot 4x$ $240 = 6 \cdot 4x$ 240 = 24x
	Divide both sides of the equation by 24. Simplify the expression.	$\frac{\frac{240}{24}}{10} = \frac{\frac{24x}{24}}{10} = x$
	Substitute 10 for x in the list of variables.	$\frac{b_1 = 10}{b_2 = 3(10)}$ $\frac{b_2 = 30}{b_2 = 30}$
163.	Write the applicable formula. List the values for the variables.	$C = \frac{5}{9}(F - 32)$ C = 40
	Substitute the given values into the formula. Multiply both sides of the equation by 9. Simplify the expression.	$F = ?$ $40 = \frac{5}{9}(F - 32)$ $9(40) = 9[\frac{5}{9}(F - 32)]$ $360 = 5(F - 32)$ $360 = 5F - 5(32)$ $360 = 5F - 160$
家	Add 160 to both sides of the equation. Combine like terms on each side of the equation.	360 + 160 = 5F + 160 - 160 520 = 5F
	Divide both sides of the equation by 5. Simplify the expression.	$\frac{520}{5} = \frac{5F}{5}$ 104 = F
164.	Write the applicable formula. List the values for the variables.	$ \frac{C}{C} = \frac{5}{9}(F - 32) \\ C = ? \\ F = 50 $
	Substitute the given values into the formula.	$C = \frac{5}{9}(50 - 32)$
	Simplify the expression.	$C = \frac{5}{9}(18)$ $C = \frac{5}{9}(\frac{18}{1})$

165.	Write the applicable formula. List the values for the variables.	$V = \pi r^{2} h$ $V = ?$ $r = 2$ $h = 4$
	Substitute the given values into the formula. Simplify the expression. Include the units.	b = 4 $\pi = 3.14$ $V = (3.14)(2)^2(4)$ V = 50.24 V = 50.24 ft ³
166.	Write the applicable formula. List the values for the variables.	$V = \pi r^2 h$ V = 339.12 r = ? h = 12
	Substitute the given values into the formula. Simplify the expression. Divide both sides of the equation by 37.68. Simplify the expression. Include the units.	$\pi = 3.14$ $339.12 = (3.14)r^{2}(12)$ $339.12 = 37.68 r^{2}$ $\frac{339.12}{37.68} = \frac{37.68r^{2}}{37.68}$ $9 = r^{2}$ $3 = r$ $3 \text{ cm} = r$
167.	Write the applicable formula. List the values for the variables.	$V = \pi r^2 h$ V = 13,565 r = 12 h = ?
E	Substitute the given values into the formula. Simplify the expression. Divide both sides of the equation by 452.16. Simplify the expression. Include the units.	h = f $\pi = 3.14$ $13,565 = (3.14)(12^2)h$ 13,565 = 452.16h $\frac{13,565}{452.16} = \frac{452.16h}{452.16}$ 30 = h 30 feet = h
168.	Write the applicable formula. List the values for the variables.	$S = 2\pi r(r + b)$ S = ? r = 20 b = 40
	Substitute the given values into the formula. Simplify the expression. Include the units.	$\pi = 3.14$ S = 2(3.14)(20)(20 + 40) S = 7,536 $S = 7,536 \text{ cm}^2$

	169	Write the applicable formula.	$S = 2\pi r(r+b)$	
	103.	List the values for the variables.	S = 282.6	
			r = 3	
			b = ?	
			$\pi = 3.14$	
		Substitute the given values into		
		the formula.	282.6 = 2(3.14)(3)(3+b)	
		Simplify the expression.	282.6 = 18.84(3 + h)	
		Use the distributive property		
		of multiplication.	282.6 = 18.84(3) + 18.84(b)	
		Simplify the expression.	282.6 = 56.52 + 18.84 <i>b</i>	
		Subtract 56.52 from both sides		
		of the equation.	282.6 - 56.52 = 56.52 - 56.52 + 18.84	
		Simplify the expression.	226.08 = 18.84h	
		Divide both sides of the	226.08 8.84 <i>b</i>	
		equation by 18.84.	$\frac{226.08}{18.84} = \frac{8.84b}{18.84}$ 12 = b	
		Simplify the expression. Include the units.	12 = b 12 in = b	
		include the units.	$\frac{12 \text{ III} - h}{2}$	1
	170.	Write the applicable formula.	$S = 2\pi r(r+b)$	
		List the values for the variables.	S = 2,512	
			r = x	
			b = 3x	
			$\pi = 3.14$	
		Substitute the given values into		
		the formula.	2,512 = 2(3.14)(x)(x + 3x)	
		Simplify the expression.	2,512 = 6.28x(4x)	
Ę		Divide both sides of the	$\frac{2,512}{25.12} = \frac{25.12x^2}{25.12}$	
Ę	133	equation by 25.12.	$\frac{25.12}{100} = \frac{25.12}{25.12}$	
-		Simplify the expression. Solve for <i>x</i> .	$100 = x^{-1}$ 10 = x	
		Substitute the value for x into	$10 - \lambda$	
		the values list.	r = x = 10 feet	
			$\frac{1}{b} = 3x = 3(10) = 30$ feet	



Graphing Linear Equations

This chapter asks you to find solutions to linear equations by graphing. The solution of a linear equation is the set of ordered pairs that form a line on a coordinate graph. Every point on the line is a solution for the equation. One method for graphing the solution is to use a table with x and y values that are solutions for the particular equation. You select a value for x and solve for the y value. But in this chapter, we will focus on the slope and y-intercept method.

The slope and y-intercept method may require you to change an equation into the slope-intercept form. That is, the equation with two variables must be written in the form y = mx + b. Written in this form, the *m* value is a number that represents the slope of the solution graph and the *b* is a number that represents the y-intercept. The slope of a line is the ratio of the change in the y value over the change in the x value from one point on the solution graph to another. From one point to another, the slope is the rise over the run. The y-intercept is the point where the solution graph (line) crosses the y-axis. Another way of saying that is: The y-intercept is the place where the value of x is 0.

Tips for Graphing Linear Equations

- Rewrite the given equation in the form y = mx + b.
- Use the *b* value to determine where the line crosses the *y*-axis. That is the point (0,*b*).

- If the value of *m* is negative, use a negative sign in only the numerator or the denominator, not both. For example, ⁻³/₄ = ⁻³/₄ = ³/₋₄.

Graph the following equations using the slope and *y*-intercept method.

171. y = 2x + 3**172.** y = 5x - 2**173.** y = -2x + 9**174.** $y = \frac{3}{4}x - 1$ **175.** $y = \frac{5}{2}x - 3$ **176.** y - 2x = 4**177.** y + 3x = -2**178.** $y - \frac{1}{2}x = 3\frac{1}{2}$ **179.** 2x + 5y = 30**180.** 2y + 4x = 10**181.** x - 3y = 12**182.** 3x + 9y = -27**183.** $^{-5}x - y = -\frac{7}{2}$ **184.** x = 7y - 14**185.** 0 = 3x + 2y**186.** 3x + 12y = -18**187.** y - 0.6x = -2**188.** $\frac{2}{3}y - \frac{1}{2}x = 0$ **189.** $\frac{5}{6}x - \frac{1}{3}y = 2$ **190.** 7x = 4y + 8**191.** 20x - 15 = 5y**192.** 6y + 13x = 12**193.** 0.1x = 0.7y + 1.4

194. -34x + 85 = 17y

195. 6y + 27x = -42

For the following problems, use the slope/*y*-intercept method to write an equation that would enable you to draw a graphic solution for each problem.

- **196.** A glider has a 25:1 descent ratio when there are no updrafts to raise its altitude. That is, for every 25 feet it moves parallel to the ground, it will lose 1 foot of altitude. Write an equation to represent the glider's descent from an altitude of 250 feet.
- **197.** An Internet service provider charges \$15 plus \$0.25 per hour of usage per month. Write an equation that would represent the monthly bill of a user.
- **198.** A scooter rental agency charges \$20 per day plus \$0.05 per mile for the rental of a motor scooter. Write an equation to represent the cost of one day's rental.
- 199. A dive resort rents scuba equipment at a weekly rate of \$150 per week and charges \$8 per tank of compressed air used during the week of diving. Write an equation to represent a diver's cost for one week of diving at the resort.

200. A recent backyard bird count showed that one out of every seven birds that visited backyard feeders was a chickadee. Write an equation to represent this ratio.

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Answers

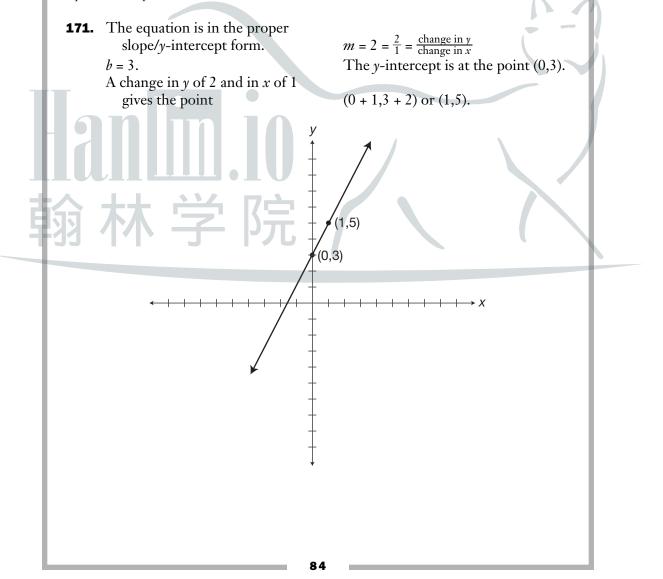
Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

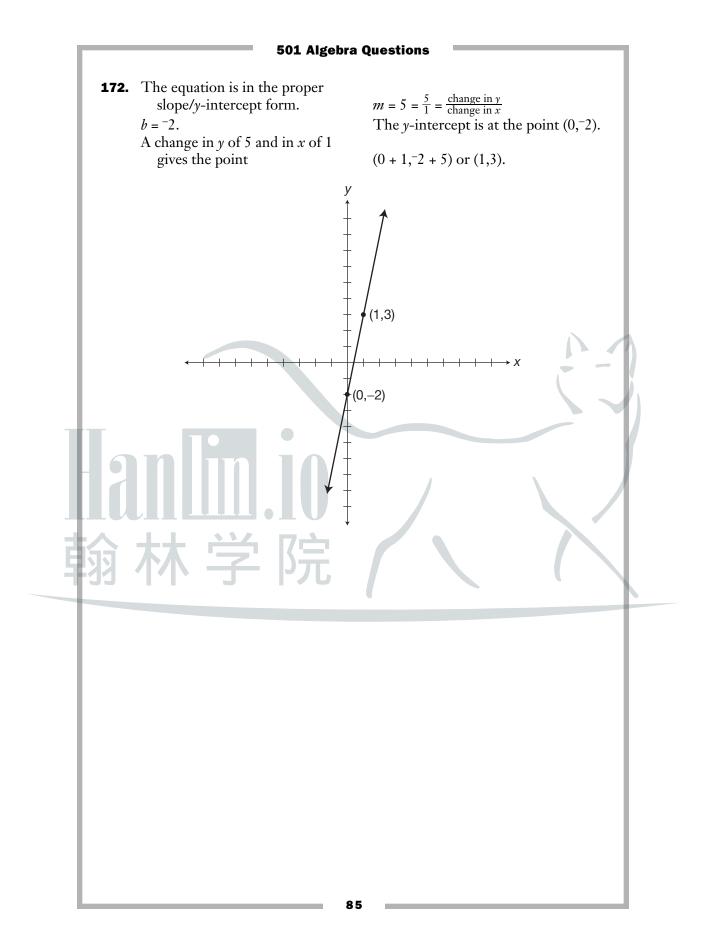
Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

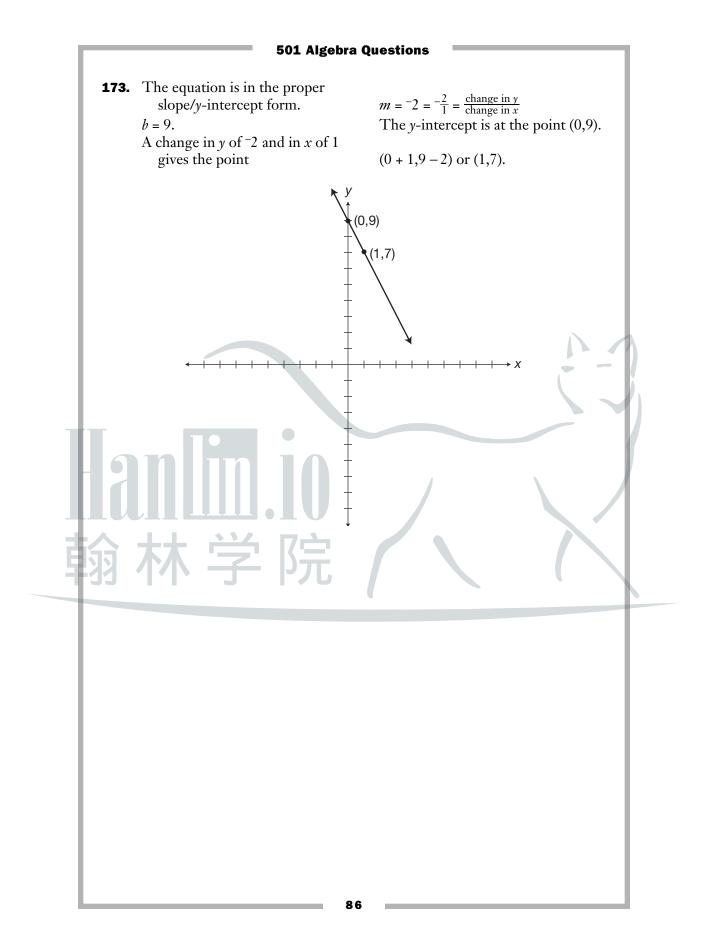
When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

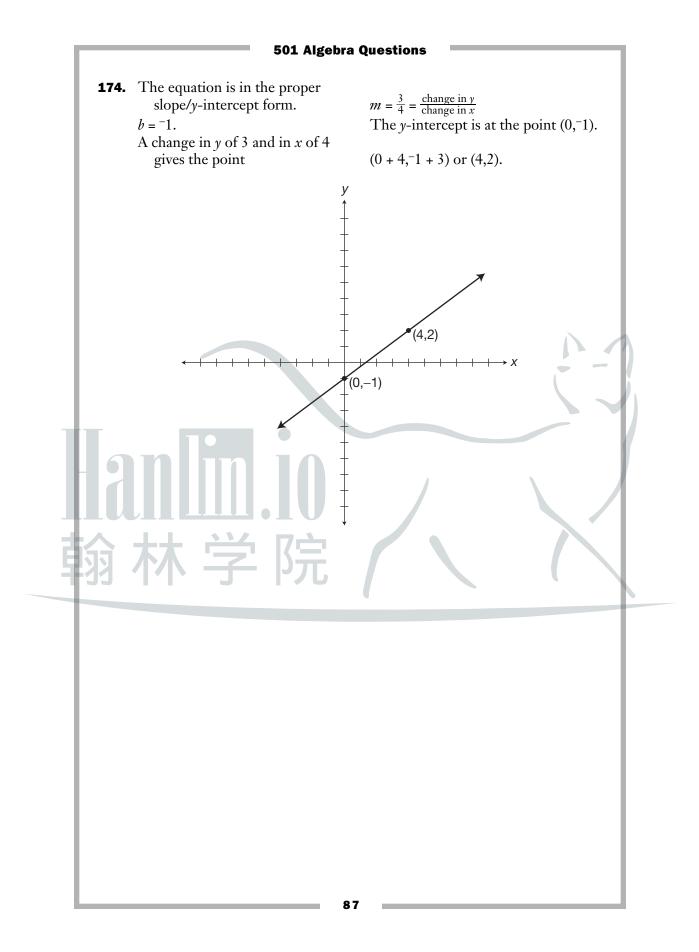
Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

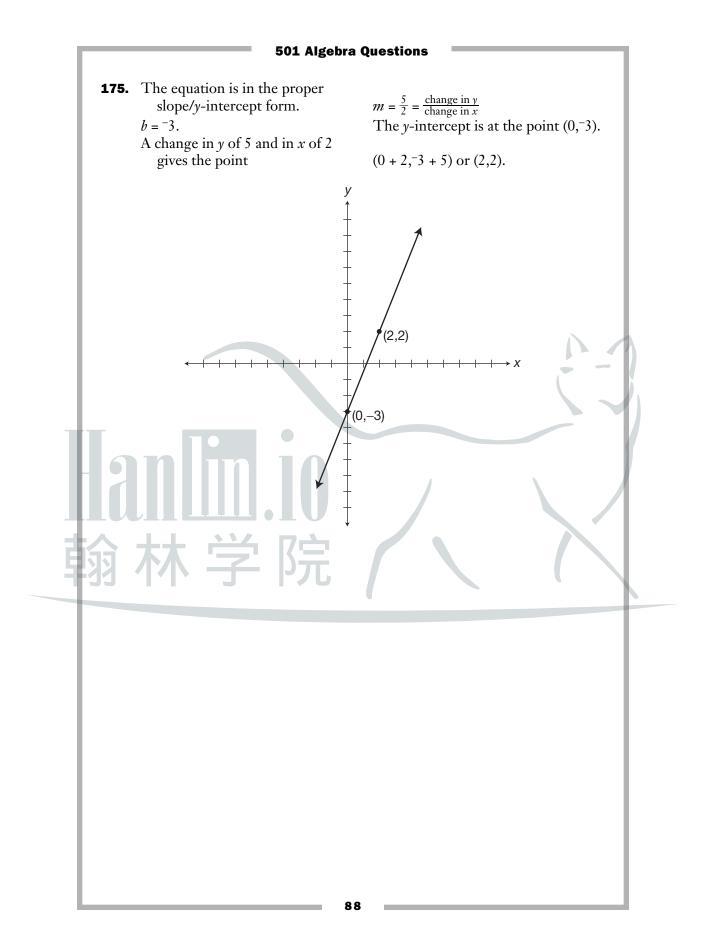
<u>Underlined</u> expressions show the original algebraic expression as an equation with the expression equal to its simplified result.



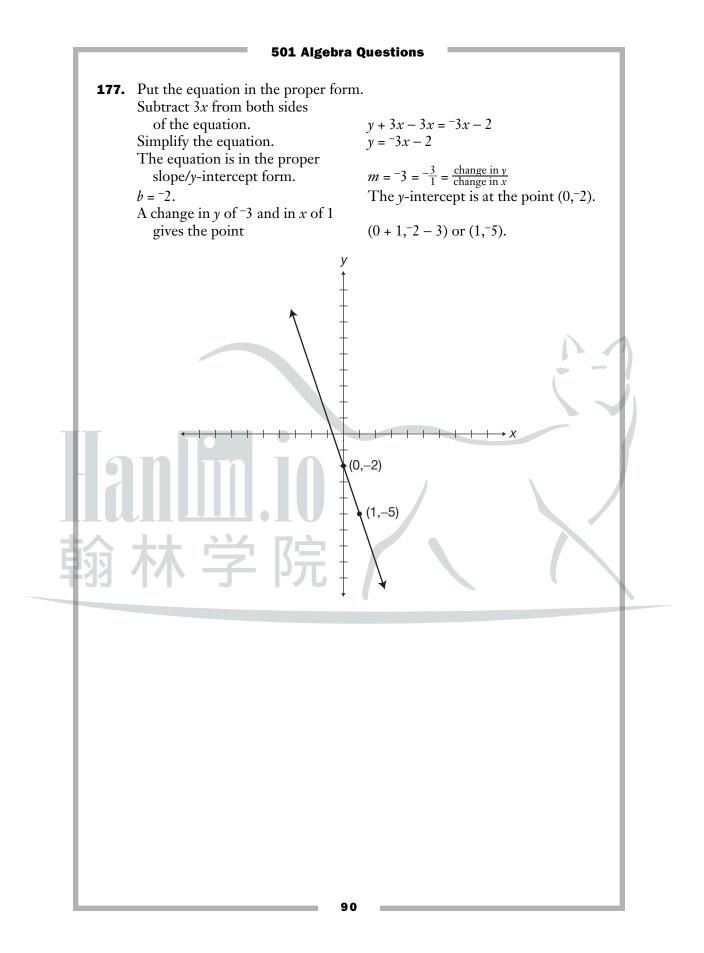


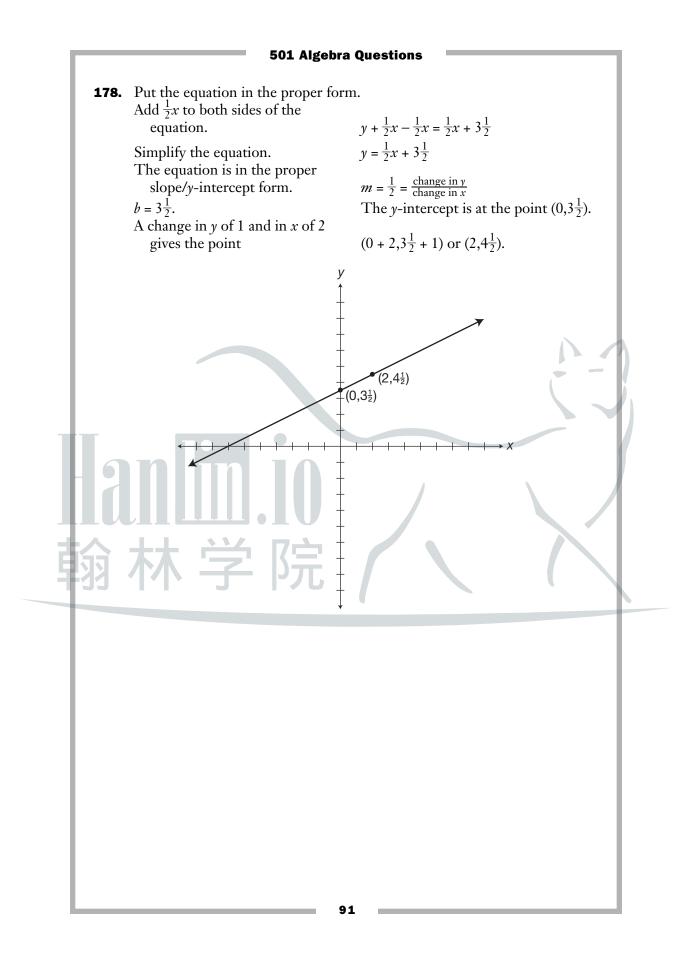


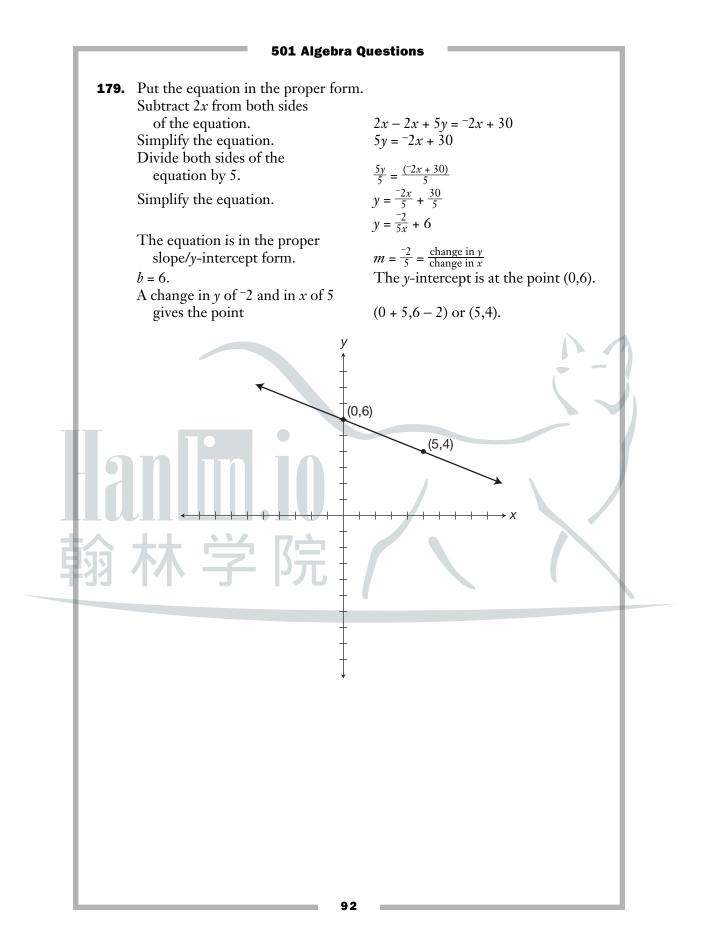


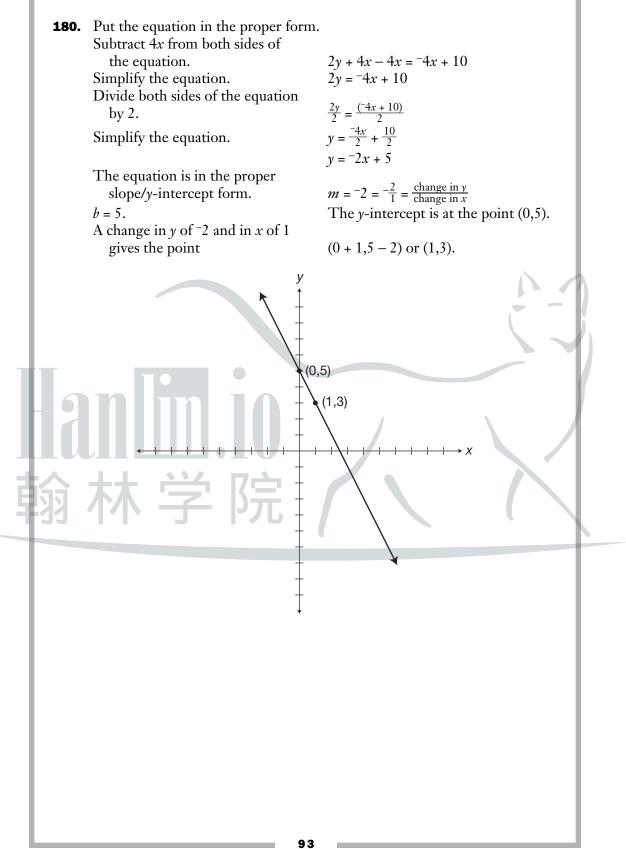


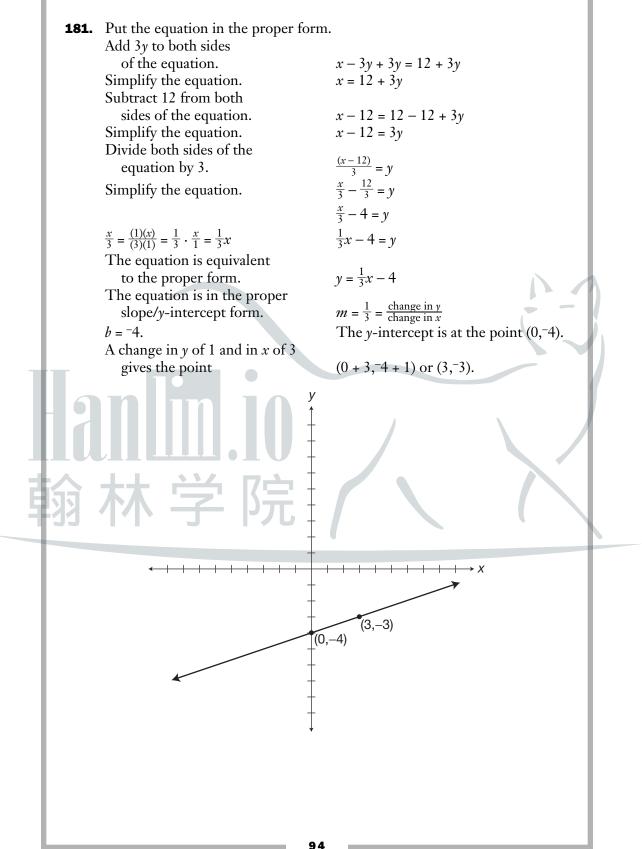
176. Put the equation in the proper form. Add 2x to both sides of the equation. Simplify the equation. The equation is in the proper slope/y-intercept form. b = 4. A change in y of 2 and in x of 1 gives the point y + 2x - 2x = 2x + 4 y = 2x + 4 The y-intercept is x (0 + 1,4 + 2) or $(1,6)$. y (0,4)
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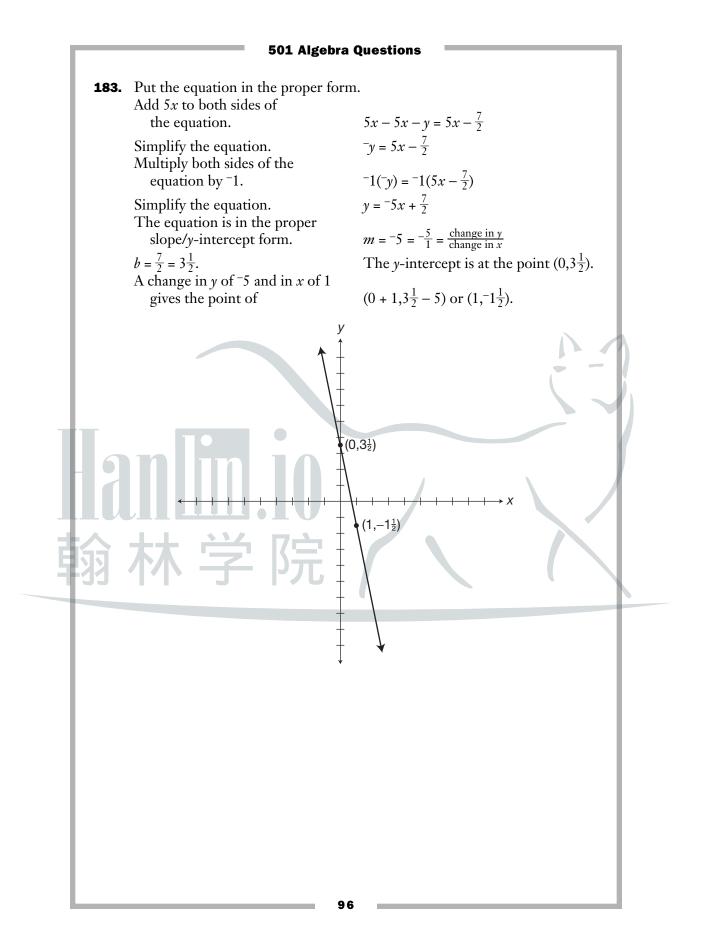


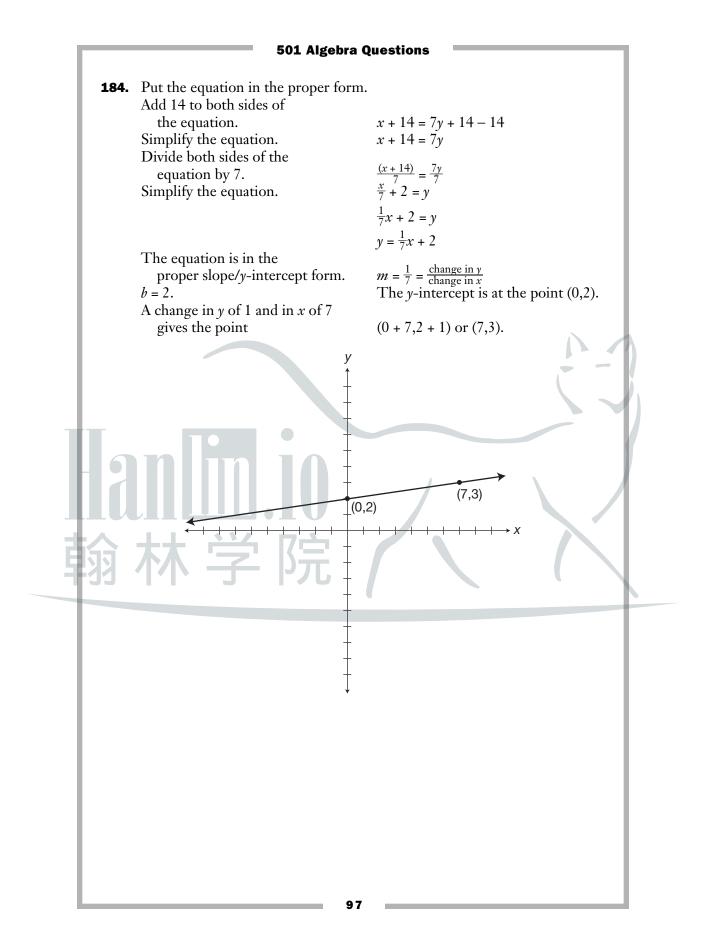


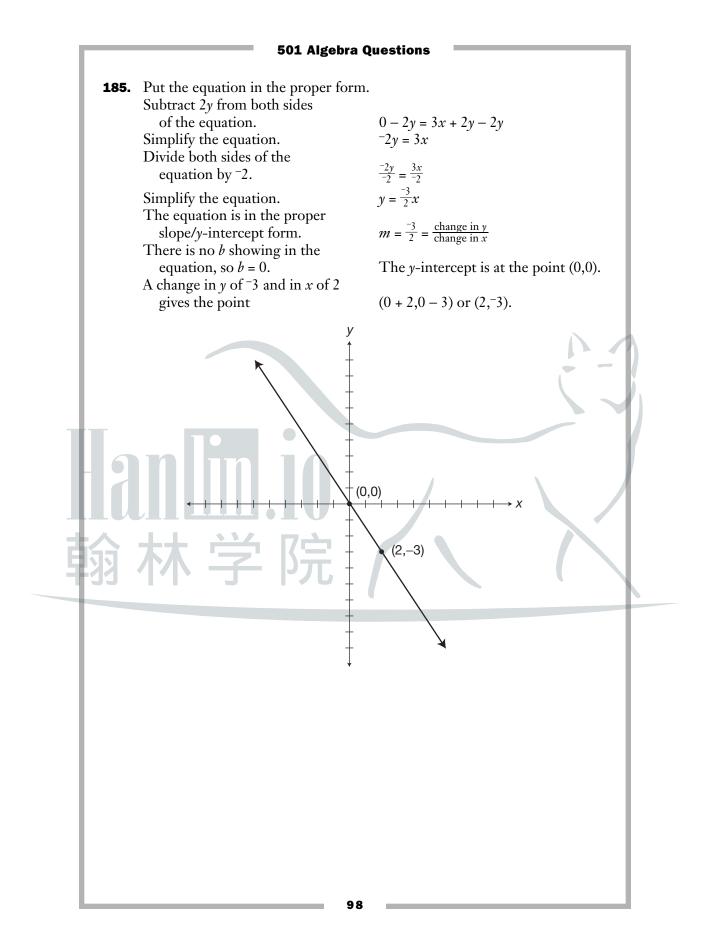


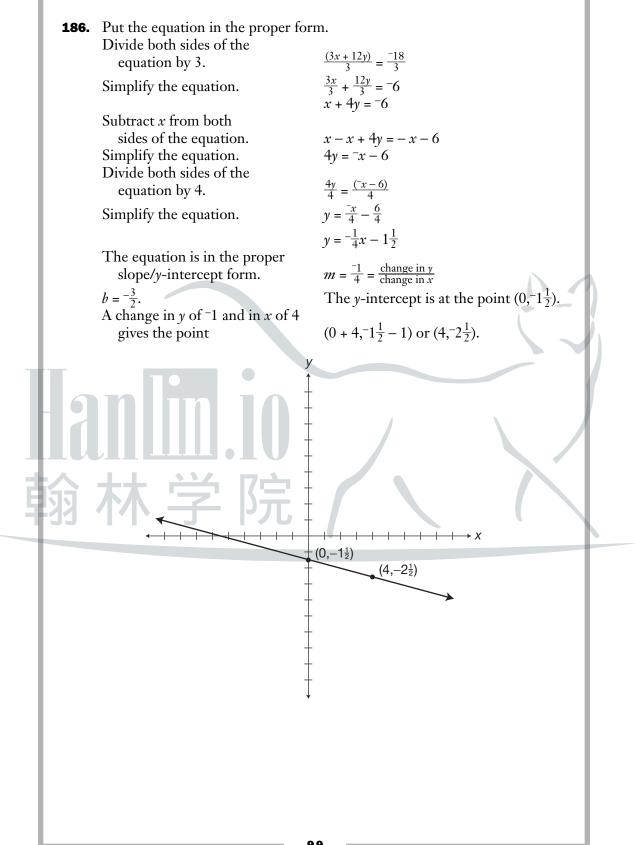


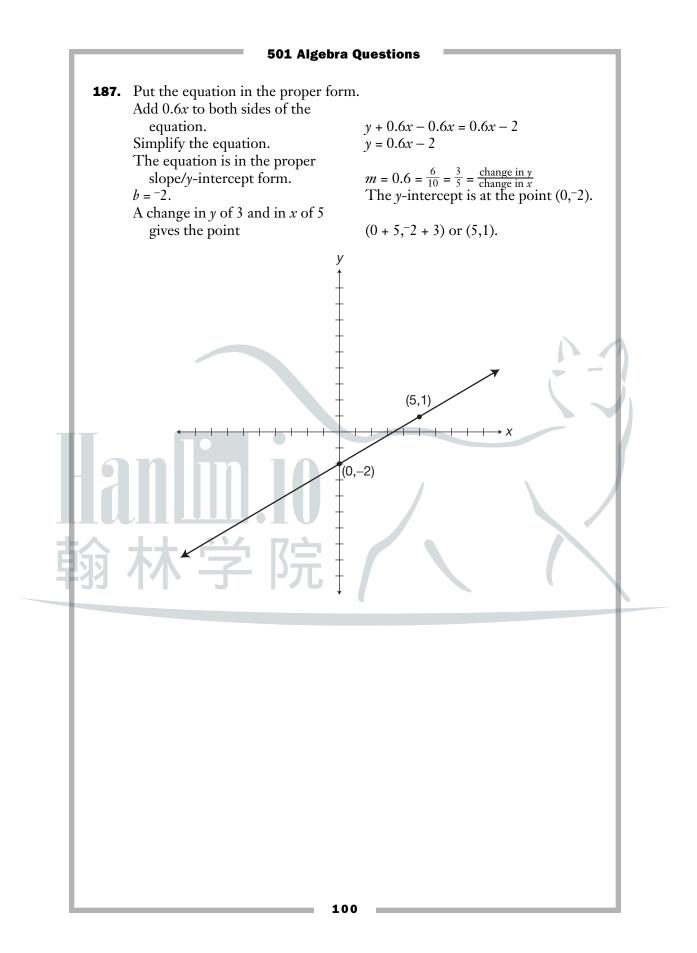
501 Algebra Questions 182. Put the equation in the proper form. Divide both sides of the $\frac{(3x+9y)}{3} = \frac{-27}{3}$ equation by 3. $\frac{3x}{3} + \frac{9y}{3} = -9$ x + 3y = -9Simplify the equation. Subtract *x* from both sides x - x + 3y = x - 93y = x - 9of the equation. Simplify the equation. Divide both sides of the $\frac{3y}{3} = \frac{(-x-9)}{3}$ equation by 3. $y = \frac{-x}{3} - \frac{9}{3}$ Simplify the equation. $y = \frac{-x}{3} - \frac{-9}{3}$ $y = \frac{-1}{3x} - 3$ The equation is in the proper $m = -\frac{1}{3} = \frac{\text{change in } y}{\text{change in } x}$ The *y*-intercept is at the point (0,-3). slope/y-intercept form. b = -3. A change in y of -1 and in x of 3(0 + 3, -3 - 1) or (3, -4). gives the point (0,-3) (3,-4) 95

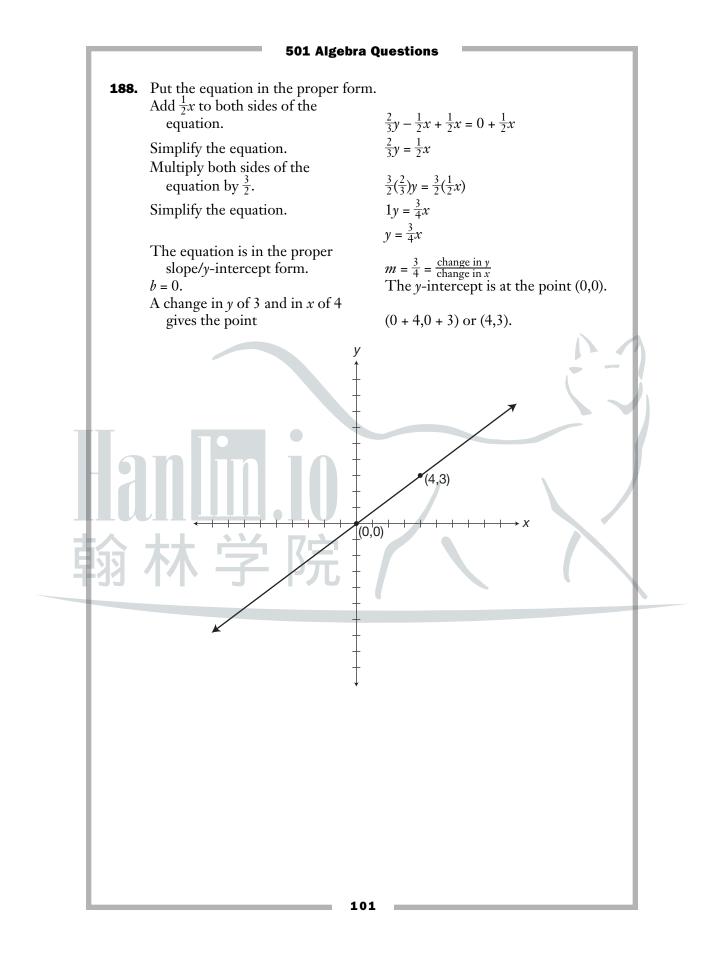


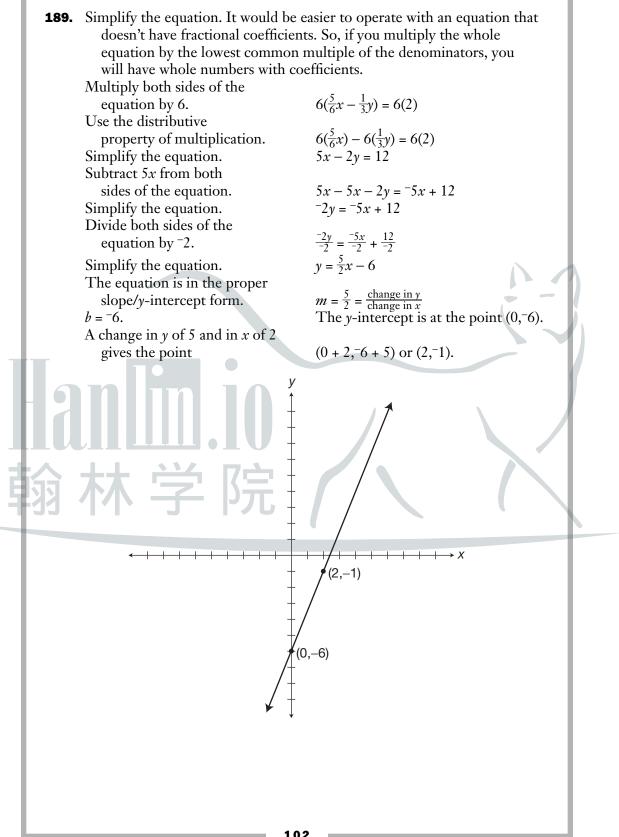


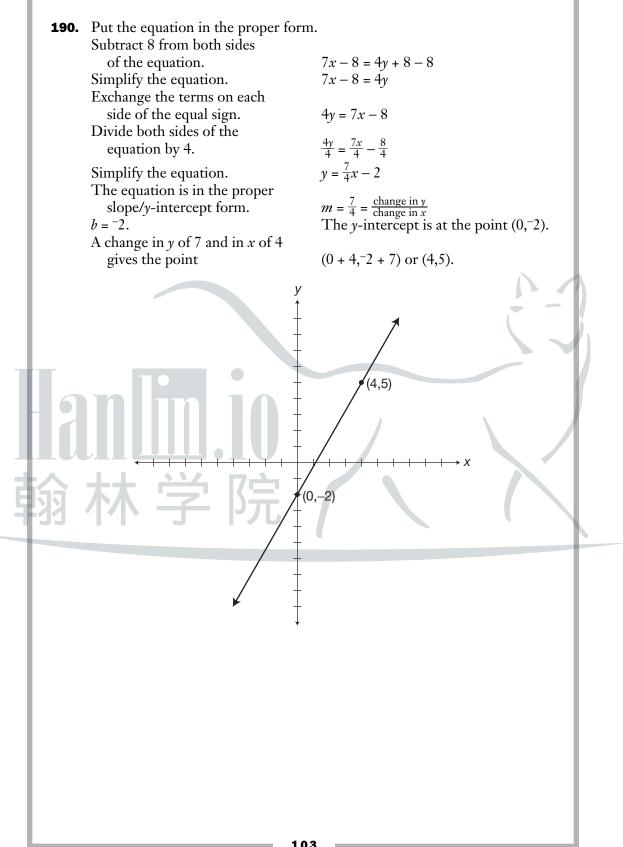


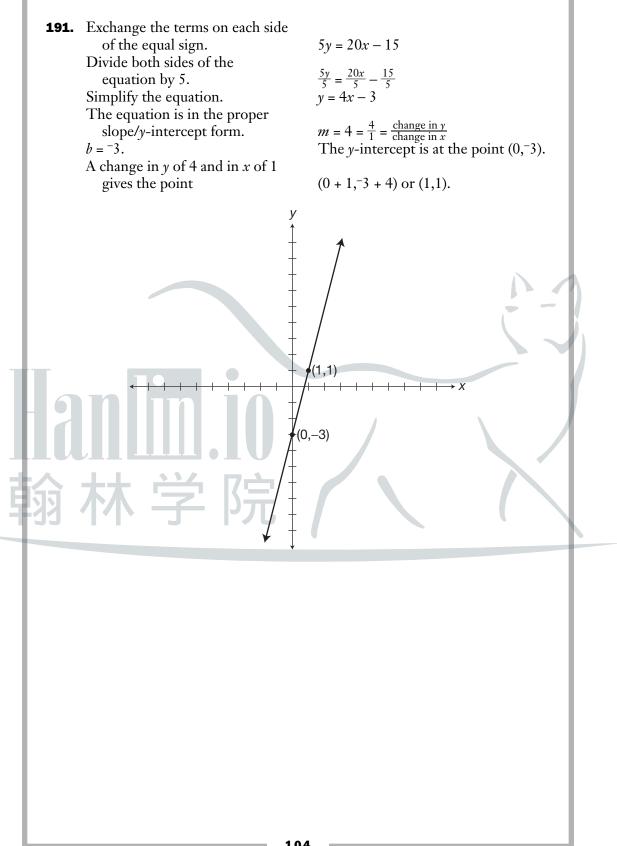


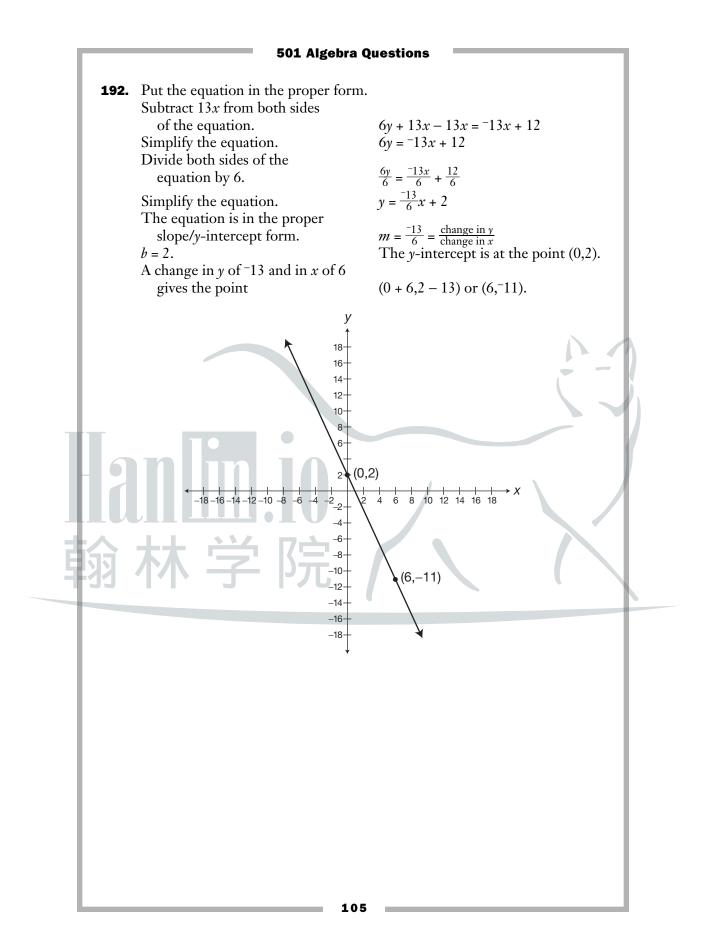


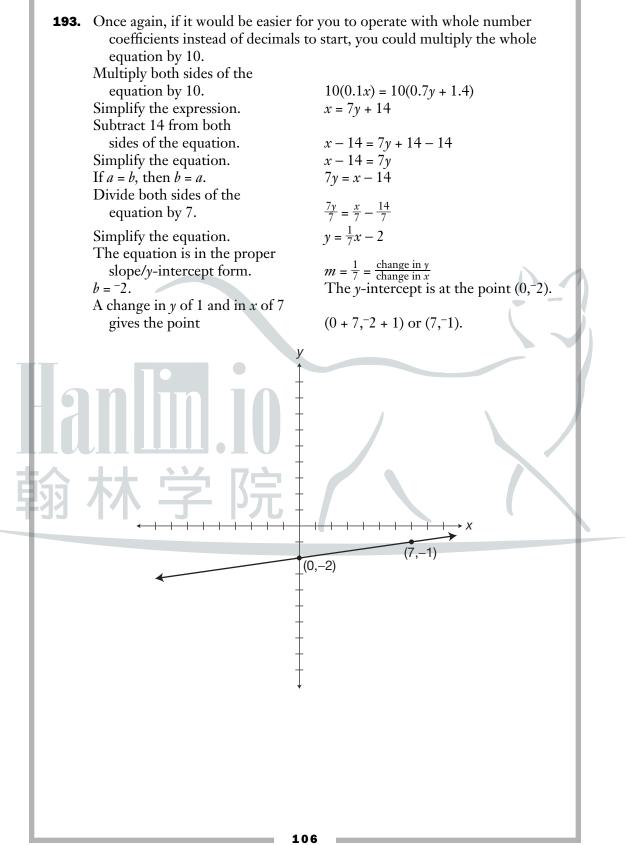


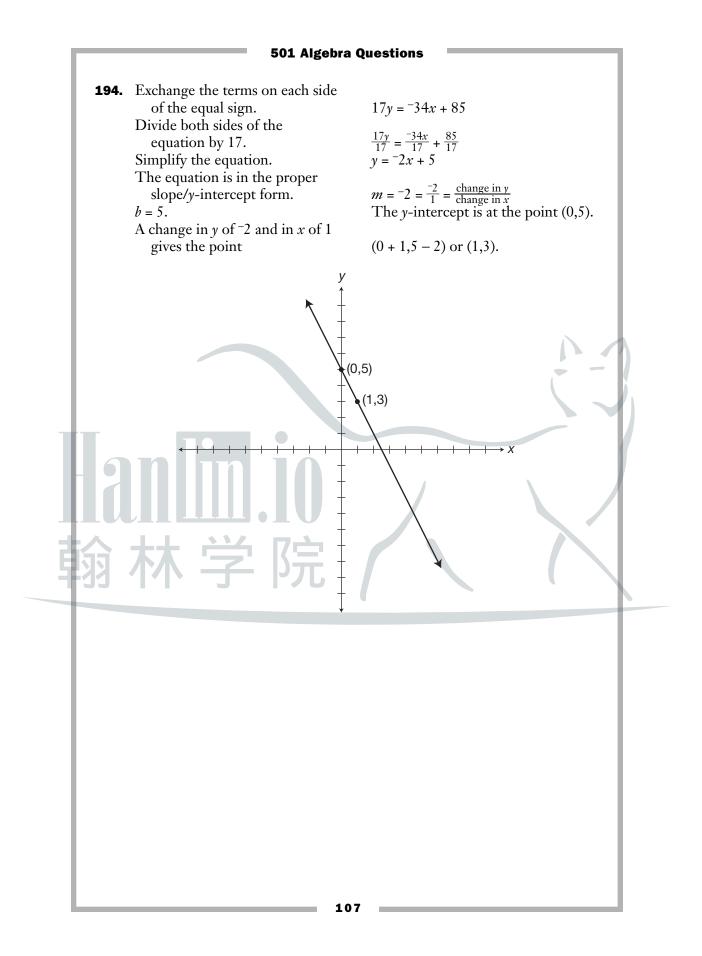


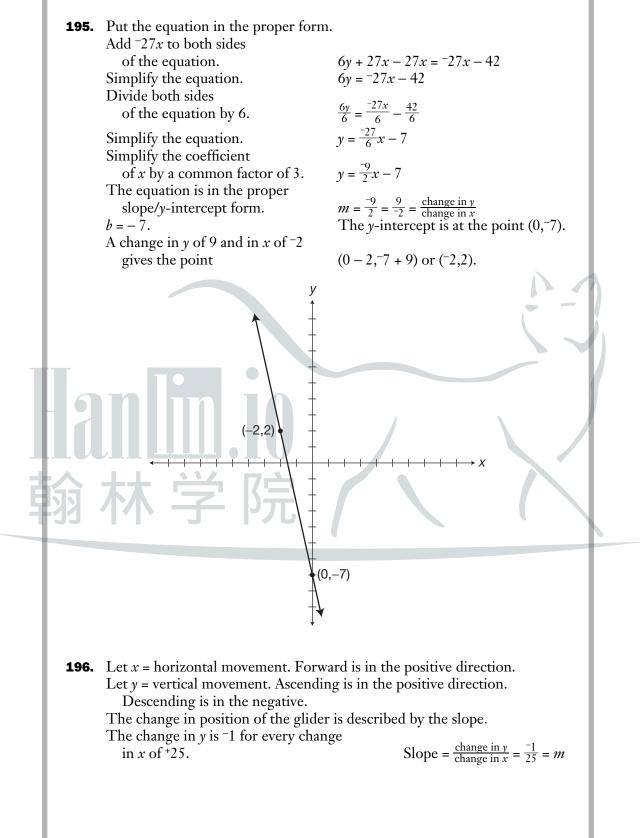












The starting position for the purposes of this graphic solution is at an altitude of 250 ft or *250. So: Using the standard form $y = mx + b$, you substitute the given values into the formula. A graph of this equation would have a slope of $\frac{1}{25}$ and the <i>y</i> -intercept would be at (0,250) 197. Let $y =$ the amount of a monthly bill. Let $x =$ the hours of Internet use for the month. The costs for the month will equal \$15 plus the \$.25 times the number of hours of use. Written as an equation, this information would be as follows: y = 0.25x + 15 A graph of this equation would have a slope of 0.25 or The <i>y</i> -intercept would be at (0,15) 198. Let $y =$ the cost of a scooter rental for one day. Let $x =$ the number of miles driven in one day. The problem tells us that the cost would be equal to the daily charges plus the 0.05 times the number of miles driven. Written as an equation, this would be The graph would have a <i>y</i> -intercept at $(0,20)$ and the slope would be The graph would have a <i>y</i> -intercept at $(0,20)$ and the slope would be y = 0.05x + 20 $\frac{5}{100} = \frac{1}{20}$ 199. Let $y =$ the total cost for equipment. Let $x =$ the number of tanks used during the week. The problem tells us that the cost would be equal to the weekly charge for gear rental plus 8 times the number of tanks used. A formula that would represent this information would be: y = 8x + 150 The <i>y</i> -intercept would be at $(0,150)$ and the slope = $8 = \frac{5}{1}$. 200. Let $y =$ the number of birds that visited a backyard feeder. Let $x =$ the number of birds that visited he feeder. An equation that represents the statement would be: The <i>y</i> -intercept is $(0,0)$ and the slope $= 7 = \frac{7}{1}$.		501 Algebra Questions	
 would be: <u>y = 8x + 150</u> The <i>y</i>-intercept would be at (0,150) and the slope = 8 = ⁸/₁. 200. Let <i>y</i> = the number of birds that visited a backyard feeder. Let <i>x</i> = the number of chickadees that visited the feeder. An equation that represents the statement would be: <u>y = 7x</u> 	198.	 The starting position for the purposes of this graphic solution is at an altitude of 250 ft or +250. So: Using the standard form y = mx + b, you substitute the given values into the formula. A graph of this equation would have a slope of -1/25 and the <i>y</i>-intercept would be at Let y = the amount of a monthly bill. Let x = the hours of Internet use for the month. The costs for the month will equal \$15 plus the \$.25 times the number of hours of use. Written as an equation, this information would be as follows: A graph of this equation would have a slope of 0.25 or The <i>y</i>-intercept would be at Let y = the cost of a scooter rental for one day. Let x = the number of miles driven in one day. The problem tells us that the cost would be equal to the daily charges plus the 0.05 times the number of miles driven. Written as an equation, this would be The graph would have a <i>y</i>-intercept at (0,20) and the slope would be Let y = the total cost for equipment. Let x = the number of tanks used during the week. The problem tells us that the cost would be equal to the weekly charge for gear rental plus 8 times the number of tanks used. 	$\frac{y = \frac{-1}{25}x + 250}{(0,250)}$ $\frac{y = 0.25x + 15}{\frac{25}{100} = \frac{1}{4}}{(0,15)}$
Let x = the number of chickadees that visited the feeder. An equation that represents the statement would be: y = 7x		would be: The <i>y</i> -intercept would be at (0,150) and the	$\underline{y = 8x + 150}$
	200.	Let <i>x</i> = the number of chickadees that visited the feeder. An equation that represents the statement would be:	y = 7x

9

Solving Inequalities

If you compare Chapter 9 to Chapter 6, you will find only a few differences between solving inequalities and solving equalities. The methods and procedures you use are virtually the same. Your goal is to isolate the variable on one side of the inequality, and the result will be your solution. In this chapter, there will be 25 inequalities so you can practice your solving skills. Look at the following tips to see what makes solving inequalities different from solving equalities.

Tips for Solving Inequalities

- Keep the inequality symbol facing the same way when you perform an addition or subtraction to both sides of the inequality. Keep the symbol facing the same way when you multiply or divide by a positive factor. But remember to change the direction of the inequality when you multiply or divide by a negative factor.
- When you have fractional coefficients or terms in an equality or inequality, multiply both sides by the least common multiple of the denominators and work with whole numbers. If the

coefficients and/or terms are decimals, multiply by multiples of ten until you have whole numbers to work with.

Solve the following inequalities.

201.
$$3x + 2 < 11$$

202. $4x - 6 > 30$
203. $\frac{2}{5}x \le 18$
204. $4x + 26 \ge 90$
205. $8 - 6x < 50$
206. $5x - 9 \le -2$
207. $2x + 0.29 > 0.79$
208. $-6(x + 1) \ge 60$
209. $3(5 - 4x) < x - 63$
210. $4(x + 1) < 5(x + 2)$
211. $2(7x - 3) \ge -2(5 + 3x)$
212. $16x - 1 < 4(6 - x)$
213. $\frac{x}{0.3} \le 20$
214. $\frac{4}{3}x - 5 > x - 2$
215. $3x + 5 \ge -2(x + 10)$
216. $-4x + 3(x + 5) \ge 3(x + 2)$
217. $x - \frac{3}{4} < -\frac{3}{4}(x + 2)$
218. $\frac{3}{2}x + 0.1 \ge 0.9 + x$
219. $x - 4\frac{1}{3} < 9 + \frac{2}{3}x$
220. $-7(x + 3) < -4x$
221. $\frac{5}{4}(x + 4) > \frac{1}{2}(x + 8) - 8$
222. $3(1 - 3x) \ge -3(x + 27)$
223. $-5[9 + (x - 4]] \ge 2(13 - x)$
224. $11(1 - x) \ge 3(3 - x) - 1$
225. $3(x - 16) - 2 < 9(x - 2) - 7x$

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

	<u>Un</u>	derlined inequalities show the simplified result.	
	201.	Subtract 2 from both sides of the inequality. Simplify the inequality. Divide both sides of the inequality by 3. Simplify.	3x + 2 - 2 < 11 - 2 3x < 9 $\frac{3x}{3} < \frac{9}{3}$ x < 3
	202.	Add 6 to both sides of the inequality. Simplify the inequality. Divide both sides of the inequality by 4. Simplify.	$4x-6+6 > 30+6$ $4x > 36$ $\frac{4x}{4} > \frac{36}{4}$ $x > 9$
101	203.	Multiply both sides of the inequality by $\frac{5}{2}$. Simplify.	$\frac{\frac{5}{2}(\frac{2}{5})x \le \frac{5}{2}(18)}{(\frac{10}{10})x \le \frac{5}{2}(\frac{18}{1})}$ $(1)x \le 45$ $x \le 45$
	204.	Subtract 26 from both sides of the inequality. Simplify. Divide both sides of the inequality by 4. Simplify the inequality.	$4x + 26 - 26 \ge 90 - 26$ $4x \ge 64$ $\frac{4x}{4} \ge \frac{64}{4}$ $x \ge 16$
	205.	Subtract 8 from both sides of the inequality. Simplify the inequality. Divide both sides of the inequality by ⁻⁶ and change the direction of the inequality sign. Simplify.	8 - 8 - 6x < 50 - 8 -6x < 42 $\frac{-6x}{-6} > \frac{42}{-6}$ <u>x > -7</u>

	206.	Add 10 to both sides of the inequality. Combine like terms on each side of	$5x - 9 + 9 \le -2 + 9$	
		the inequality.	$5x \le 7$	
		Divide both sides of the inequality by 5.	$\frac{5x}{5} \le \frac{7}{5}$	
		Simplify.	$x \leq \frac{7}{5}$	
			$\underline{x \le 1\frac{2}{5}}$	
	207.	inequality.	2x + 0.29 - 0.29 > 0.79 - 0.29	
		Combine like terms on each side of the inequality.	2x > 0.50	
		Divide both sides of the inequality by 2.	$\frac{2x}{2} > \frac{0.50}{2}$	
		Simplify the inequality.	$\frac{x}{x} > 0.25$	
	208.	Divide both sides of the inequality by ⁻ 6 and change the direction of the inequality sign.	$\frac{-6(x+1)}{-6} \le \frac{60}{-6}$	
T		Simplify the expressions.	$x + 1 \le -10$	
	- 9	Subtract 1 from both sides of the inequality.	$x + 1 - 1 \le -10 - 1$	
		Simplify.	$\underline{x \leq -11}$	
2	209.	Use the distributive property of multiplication.	3(5) - 3(4x) < x - 63	
Ę	55	Simplify.	15 - 12x < x - 63	
	-33	Add $12x$ to both sides of the inequality. Combine like terms on each side of	15 - 12x + 12x < x + 12x - 63	
		the inequality. Add 63 to both sides of the	15 < 13x - 63	
		inequality. Simplify the inequality.	15 + 63 < 13x - 63 + 63 78 < 13x	
		Divide both sides of the inequality		
		by 13. Simplify.	$\frac{\frac{78}{13}}{\frac{6}{13}} < \frac{\frac{13x}{13}}{\frac{6}{13}}$	

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210.	Use the distributive property of multiplication. Simplify. Subtract 4 from both sides of the	4(x) + 4(1) < 5(x) + 5(2) 4x + 4 < 5x + 10
	inequality. Combine like terms on each side	4x + 4 - 4 < 5x + 10 - 4
	of the inequality. Subtract $5x$ from both sides of	4x < 5x + 6
	the inequality.	4x - 5x < 5x - 5x + 6
	Simplify the inequality. Multiply both sides of the equation by ⁻¹ and change the direction of the	$\overline{x} < 6$
	inequality sign.	-1(-x) > -1(6)
	Simplify.	$\underline{x > -6}$
211.	Use the distributive property of	
	multiplication.	$2(7x) - 2(3) \ge -2(5) - 2(3x)$
	Simplify the expressions.	$14x - 6 \ge -10 - 6x$
	Add $6x$ to both sides of the inequality.	$14x + 6x - 6 \ge -10 - 6x + 6x$
	Combine like terms.	$20x - 6 \ge -10$
	Add 6 to both sides of the inequality.	$20x - 6 + 6 \ge -10 + 6$
	Simplify.	$20x \ge -4$
6	Divide both sides of the inequality	
	by 20.	$\frac{20x}{20} \ge \frac{-4}{20}$
	Simplify.	$x \ge \frac{-4}{20}$
	Reduce the fraction to lowest terms.	$\underline{x \ge \frac{-1}{5}}$
212.	Use the distributive property of	
	multiplication.	16x - 1 < 4(6) - 4(x)
	Simplify.	16x - 1 < 24 - 4x
	Add 1 to both sides of the inequality.	16x - 1 + 1 < 1 + 24 - 4x
	Combine like terms.	16x < 25 - 4x
	Add $4x$ to both sides of the	
	inequality.	16x + 4x < 25 - 4x + 4x
	Combine like terms on each side	
	of the inequality.	20x < 25
	Divide both sides of the	
	inequality by 20.	$\frac{20x}{20} < \frac{25}{20}$
	Simplify and express the fraction	20 20
	in simplest terms.	$\underline{x < 1\frac{1}{4}}$
	Multiply both sides of the	
212	inequality by 0.3.	$0.3(\frac{-x}{0.3}) \le 0.3(20)$
213.	$\mathbf{H}_{\mathbf{C}}$	$0.3(_{0.3}) \ge 0.3(20)$
213.		
213.	Simplify the expressions on both sides.	$\overline{x} \le 6$

	501 Algebra Questio	
	Multiply both sides of the inequality by ⁻ 1 and change the direction of the inequality sign. Simplify the expressions.	$ \frac{-1(-x) \ge -1(6)}{x \ge -6} $
214.	Add 5 to both sides of the inequality.	$\frac{4}{3}x - 5 + 5 > x - 2 + 5$
	Simplify.	$\frac{4}{3}x > x + 3$
	Subtract $1x$ from both sides of the inequality.	$\frac{4}{3}x - x > x - x + 3$
	moquanty.	$\frac{4}{3}x - \frac{3}{3}x > x - x + 3$
	Simplify the expressions.	$\frac{1}{3}x > 3$
	Multiply both sides of the inequality	
	by 3.	$3(\frac{1}{3}x) > 3(3)$
		$\frac{3}{1}(\frac{1}{3}x) > 3$ (3)
	Simplify the expressions.	$\frac{x > 9}{x > 9}$
215.	Use the distributive property of	
	multiplication. Simplify.	$3x + 5 \ge -2(x) - 2(10)$ $3x + 5 \ge -2x - 20$
	Subtract 5 from both sides of the	
	inequality. Combine like terms on each side of	$3x + 5 - 5 \ge -2x - 20 - 5$
	the inequality.	$3x \ge -2x - 25$
	Add $2x$ to both sides of the inequality.	$3x + 2x \ge 2x - 2x - 25$
	Combine like terms.	$5x \ge -25$ $\frac{5x}{5} \ge \frac{-25}{5}$
	Divide both sides of the inequality by 5. Simplify.	$\frac{1}{5} \ge \frac{1}{5}$ $x \ge -5$
	1	<u></u>
216.	Use the distributive property of multiplication.	$^{-4}x + 3(x) + 3(5) \ge 3(x) + 3(2)$
	Simplify.	$-4x + 3x + 15 \ge 3x + 6$
	Combine like terms.	$(^{-}4x + 3x) + 15 \ge 3x + 6$
	Simplify.	$\overline{x} + 15 \ge 3x + 6$
	Add x to both sides of the inequality.	$x - x + 15 \ge x + 3x + 6$
	Combine like terms. Subtract 6 from both sides of the	$15 \ge 4x + 6$
	inequality.	$15 - 6 \ge 4x + 6 - 6$
	Simplify.	$9 \ge 4x$
	Divide both sides of the inequality by 4.	$\frac{9}{4} \ge \frac{4x}{4}$
	Simplify.	$\frac{9}{4} \ge x$
	Express the fraction in its simplest form.	$2\frac{1}{4} \ge x$

217.	You can simplify equations (and inequalities))
	with fractions by multiplying them by a	
	common multiple of the denominators.	
	Multiply both sides of the inequality	4(
	by 4.	$4(x - \frac{3}{4}) < 4(\frac{-3}{4}(x + 2))$
	Use the distributive property	4(2) $4(3)$ $4(-3)$ (2)
	of multiplication.	$4(x) - 4(\frac{3}{4}) < 4(\frac{-3}{4})(x+2)$
	Simplify the expressions.	4x - 3 < -3(x + 2)
	Use the distributive property of	4x - 3 < -3(x) - 3(2)
	multiplication.	4x - 3 < 3(x) - 3(2) 4x - 3 < -3x - 6
	Simplify. Add 3 to both sides of the inequality.	4x - 3 < 3x - 6 4x - 3 + 3 < -3x - 6 + 3
	Combine like terms.	4x < -3x - 3
	Add $3x$ to both sides of the equation.	3x + 4x < 3x - 3x - 3
	Combine like terms.	7x < -3
		$\frac{7x}{7} < \frac{-3}{7}$
	Divide both sides of the inequality by 7. Sure, you have a fraction for an answer,	7 < 7
	but it can be easier to operate with	
	whole numbers until the last step.	
	Simplify the expressions.	$x < \frac{-3}{7}$
T	Simplify the expressions.	
218.	Subtract 0.1 from both sides of the	
	inequality.	$\frac{3}{2}x + 0.1 - 0.1 \ge 0.9 - 0.1 + x$
	Combine like terms on each side of the	1
	inequality.	$\frac{3}{2}x \ge 0.8 + x$
	Subtract <i>x</i> from both sides of the	
	inequality.	$\frac{3}{2}x - x \ge 0.8 + x - x$
	Simplify. — РТ	$\frac{1}{2}x \ge 0.8$
	Multiply both sides of the inequality by 2.	$2(\frac{1}{2}x) \ge 2(0.8)$
	Simplify the expressions.	$x \ge 1.6$
219.	Change the term to an improper fraction.	$x - \frac{13}{3} < 9 + \frac{2}{3}x$
	Multiply both sides of the inequality by 3.	$3(x - \frac{13}{3}) < 3(9 + \frac{2}{3}x)$
	Use the distributive property of	
	multiplication.	$3(x) - 3(\frac{13}{3}) < 3(9) + 3(\frac{2}{3}x)$
	Simplify the terms.	3x - 13 < 27 + 2x
	Add 13 to both sides of the inequality.	3x - 13 + 13 < 13 + 27 + 2x
	Combine like terms and simplify.	3x < 40 + 2x
	Subtract $2x$ from both sides of the	
	inequality.	3x - 2x < 40 + 2x - 2x
	Simplify.	$\underline{x < 40}$
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	220.	Use the distributive property of multiplication. Simplify the terms. Add 21 to both sides of the inequality. Simplify by combining like terms. Add 4 <i>x</i> to both sides of the inequality. Simplify the terms. Divide both sides of the inequality by ⁻³ and change the direction of the inequality sign. Simplify the expressions.	$\begin{array}{l} -7(x) - 7(3) < -4x \\ -7x - 21 < -4x \\ -7x - 21 + 21 < -4x + 21 \\ -7x < -4x + 21 \\ -7x + 4x < -4x + 4x + 21 \\ -3x < 21 \end{array}$ $\begin{array}{l} \frac{-3x}{-3} > \frac{21}{-3} \\ x > -7 \end{array}$
	221.	multiplication.	$\frac{5}{4}(x) + \frac{5}{4}(4) > \frac{1}{2}(x) + \frac{1}{2}(8) - 8$
		Simplify the terms.	$\frac{5}{4}x + 5 > \frac{1}{2}x + 4 - 8$
		Combine like terms. Subtract $\frac{1}{2}x$ from both sides of the inequality.	$\frac{5}{4}x + 5 > \frac{1}{2}x + 4 - 8$ $\frac{5}{4}x + 5 > \frac{1}{2}x - 4$ $\frac{5}{4}x - \frac{1}{2}x + 5 > \frac{1}{2}x - \frac{1}{2}x - 4$
		Combine like terms.	$\frac{3}{4}x + 5 > -4$
Т		Subtract 5 from both sides of the	4 <i>4</i> +3 > +
		inequality.	$\frac{3}{4}x + 5 - 5 > 4 - 5$
		Simplify.	$\frac{3}{4}x > -9$
		Multiply both sides by $\frac{4}{3}$	4.3 . 4
Л		(the reciprocal of $\frac{3}{4}$).	$\frac{4}{3}(\frac{3}{4}x) > \frac{4}{3}(-9)$
R		Simplify the expressions.	x > -12
4	222.	Use the distributive property of	
_		multiplication.	$3(1) - 3(3x) \ge -3(x) - 3(27)$
		Simplify terms.	$3 - 9x \ge -3x - 81$
		Add $9x$ to both sides.	$3 - 9x + 9x \ge 9x - 3x - 81$
		Combine like terms. Add 81 to both sides of the inequality.	$3 \ge 6x - 81 3 + 81 \ge 6x - 81 + 81$
		Combine like terms.	$84 \ge 6x$
		Divide both sides of the inequality by 6.	$\frac{84}{6} \ge \frac{6x}{6}$
		Simplify.	$\begin{array}{c} 6 = 6 \\ 14 \ge x \end{array}$
		Simpiny.	$\underline{1 + \leq \lambda}$
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223.	Remove the inner brackets, use the commutative property of addition and combine like terms.	$^{-5}[9 + x - 4] \ge 2(13 - x)$ $^{-5}[x + 9 - 4] \ge 2(13 - x)$
	Use the distributive property of	$^{-5}[x+5] \ge 2(13-x)$
	multiplication.	$-5[x] - 5[5] \ge 2(13) - 2(x)$
	Simplify terms.	$-5x - 25 \ge 26 - 2x$
	Add $5x$ to both sides of the inequality.	$^{-5}x + 5x - 25 \ge 26 - 2x + 5x$
	Combine like terms.	$-25 \ge 26 + 3x$
	Subtract 26 from both sides of	
	the inequality.	$-25 - 26 \ge 26 - 26 + 3x$
	Combine like terms.	$-51 \ge 3x$
	Divide both sides of the inequality by 3.	$\frac{-51}{3} \ge \frac{3x}{3}$
	Simplify terms.	$\frac{-17 \ge x}{1}$
224.	Use the distributive property of multiplication.	$11(1) - 11(x) \ge 3(3) - 3(x) - 1$
	Simplify terms.	$\frac{11}{11} - 11x \ge 9 - 3x - 1$
_	Use the commutative property.	$11 - 11x \ge 9 - 1 - 3x$
	Combine like terms.	$11 - 11x \ge 8 - 3x$
	Subtract 8 from both sides of	
	the inequality.	$11 - 8 - 11x \ge 8 - 8 - 3x$
	Combine like terms.	$3 - 11x \ge -3x$
	Add $11x$ to both sides.	$3 - 11x + 11x \ge -3x + 11x$
$\mathbf{\wedge}$	Combine like terms.	$3 \ge 8x$
77	Divide both sides by 8.	$\frac{3}{8} \ge \frac{8x}{8}$
33	Simplify.	$\frac{\frac{3}{8} \ge x}{2}$
225.	Use the distributive property of	
	multiplication.	3(x) - 3(16) - 2 < 9(x) - 9(2) - 7x
	Simplify terms.	3x - 48 - 2 < 9x - 18 - 7x
	Use the commutative property to associate like terms.	3x - 48 - 2 < 9x - 7x - 18
	Simplify terms.	3x - 50 < 2x - 18
	Add 50 to both sides of the	50 20 10
	inequality.	3x - 50 + 50 < 2x - 18 + 50
	Combine like terms.	3x < 2x + 32
	Subtract $2x$ from both sides of	
	the inequality.	3x - 2x < 2x - 2x + 32
	Combine like terms.	x < 32

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Graphing Inequalities

In this chapter, you will practice graphing inequalities that have one or two variables. When there is only one variable, you use a number line. When there are two variables, you use a coordinate plane.



Tips for Graphing Inequalities

When using a number line to show the solution graph for an inequality, use a solid circle on the number line as the endpoint when the inequality symbol is \leq or \geq . When the inequality symbol is < or >, use an open circle to show the endpoint. A solid circle shows that the solution graph includes the endpoint; an open circle shows that the solution graph does not include the endpoint.

When there are two variables, use a coordinate plane to graph the solution. Use the skills you have been practicing in the previous chapters to transform the inequality into the slope/y-intercept form you used to graph equalities with two variables. Use the slope and the *y*-intercept of the transformed inequality to show the boundary line for your solution graph. Draw a solid line when the inequality symbol is \leq or \geq . Draw a dotted line when the inequality symbol is < or >. To complete the graph, shade the region above the boundary line when the inequality symbol is < or \geq . Shade the region below the boundary line when the inequality symbol is < or \leq .

A simple way to check your graphic solution is to pick a point on either side of the boundary line and substitute the x and y values in your inequality. If the result is a true statement, then you have shaded the correct side of the boundary line. An easy point to use, if it is not your *y*-intercept, is the origin (0,0).

Graph the following inequalities on a number line.

226. $x \ge 4$ **227.** *x* < ⁻¹ **228.** $x \le 6$ **229.** *x* < 5 **230.** x > 1Graph the following inequalities on a coordinate plane. (Use graph paper.) **231.** y < x + 1**232.** $y \ge -x + 2$ **233.** y < 4x - 5**234.** $\frac{1}{2}x + y \le 3$ **235.** 2y - 3x < 8**236.** $y + 2 \le 3x + 5$ **237.** $3x - 4 \ge 2y$ **238.** $\frac{3}{4}y + 6 \ge 3x$ **239.** $0.5\gamma - x + 3 > 0$ **240.** $x - y \le 7$ **241.** $\frac{\gamma}{3} < \frac{2}{3} - x$ **242.** $-3y + 9x \le -6$ **243.** 0.5x > 0.3 y - 0.9**244.** $3x - y \le 7x + y - 8$ **245.** 3y + 4x < 9 - 2x**246.** $-12 \le -3(x + y)$ **247.** $9y + 7 \ge 2(x + 8)$ **248.** $\frac{x}{3} + y \le 3x - 5$ **249.** $2(y+3) - x \ge 6(1-x)$ **250.** $-28y \ge 2x - 14(y + 10)$

Answers

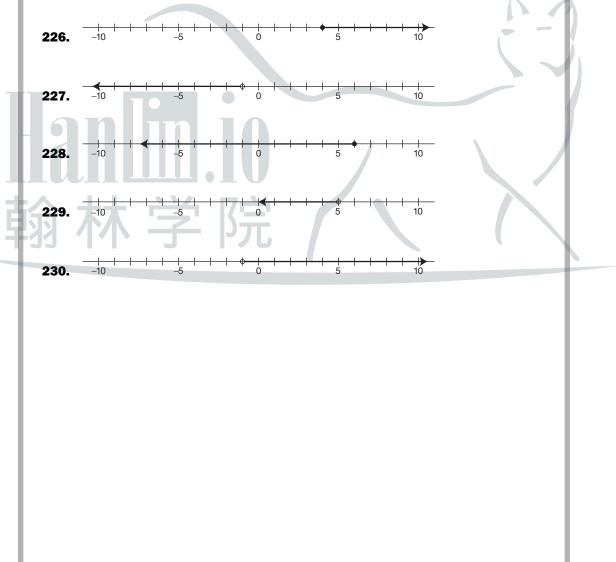
Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

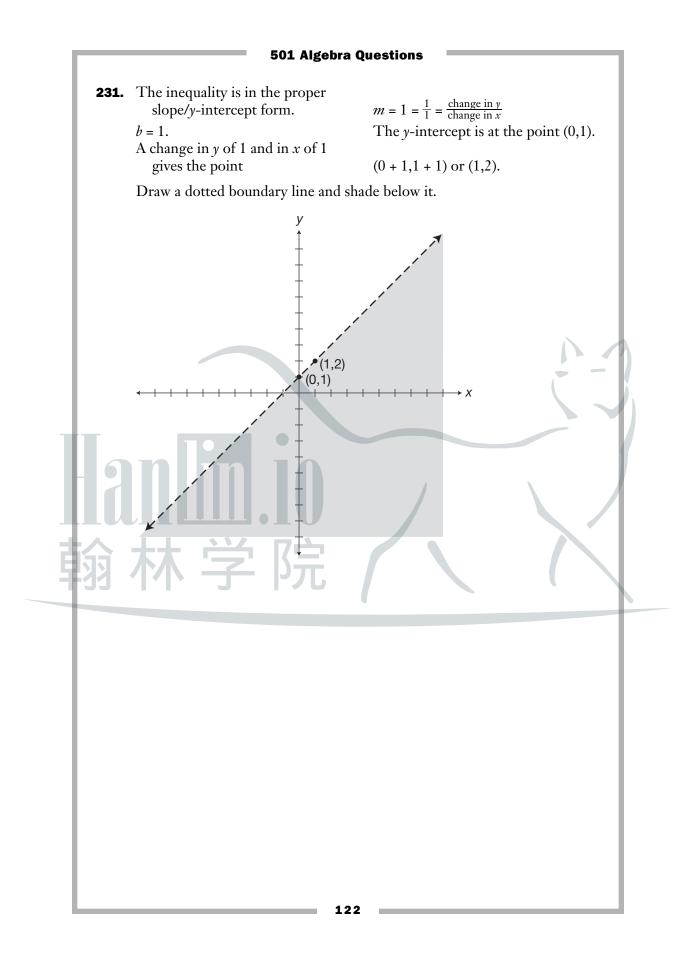
Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

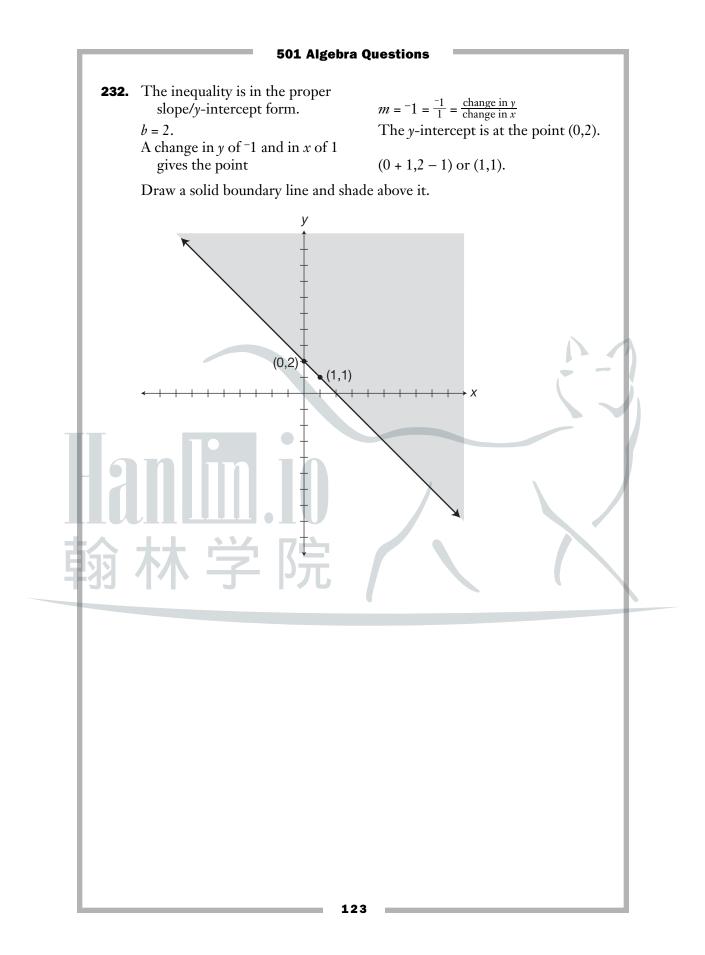
When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

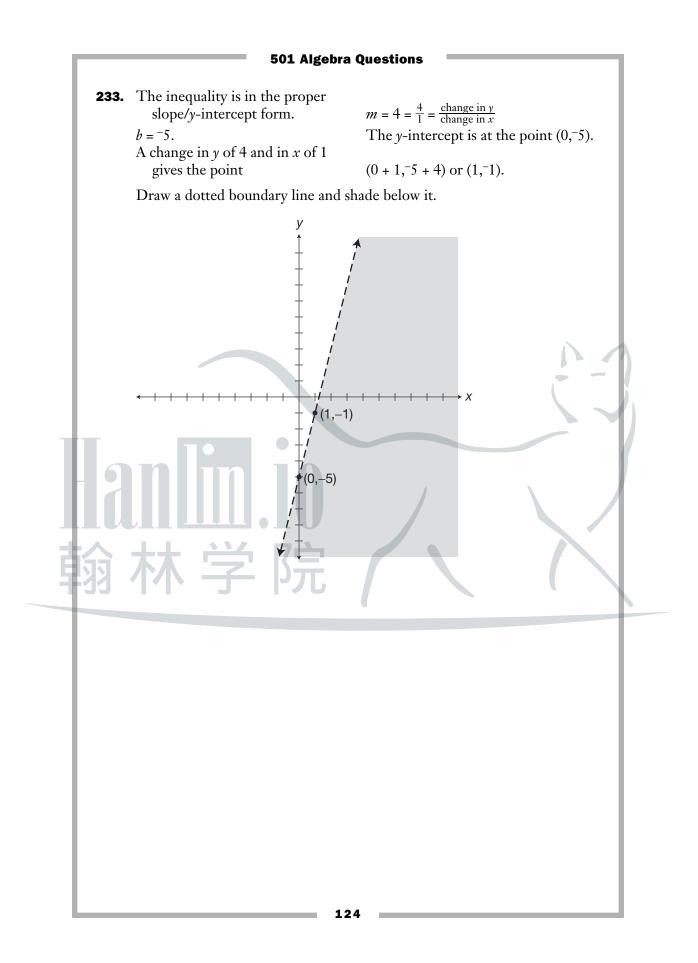
Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

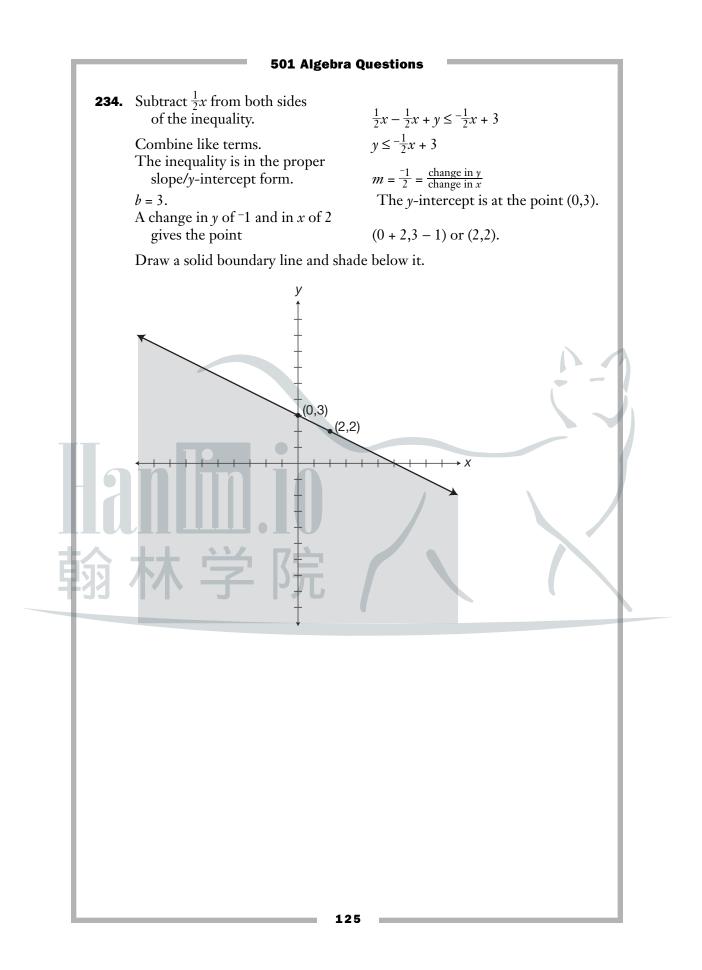
The answers to these questions are the graphs.

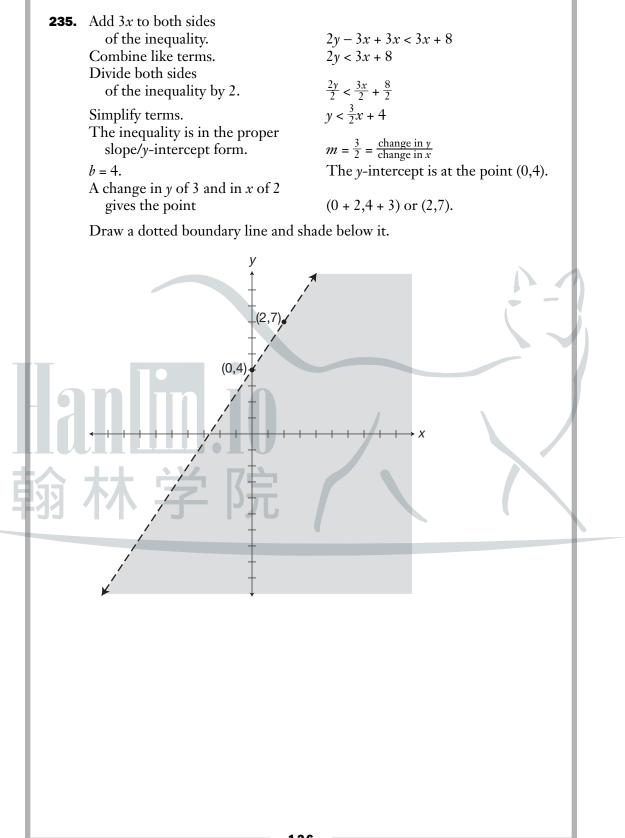


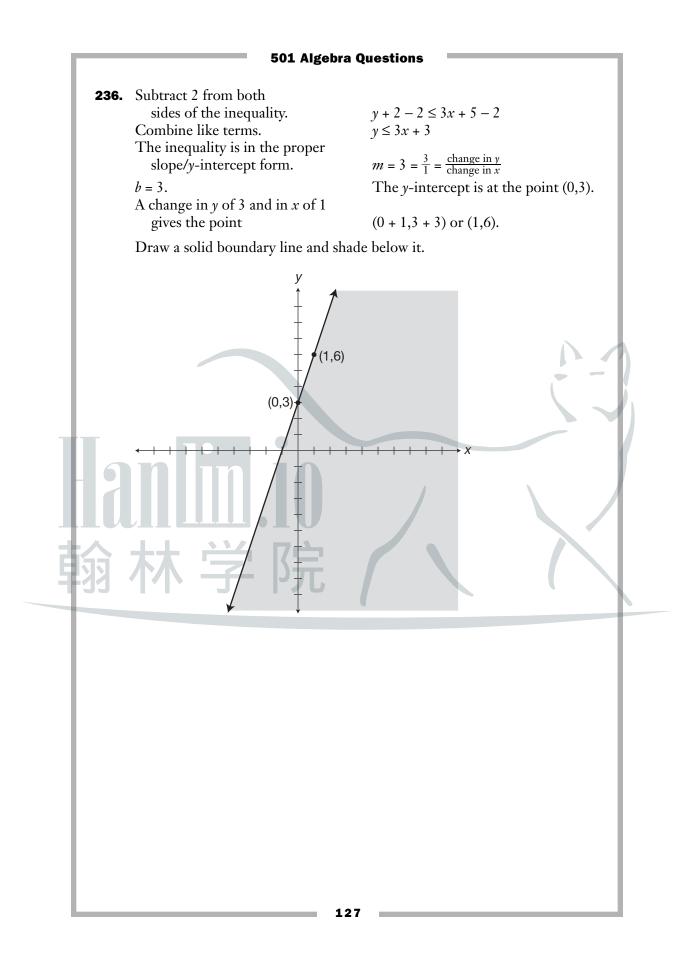


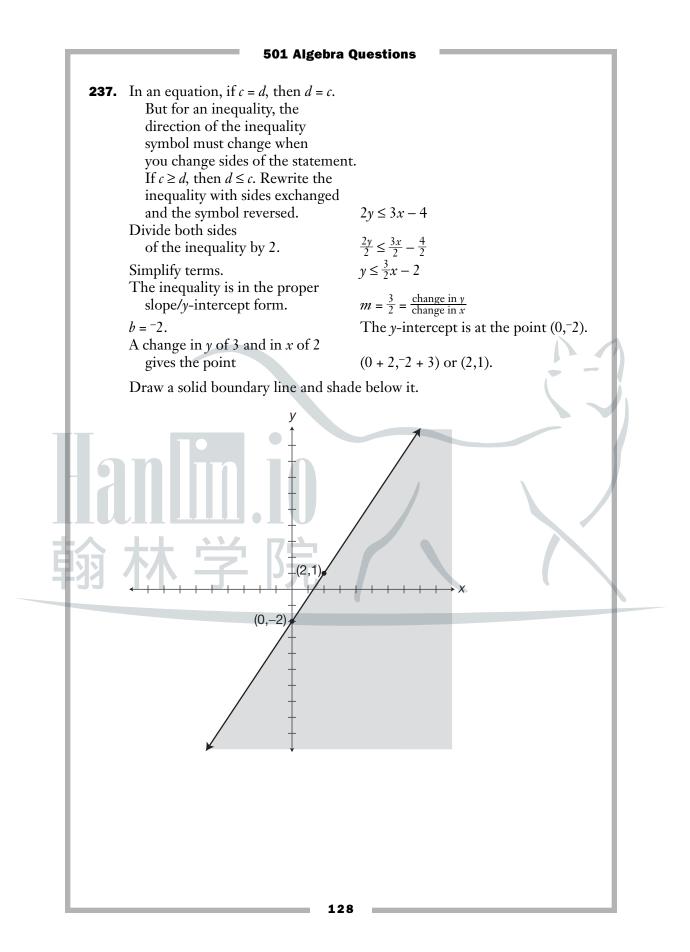


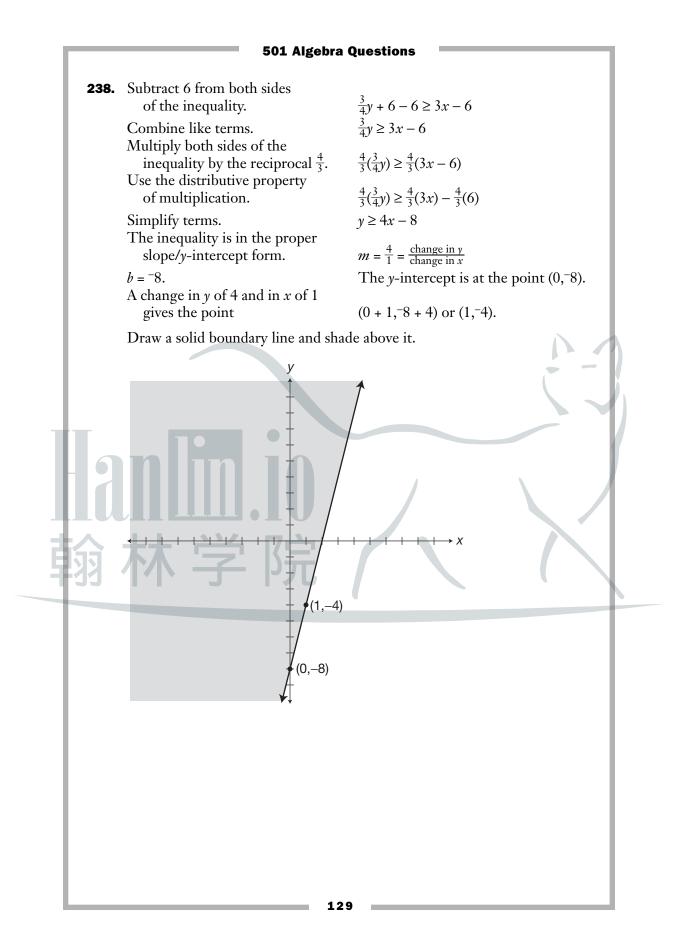


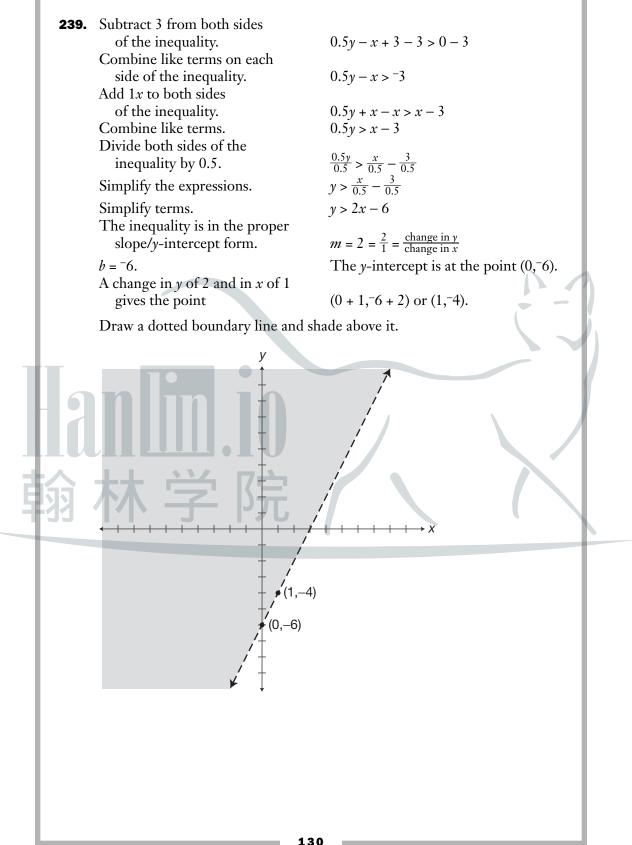


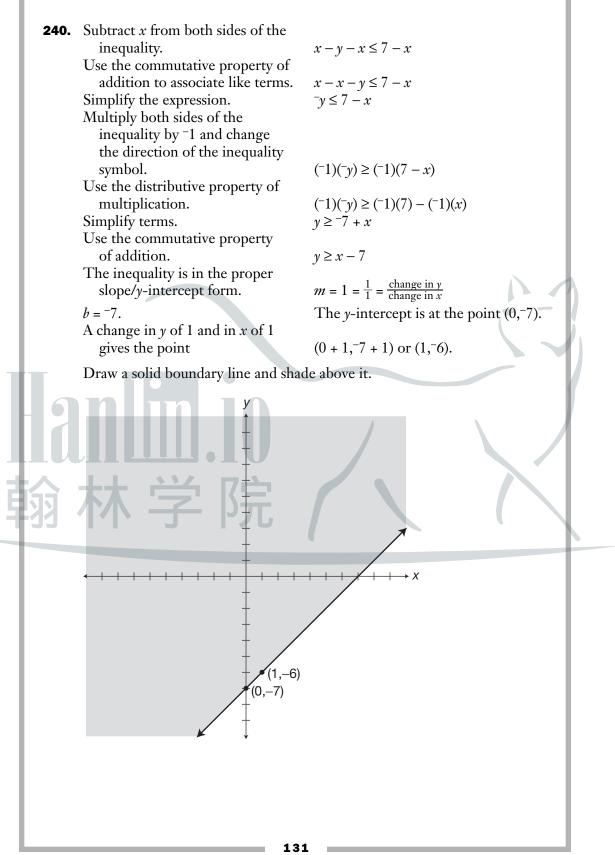


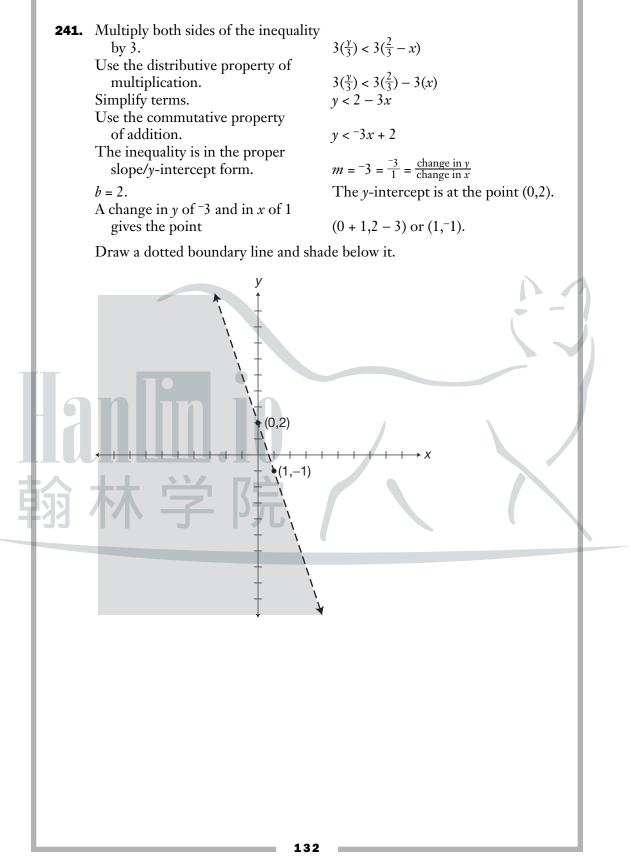


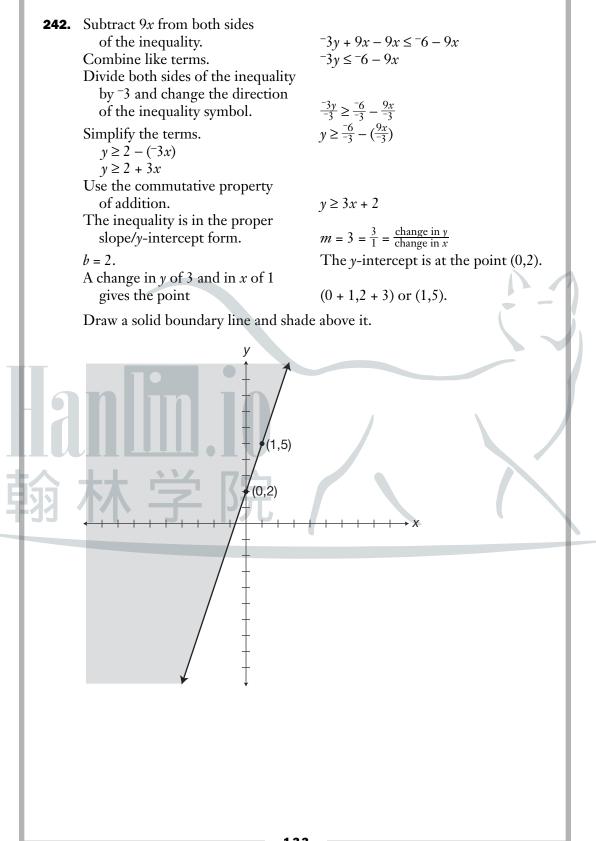


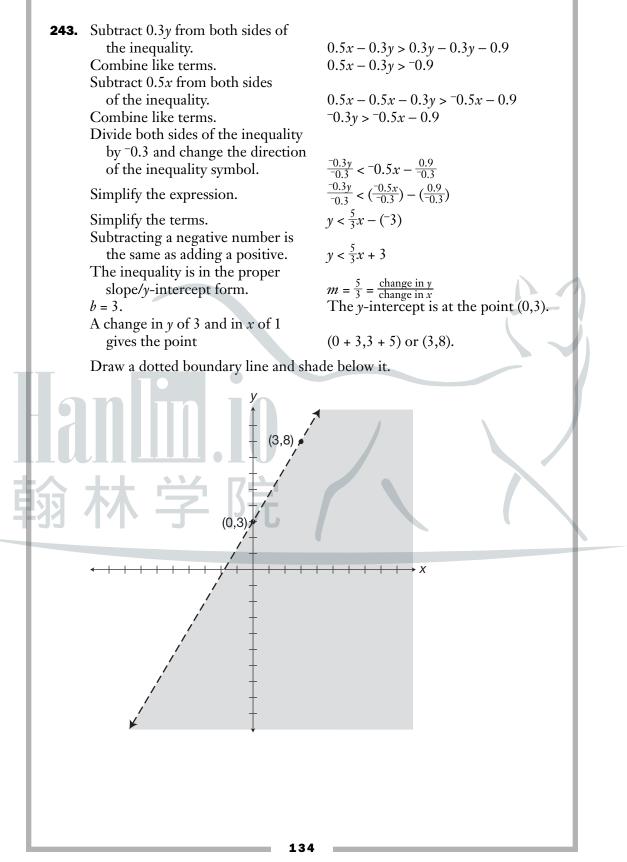


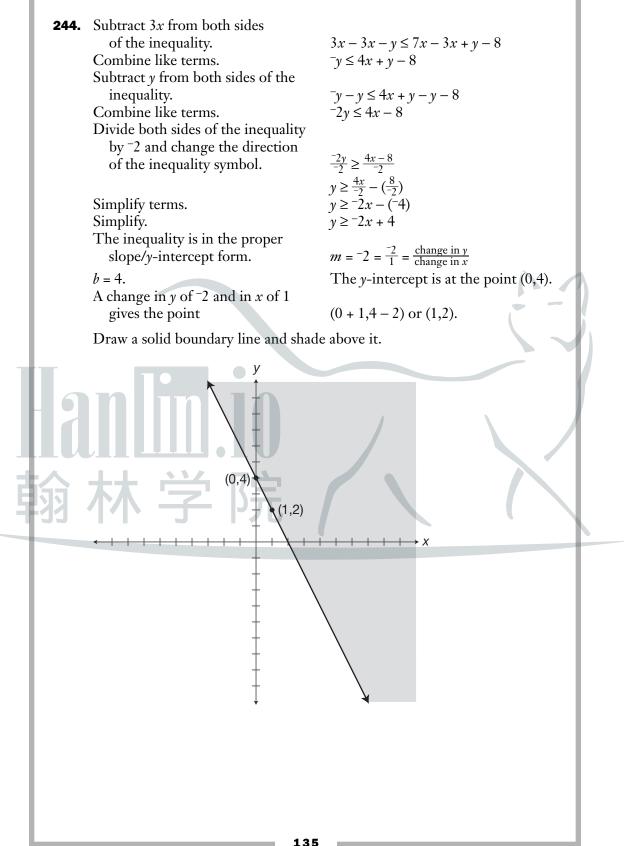


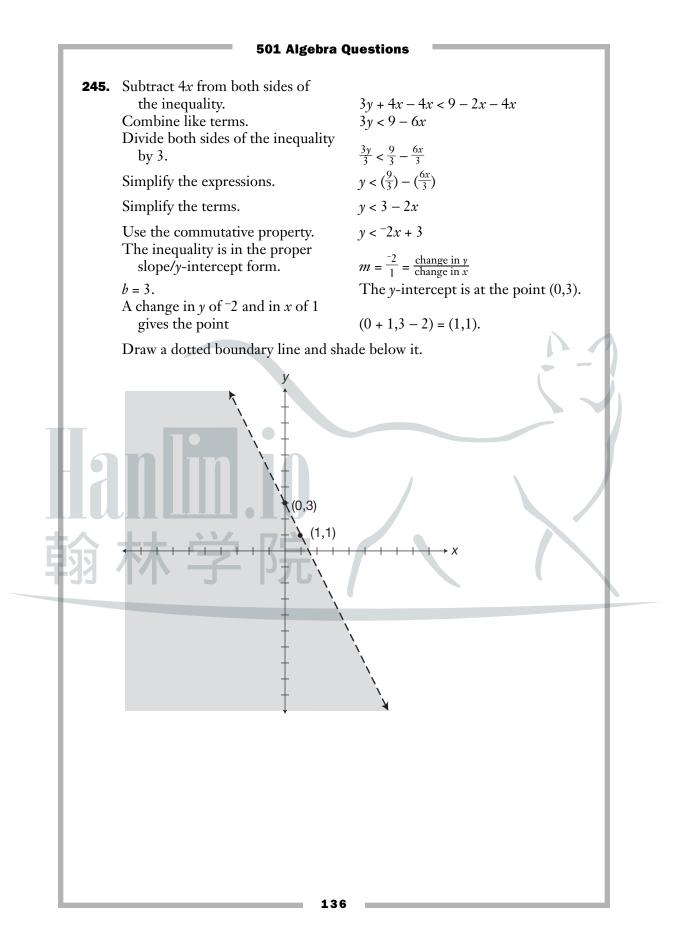


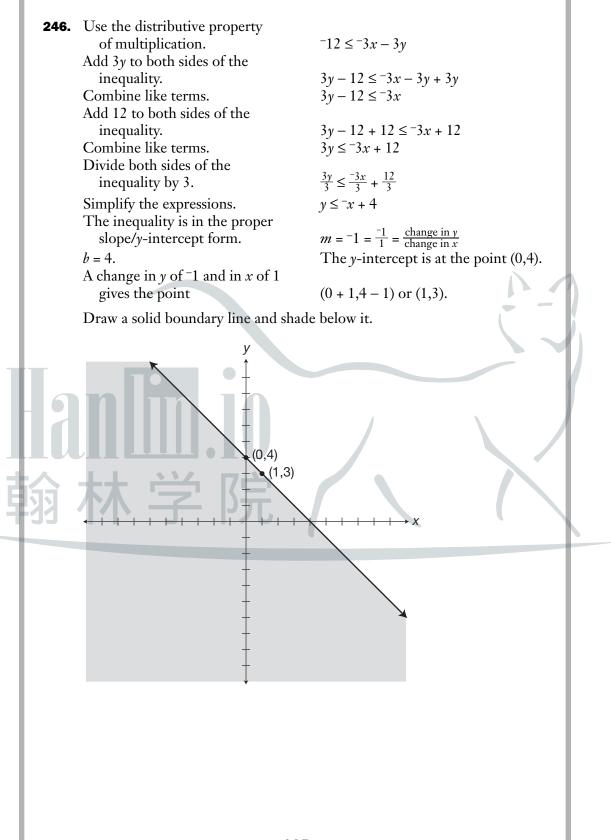




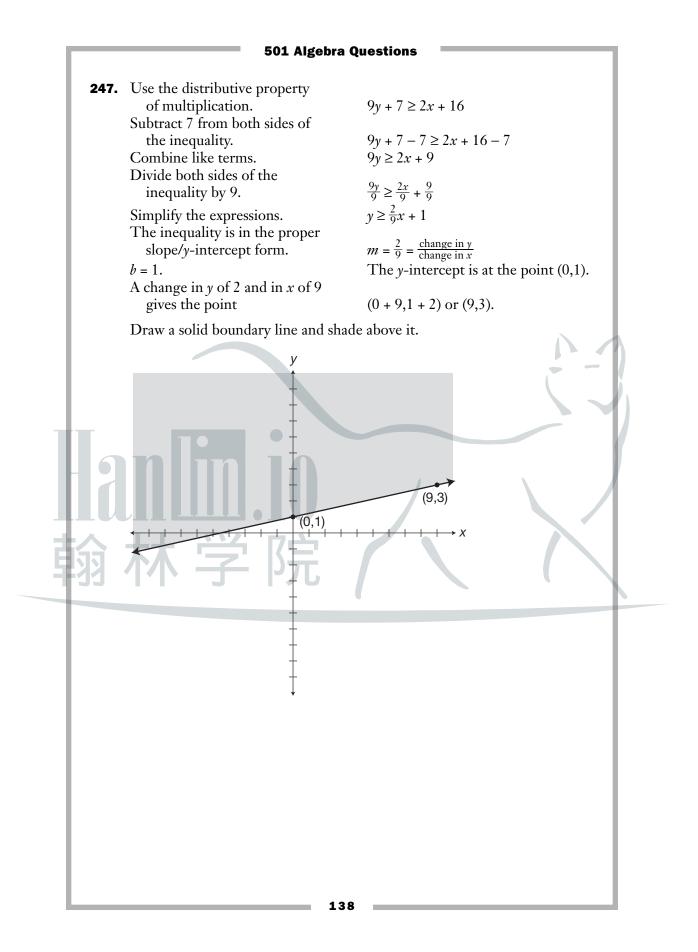


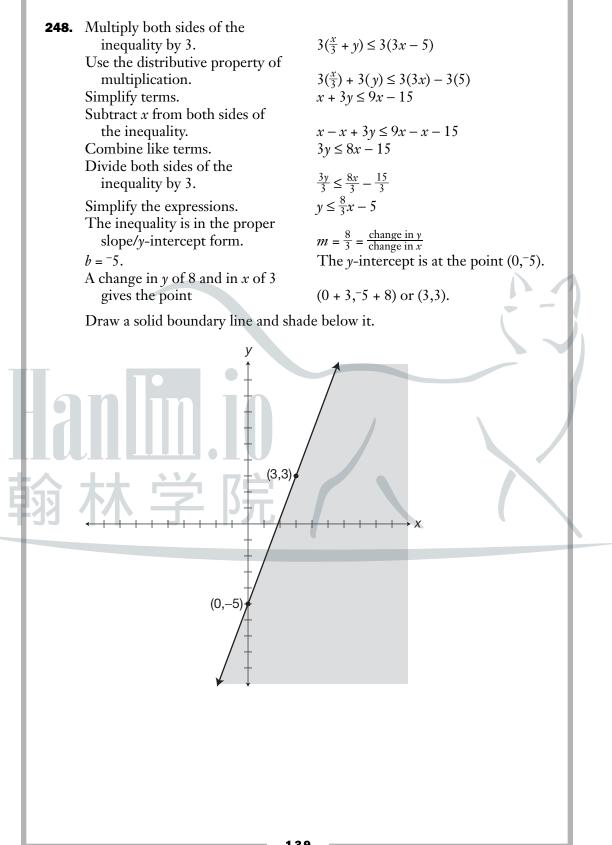


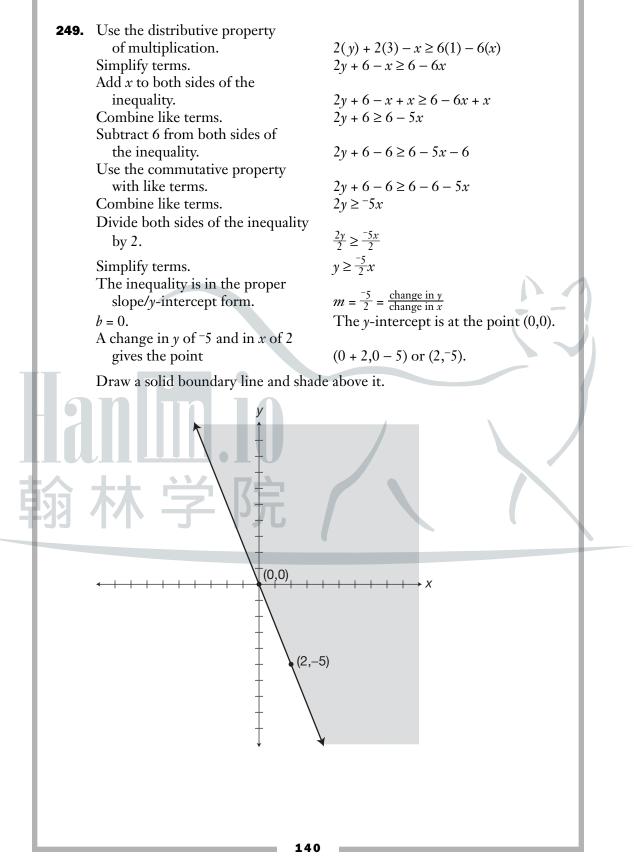


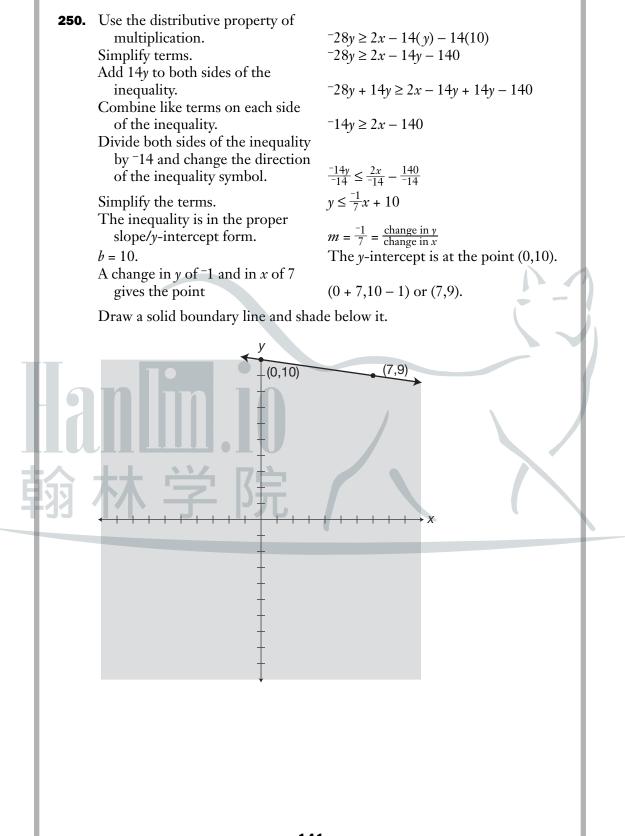


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Graphing Systems of Linear Equations and Inequalities



This chapter will present 15 systems of equalities and ten systems of inequalities as practice in finding solutions graphically. You will find complete explanations and graphs in the answer explanations.

Graphing systems of linear equations on the same coordinate plane will give you a solution that is common to both equations. There are three possibilities for a pair of equations:

- The solution will be one coordinate pair at the point of intersection.
- The solution will be all the points on the line graph because the equations coincide.
- There will be no solution if the line graphs have the same slope but different *y*-intercepts. In this case, the lines are parallel and will not intersect.

Pairs of inequalities can also have a common solution. The graphic solution will either be the common areas of the graphs of the inequalities or there will be no solution if the areas do not overlap.

Tips for Graphing Systems of Linear Equations and Inequalities

Transform each equation or inequality into the slope/y-intercept form.

For equations, graph the lines and look for the point or points of intersection. That is the solution.

For inequalities, graph the boundaries as the appropriate dotted or solid line and shade the area for each inequality depending upon the inequality symbol present. The intersection of the shaded areas will be the solution for the system.

When multiplying or dividing by a negative term, change the direction of the inequality symbol for each operation.

Find the solutions for the following systems of equations by graphing on graph paper.

- **251.** y = x + 4y = -x + 4
- **252.** 2y x = 23x + y = 8
- **253.** $4y = {}^{-7}(x + 4)$ 4y = x + 4 **254.** y - x = 5 - x ${}^{-4}y = 8 - 7x$ **255.** 2y = 6x + 14 4y = x - 16 **256.** 2x + y = 43(y + 9) = 7x

257.	y = x + 9
050	4y = 16 - x
258.	4x - 5y = 5 5y = 20 - x
259.	$6y = 9(x - 6) 3(2y + 5x) = ^-6$
260.	15y = 6(3x + 15) y = 6(1 - x)
261.	3y = 6x + 6 5y = 10(x - 5)
262.	3(2x + 3y) = 63 27y = 9(x - 6)

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263. x - 20 = 5y 10y = 8x + 20 **264.** 3x + 4y = 12 $y = 3 - \frac{6}{8}x$ **265.** 16y = 10(x - 8)8y - 17x = 56

Find the solution for each of the following systems of inequalities by graphing and shading.

266. $2y - 3x \ge -6$ $y \ge 5 - \frac{5}{2}x$ **267.** 6y < 5x - 302y < x + 4**268.** $y - x \ge 6$ $11y \ge -2(x + 11)$ **269.** $5y \le 8(x + 5)$ $5y \le 12(5-x)$ **270.** 2(x + 5y) > 5(x + 6)4x + y < 4x + 5**271.** $3y \ge -2(x+3)$ $3y \le 2(6-x)$ **272.** 9(y-4) < 4x-9y < 2(x+9)**273.** 7(y-5) < 5x $-3 < \frac{1}{4}(2x-3y)$ **274.** $y > \frac{7}{4}(4-x)$ 3(y+5) > 7x**275.** $5x - 2(y + 10) \le 0$ $2x + y \leq -3$

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

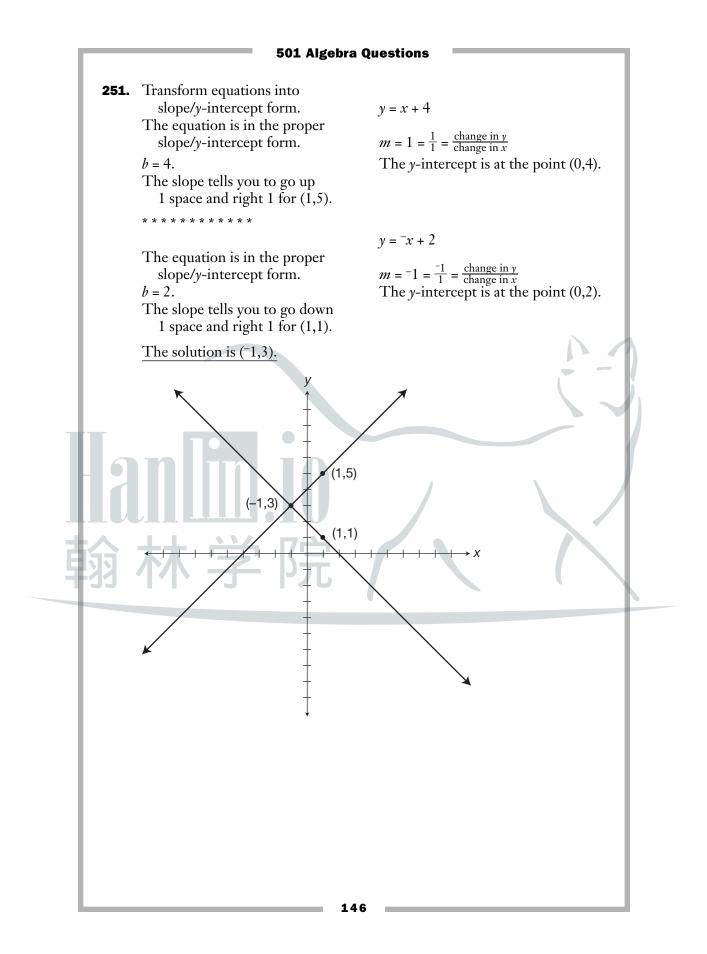
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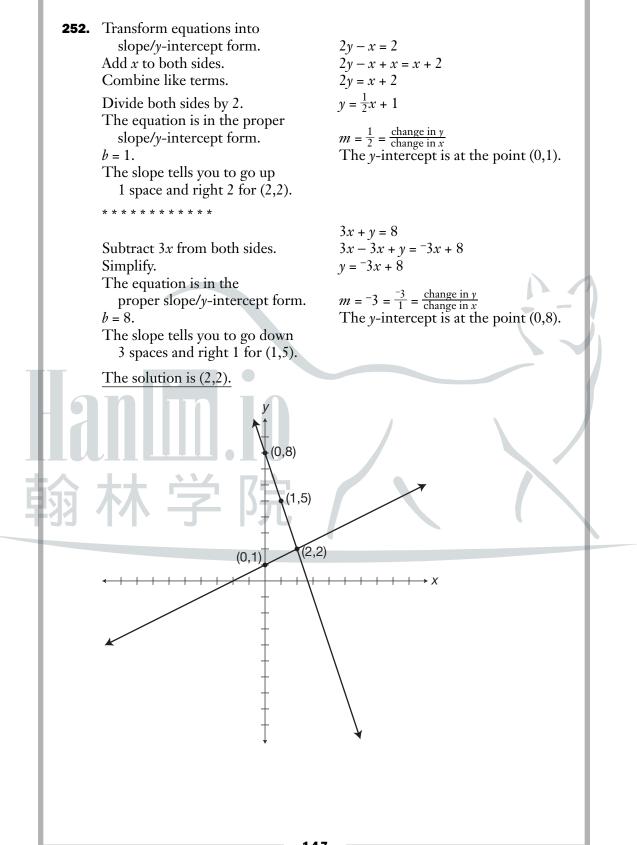
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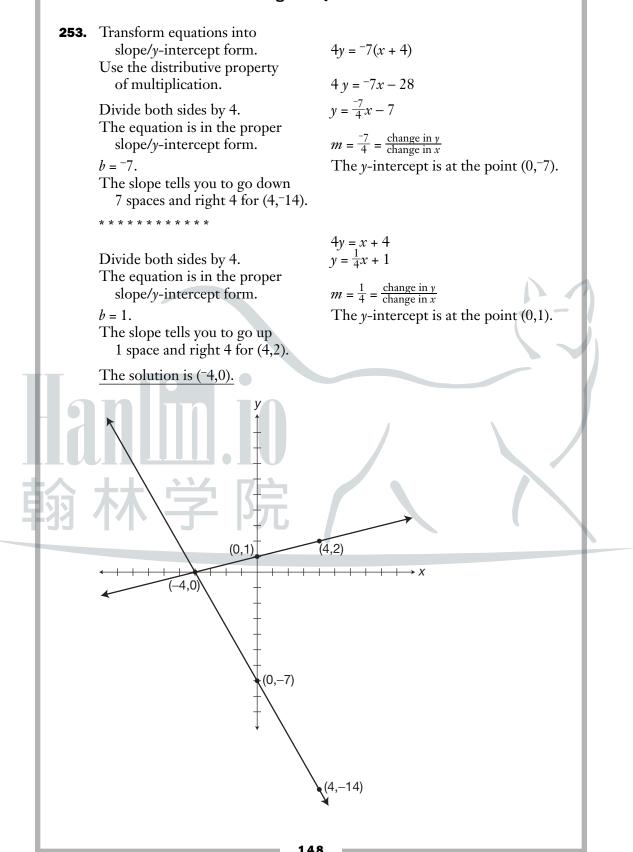
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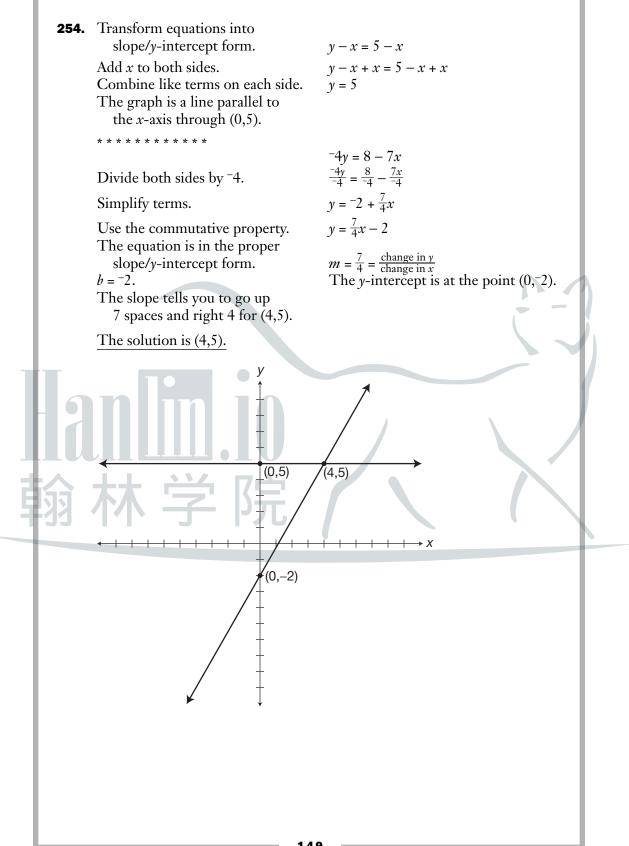
The <u>underlined</u> ordered pair is the solution. The graph is shown.

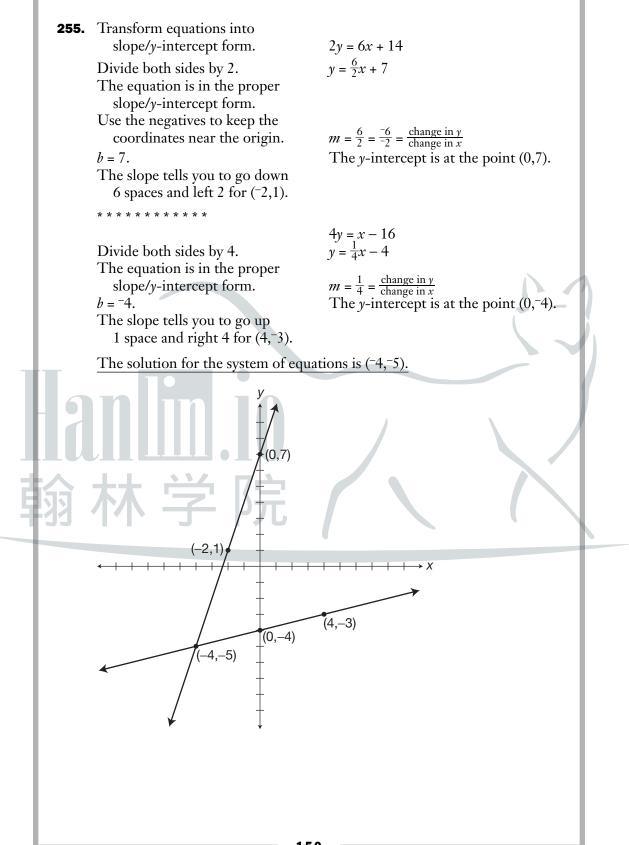
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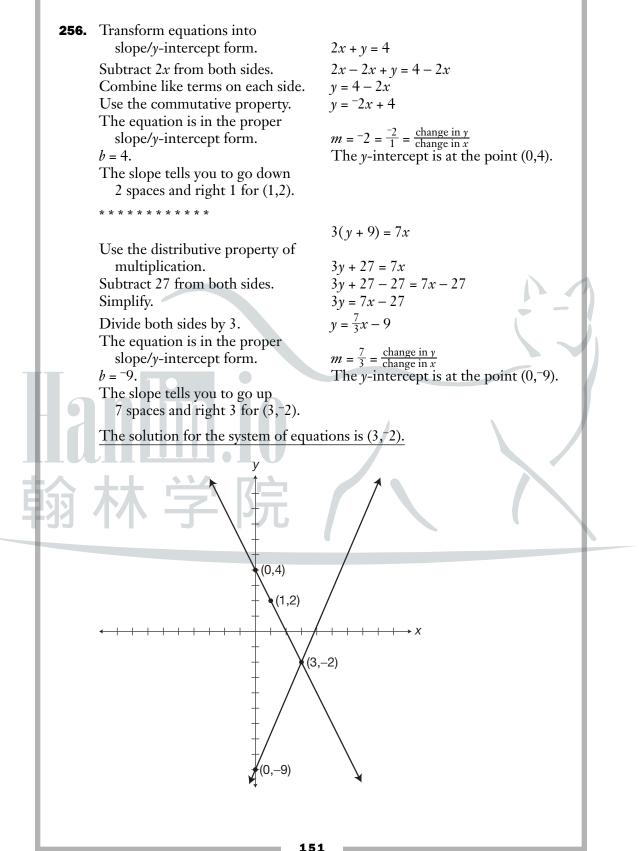


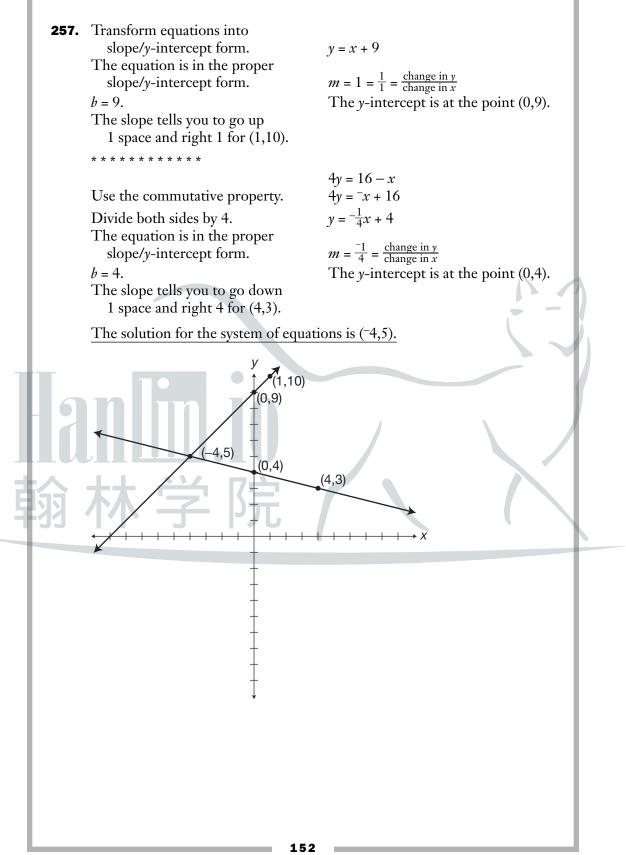


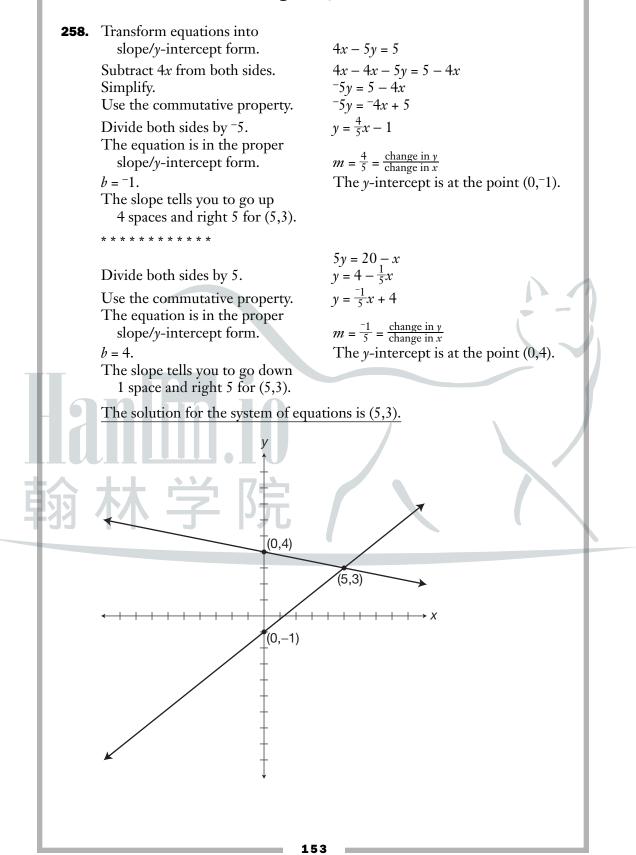


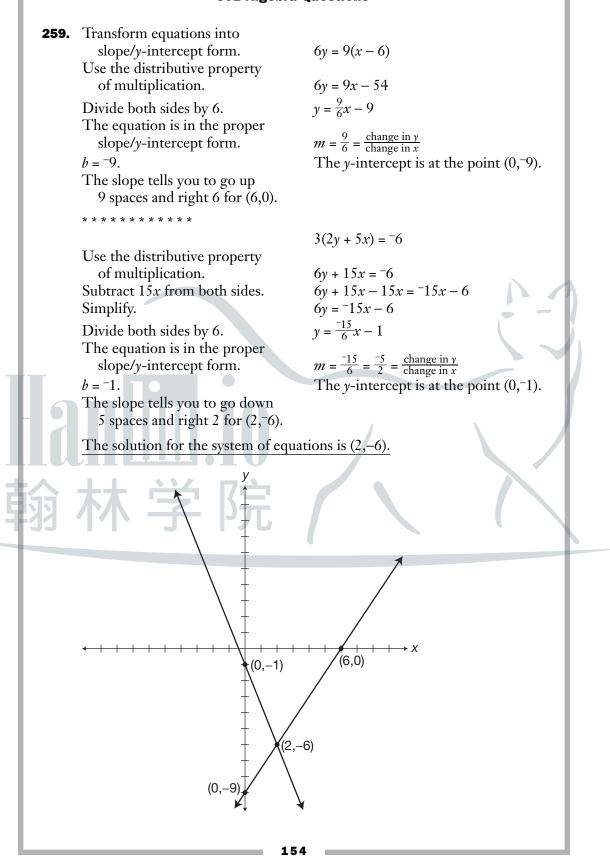


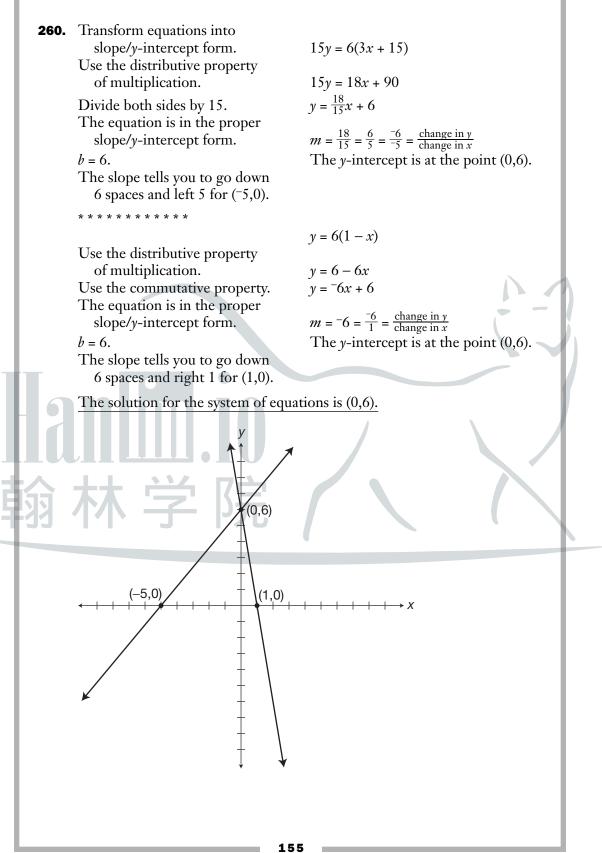
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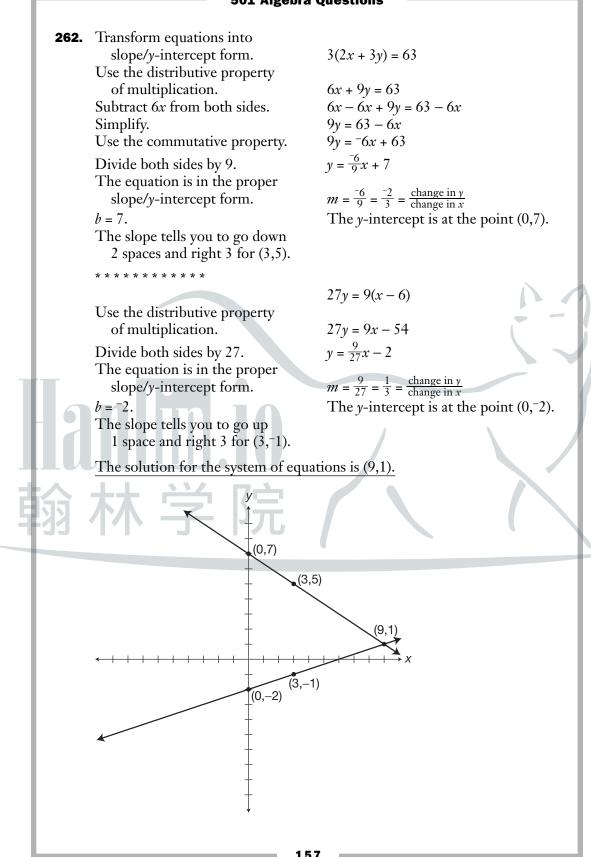


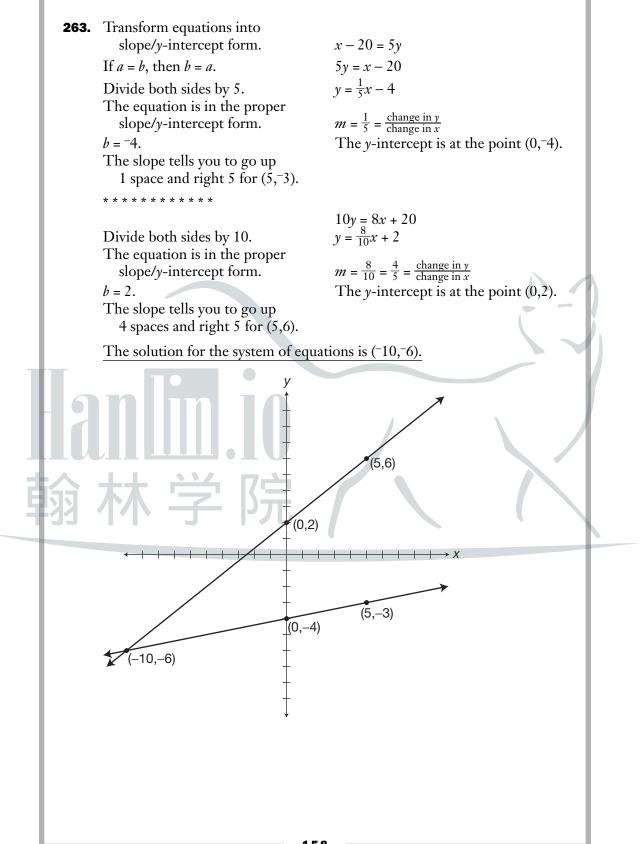


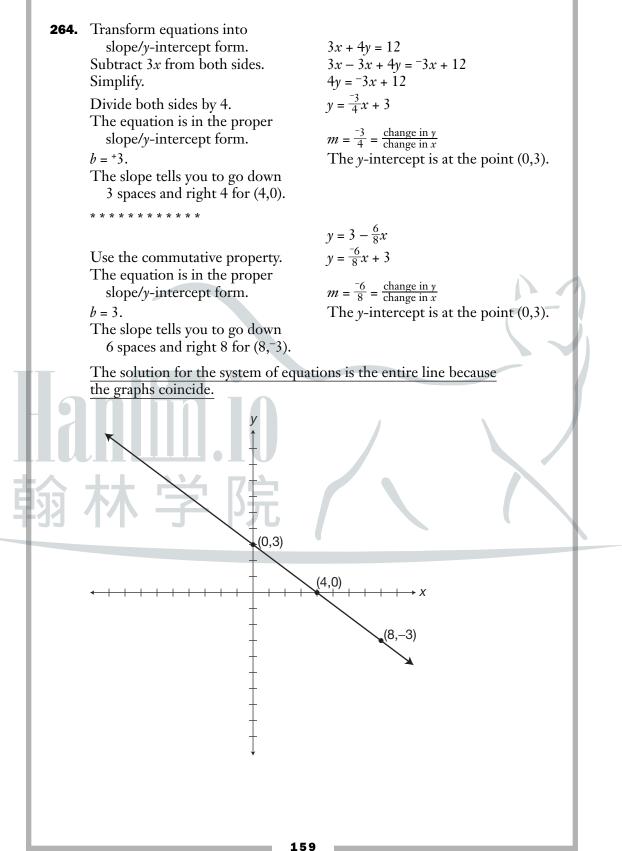




501 Algebra Questions 261. Transform equations into slope/y-intercept form. 3y = 6x + 6y = 2x + 2Divide both sides by 3. The equation is in the proper $m = 2 = \frac{2}{1} = \frac{\text{change in } y}{\text{change in } x}$ slope/y-intercept form. b = 2. The γ -intercept is at the point (0,2). The slope tells you to go up 2 spaces and right 1 for (1,4). * * * * * * * * * $5\gamma = 10(x-5)$ 5y = 10x - 50Use the distributive property. y = 2x - 10Divide both sides by 5. The equation is in the proper $m = 2 = \frac{2}{1} = \frac{\text{change in } y}{\text{change in } x}$ slope/y-intercept form. b = -10.The *y*-intercept is at the point (0, -10). The slope tells you to go up 2 spaces and right 1 for (1,-8). The slopes are the same, so the line graphs are parallel and do not intersect. (0,2)-8) -10) 156







265. Transform equations into slope/y-intercept form. Use the distributive property of multiplication. Divide both sides by 16. The equation is in the proper slope/y-intercept form. {Use the negatives to keep the coordinates near the origin.} b = -5. The slope tells you to go down 5 spaces and left 8 for (-8, -10). * * * * * * * * * * * * Subtract 17x from both sides. Simplify.

Divide both sides by 8.
The equation is in the proper slope/y-intercept form.
{Use the negatives to keep the coordinates near the origin.}
b = 7.

The slope tells you to go down 17 spaces and left 8 for (-8,-10).

16y = 10(x - 8) 16y = 10x - 80 $y = \frac{10}{16}x - 5$ $m = \frac{10}{16} = \frac{5}{8} = \frac{-5}{-8} = \frac{\text{change in } y}{\text{change in } x}$

The *y*-intercept is at the point (0,-5).

8y - 17x = 56 8y - 17x + 17 x = 17x + 56 8y = 17x + 56 $y = \frac{17}{8}x + 7$ $m = \frac{17}{8} = \frac{-17}{-8} = \frac{\text{change in } y}{\text{change in } x}$

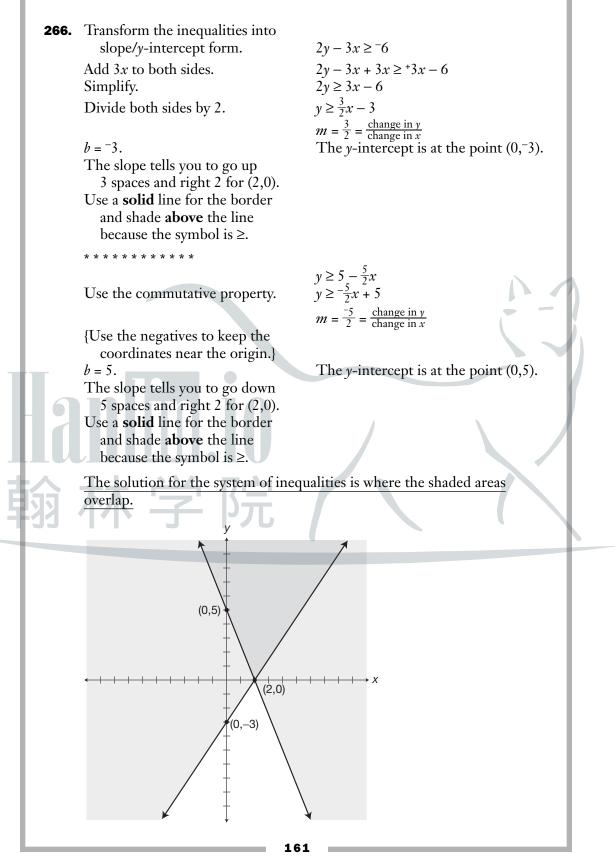
The γ -intercept is at the point (0,7).

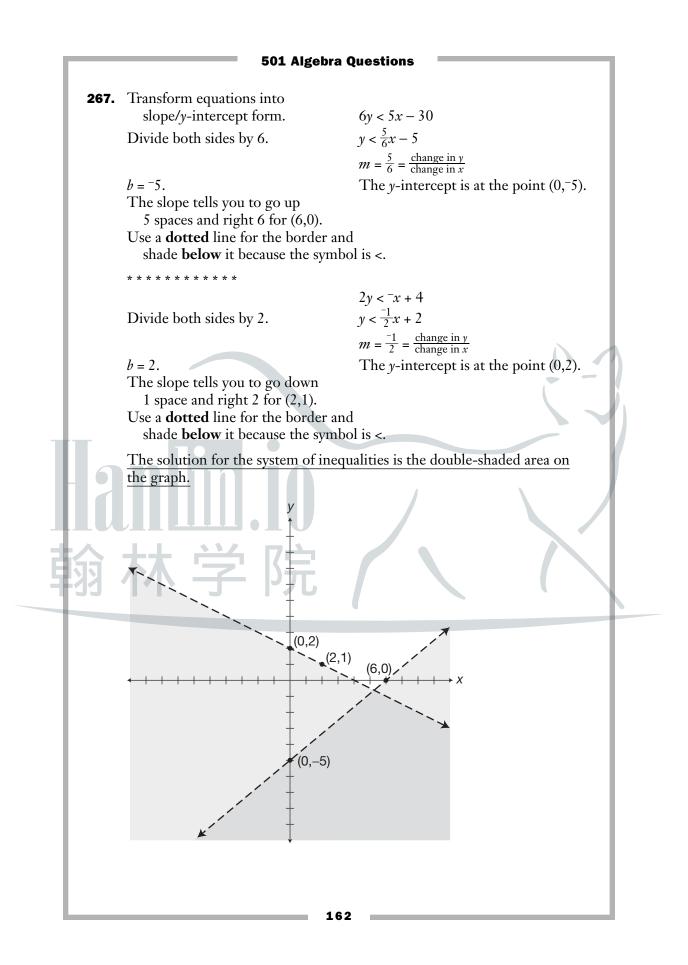
The solution for the system of equations is (-8, -10).

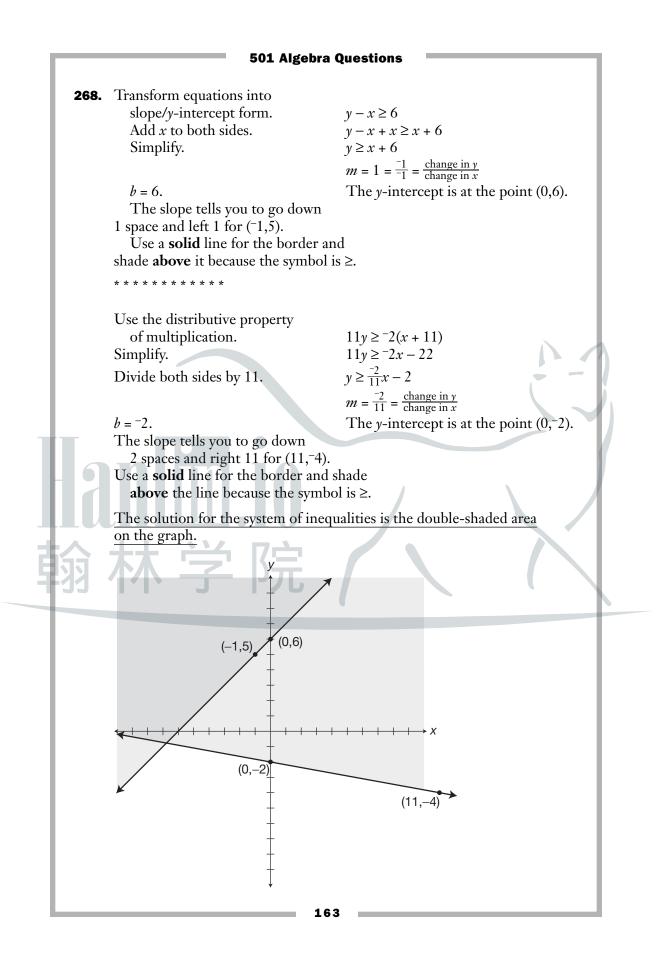
(0,7)

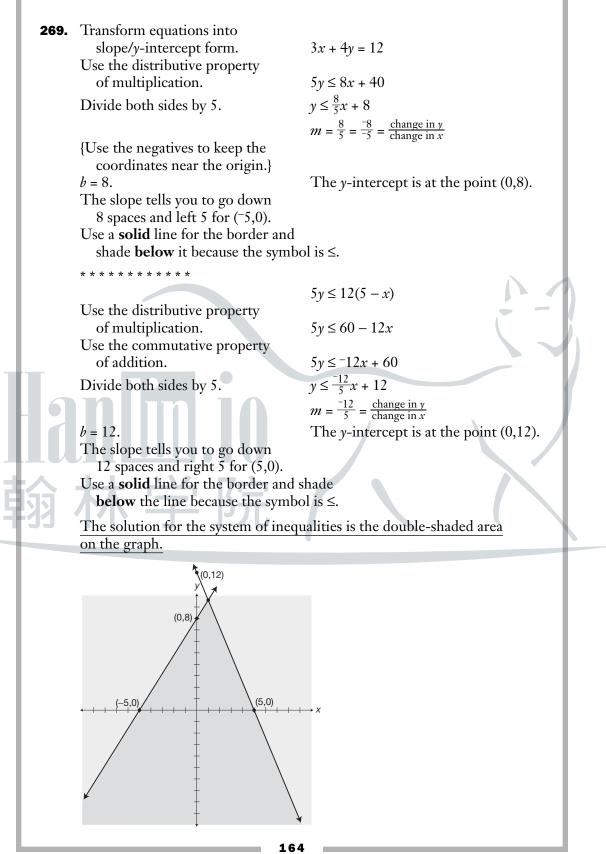
(0,-5)

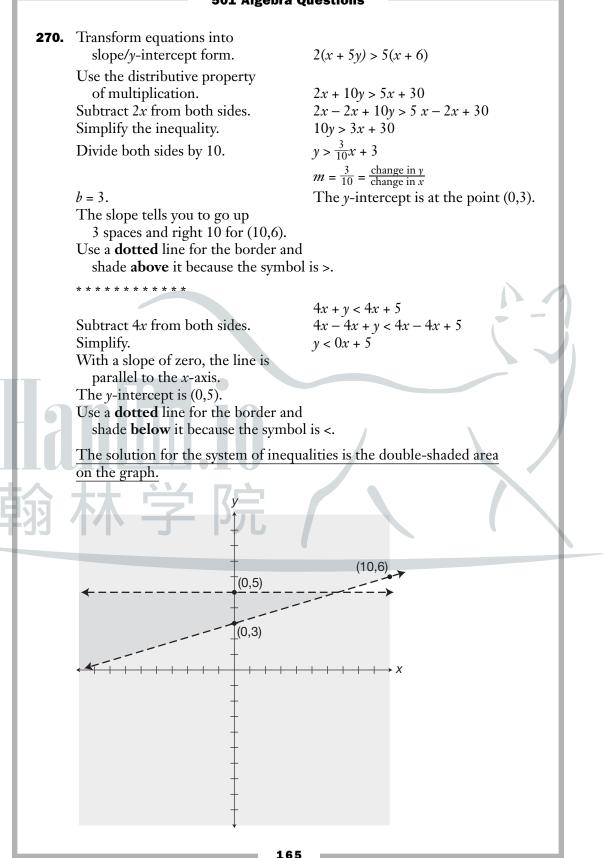
(-8,-10)

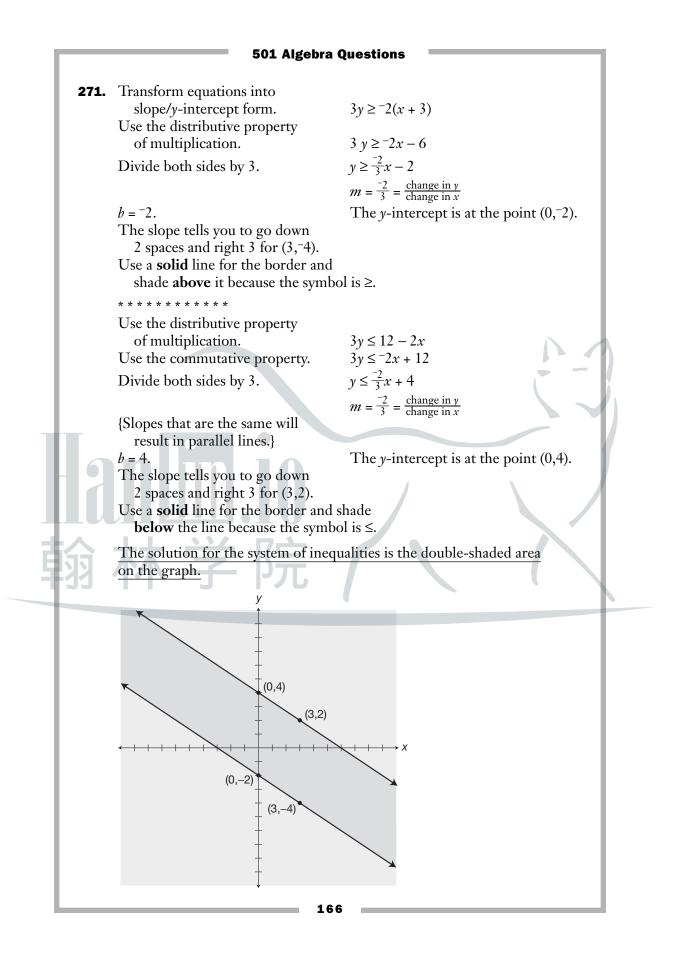












272. Transform equations into slope/y-intercept form. Use the distributive property of multiplication. Add 36 to both sides. Divide both sides by 9. b = 4. **272.** Transform equations into 9(y-4) < 4x 9y - 36 < 4x 9y - 36 < 4x + 36 $y < \frac{4}{9}x + 4$ $m = \frac{4}{9} = \frac{\text{change in } y}{\text{change in } x}$ The y-intercept is at the point (0,4).

The slope tells you to go up 4 spaces and right 9 for (9,8). Use a **dotted** line for the border and shade **below** it because the symbol is <.

Use the distributive property of multiplication. Divide both sides by ⁻⁹. Change the direction of the symbol when dividing by a negative.

* * * * * * * * *

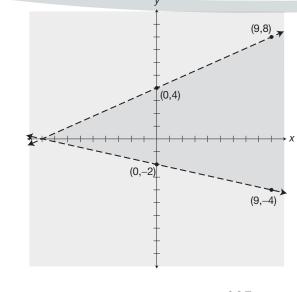
```
-9y < 2x + 18y > \frac{-2}{9}x - 2
```

-9y < 2(x+9)

 $m = \frac{-2}{9} = \frac{\text{change in } y}{\text{change in } x}$ The *y*-intercept is at the point (0,-2).

b = ⁻². The y The slope tells you to go down 2 spaces and right 9 for (9,⁻⁴).
Use a dotted line for the border and shade above the line because the symbol is >.

The solution for the system of inequalities is the double-shaded area on the graph.



273. Transform equations into slope/y-intercept form. Use the distributive property of multiplication. Add 35 to both sides. Simplify.

Divide both sides by 7.

 $7(y-5) < {}^-\!5x$

 $-3 < \frac{1}{4}(2x - 3y)$

7y - 35 < -5x7y - 35 + 35 < -5x + 35 $7\gamma < -5x + 35$ $\gamma < \frac{-5}{7}x + 5$ $m = \frac{-5}{7} = \frac{\text{change in } y}{\text{change in } x}$ The *y*-intercept is at the point (0,5).

b = 5. The
The slope tells you to go down
5 spaces and right 7 for (7,0).
Use a dotted line for the border and shade below it because the symbol is <.

Multiply both sides of the inequality by 4. Simplify the inequality.

* * * * * * * * * * * *

Add 3*y* to both sides. Simplify the inequality. Add 12 to both sides. Simplify the inequality. Divide both sides by 3.

b = 4.The slope tells you to go up

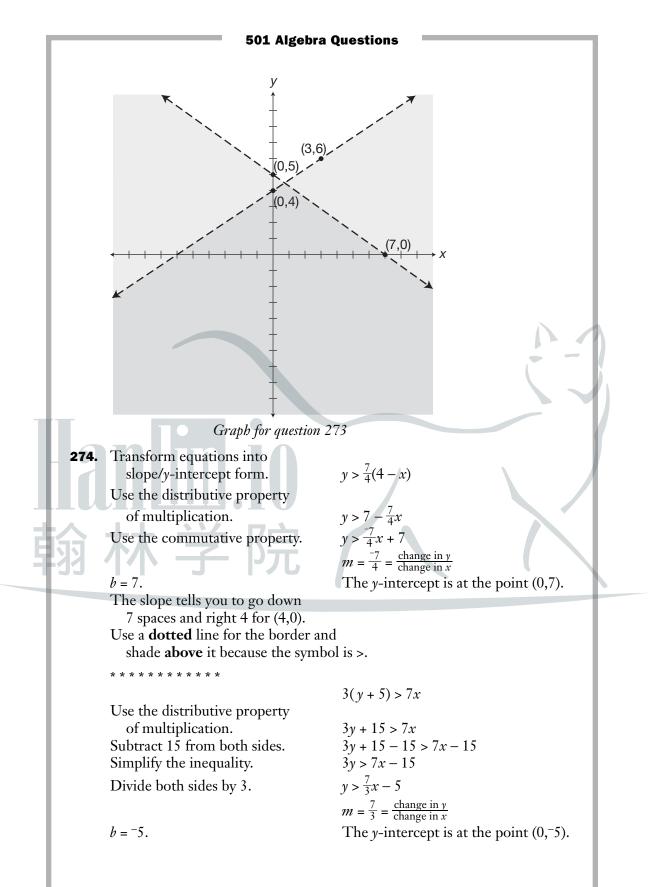
2 spaces and right 3 for (3,6).Use a **dotted** line for the border and shade **below** the line because

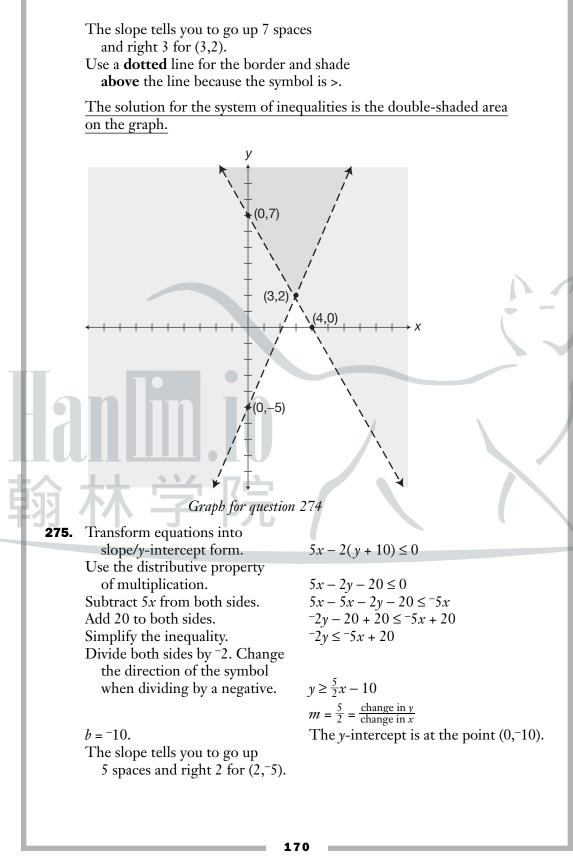
the symbol is <.

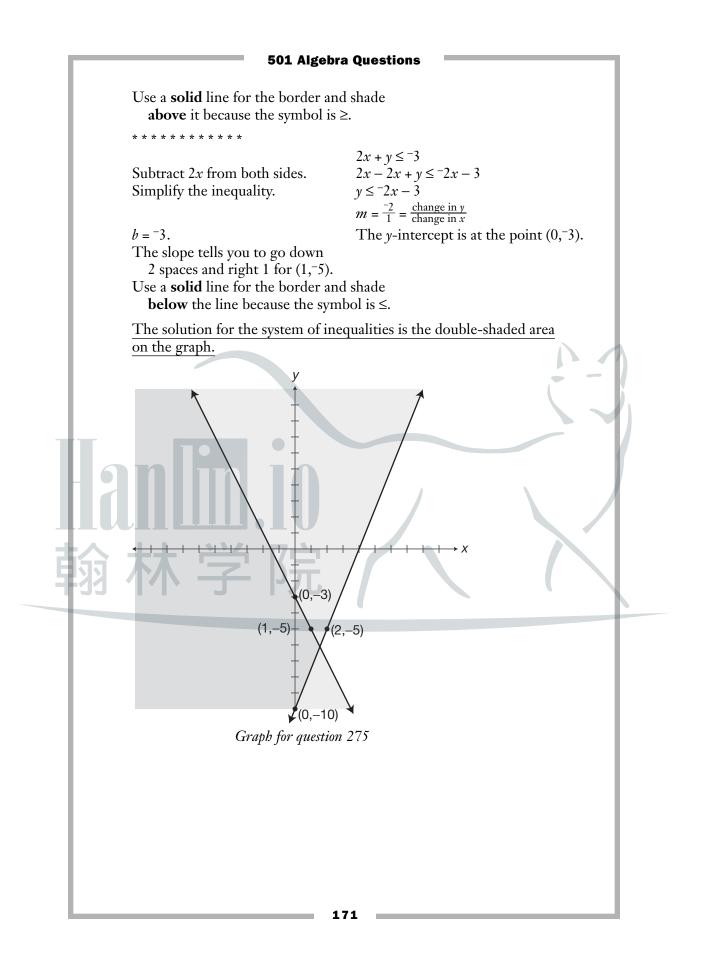
The solution for the system of inequalities is the double-shaded area on the graph (next page).

 $4(-3) < 4(\frac{1}{4})(2x - 3y)$ -12 < 1(2x - 3y)-12 < 2x - 3y-12 + 3y < 2x - 3y + 3y-12 + 3y < 2x-12 + 12 + 3y < 2x + 123y < 2x + 12 $\gamma < \frac{2}{3}x + 4$ $m = \frac{2}{3} = \frac{\text{change in } y}{\text{change in } x}$

The *y*-intercept is at the point (0,4).







Solving Systems of Equations Algebraically

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There is a faster way to solve systems of equations than graphing and finding the solution point. You can solve systems of equations using algebraic methods. The two methods you will practice here are called the **elimination method** and the **substitution method**. You will be using the skills you have practiced in the chapters on working with algebraic expressions, combining like terms, and solving equations.

In the **elimination method**, you will transform one or both of the two equations in the system so that when you add the two equations together, one of the variables will be eliminated. Then you solve the remaining equation for the remaining variable. When you find a numerical value for the remaining variable, you just substitute the found value into one of the equations and solve for the other variable.

In the **substitution method**, you will transform one of the equations so that one variable is expressed in terms of the other. Then you will eliminate the variable by substituting into the other equation and solve. When you find a numerical value for one variable, use it in one of the two equations to determine the value of the remaining variable.

One method is not better than the other. But you may find that you will begin to see which equations, because of their structure, lend themselves to one method over the other. Practice will help you decide.

Tips for Solving Systems of Equations Algebraically

When using the elimination method, first make a plan to determine which variable you will eliminate from the system. Then transform the equation or equations so that you will get the result you want.

Express your solution as a coordinate point or in the form (x,y), or as variables such as x = 2 and y = 4.

Use the elimination method to solve the following systems of equations.

276.	x + y = 4 2x - y = -1	
277.	3x + 4y = 17 x + 2y = 1	
278.	7x + 3y = 11 $2x + y = 3$	
279.	0.5x + 5y = 28 3x - y = 13	
281.	$3(x + y) = 185x + y = -2\frac{1}{2}x + 2y = 112x - y = 17$	
TTT	5x + 8y = 25 3x - 15 = y 6y + 3x = 30 2y + 6x = 0	
284.	3x = 5 - 7y 2y = x - 6	
285.	$3x + y = 20$ $\frac{x}{3} + 10 = y$	
286.	2x + 7y = 45 $3x + 4y = 22$	
287.	3x - 5y = -21 2(2y - x) = 16	
288.	$\frac{1}{4}x + y = 12$ 2x - $\frac{1}{3}y = 21$	

Use the substitution method to solve the following systems of equations.

```
289. y = 5x
       4x + 5y = 87
290. x + y = 3
       3x + 101 = 7y
291. 5x + y = 3.6
      y + 21x = 8.4
292. 8x - y = 0
       10x + y = 27
293. \frac{x}{3} = y + 2
       2x - 4y = 32
294. y + 3x = 0
      y - 3x = 24
295. 5x + y = 20
       3x = \frac{1}{2}y + 1
296. 2x + y = 2 - 5y
       x - y = 5
297. \frac{2x}{10} + \frac{y}{5} = 1
       3x + 2y = 12
298. x + 6y = 11
x - 3 = 2y
299. 4y + 31 = 3x
      y + 10 = 3x
300. 2(2-x) = 3y - 2
       3x + 9 = 4(5 - y)
```

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

The <u>underlined</u> ordered pair is the solution. Be aware that you may have used a different method of elimination to arrive at the correct answer.

276. Add the equations.

3.	Add the equations.	x + y = 4 —
		2x - y = -1
		$\overline{3x+0} = 3$
	Additive identity.	3x = 3
	Now solve for <i>x</i> .	
_	Divide both sides by 3.	$\frac{3x}{3} = \frac{3}{3}$
	Simplify terms.	x = 1
	Substitute the value of x into one of the equations	
	in the system and solve for <i>y</i> .	(1) + y = 4
	Subtract 1 from both sides.	1 - 1 + y = 4 - 1
	Simplify.	y = 3
	The solution for the system of equations is $(1,3)$.	5
7.	We could add the equations together if we had	
	a $-3x$ in the second equation.	
	Multiply the second equation by 3.	3(x + 2y = 1)
	Simplify.	-3x + 6y = 3
	Add the first and transformed second equations.	3x + 4y = 17
	1	$\overline{0 + 10y} = 20$
	Identity element of addition.	10y = 20
	Divide both sides by 4.	y = 2
	Substitute the value of <i>y</i> into one of the equations	5
	in the system and solve for <i>x</i> .	x + 2(2) = 1
	Simplify.	x + 2(2) = 1
	Subtract 4 from both sides.	x + 4 - 4 = 1 - 4
	Simplify.	x = -3
	Multiply both sides by ⁻ 1.	x = 3

278.	Transform the second equation so you can add it to the first and eliminate <i>y</i> . Multiply the equation by ⁻ 3. Simplify.	-3(2x + y = 3) -6x - 3y = -9
	Add the first equation to the transformed second.	$\frac{-6x - 3y = -9}{7x + 3y = 11}$ $\frac{7x + 0 = 2}{x = 2}$
	Substitute the value of <i>x</i> into one of the equations in the system and solve for <i>y</i> .	2(2) + y = 3 4 + y = 3
	Subtract 4 from both sides. Simplify.	4-4+y=3-4 y=-1
279.	The solution for the system of equations is (2,-1). If you multiply the second equation by 5	A .
	and add the equations together, you can eliminate the <i>y</i> .	5(3x - y) = 5(13)
	Distributive property of multiplication. Simplify terms. Add the first and second equations.	5(3x) - 5(y) = 5(13) 15x - 5y = 65 0.5x + 5y = 28
	Additive identity. Divide both sides by 15.5.	$ \frac{15.5x + 0 = 93}{15.5x = 93} \\ x = 6 $
	Substitute the value of x into one of the equations in the system and solve for y.	3(6) - y = 13
-33	Simplify. Subtract 18 from both sides. Simplify.	18 - y = 13 18 - 18 - y = 13 - 18 -y = -5
	Multiply both sides by ⁻ 1. Simplify. The solution for the system of equations is (6,5).	$(^{-1})(^{-}y) = (^{-1})(^{-5})$ y = 5
280.	See what the first equation looks like after	
	distributing the multiplication on the left. Use the distributive property of multiplication. Multiply the second equation by ⁻ 3 and add	3x + 3y = 18
	equations to eliminate <i>y</i> . Use the distributive property of multiplication. Simplify terms.	$\begin{array}{l} -3(5x + y) = -3(-2) \\ -3(5x) - 3(y) = -3(-2) \\ -15x - 3y = 6 \end{array}$
	Add the transformed first equation.	$\frac{3x + 3y = 18}{-12x + 0 = 24}$
	Additive identity. Divide both sides by ⁻ 12.	$^{-1}2x = 24$ $x = ^{-2}$

281.	 Substitute the value of x into one of the equations in the system and solve for y. Add 10 to both sides. Simplify. The solution for the system of equations is (-2,8). Multiply the second equation by 2 and add to the first to eliminate y. Use the distributive property of multiplication. Simplify. Add the first equation to the second. Additive identity. 	5(-2) + y = -2 -10 + y = -2 10 - 10 + y = 10 - 2 y = 8 2(2x - y) = 2(17) 2(2x) - 2(y) = 2(17) 4x - 2y = 34 $\frac{1}{2}x + 2y = 11$ $4\frac{1}{2}x + 0 = 45$
	the first to eliminate <i>y</i> . Use the distributive property of multiplication. Simplify. Add the first equation to the second.	2(2x) - 2(y) = 2(17) 4x - 2y = 34 $\frac{1}{2}x + 2y = 11$ $4\frac{1}{2}x + 0 = 45$
	Additive identity.	
282.	Multiply the equation by 2 to simplify the fraction. Simplify. Divide both sides by 9. Substitute the value of x into one of the equations in the system and solve for y . Subtract 20 from both sides. Combine like terms on each side. Multiply the equation by $\neg 1$. The solution for the system of equations is (10,3). Transform the second equation into a similar format to the first equation, then line up like terms. Add 15 to both sides. Simplify. Subtract y from both sides. Simplify. Multiply the second equation by 8 and add the first equation to the second. Use the distributive property of multiplication. Add the first equation to the second. Use the distributive property of multiplication. Add the first equation to the second. Substitute the value of x into one of the equations in the system and solve for y . Simplify. The solution for the system of equations is (5,0).	$4\frac{1}{2}x = 45$ $2(4\frac{1}{2}x = 45)$ 9x = 90 x = 10 2(10) - y = 17 20 - 20 - y = 17 - 20 7y = -3 y = 3 3x - 15 + 15 = y + 15 3x - y = y - y + 15 3x - y = y - y + 15 3x - y = y - y + 15 8(3x - y) = 15 8(3x - y) = 15 24x - 8y = 120 5x + 8y = 25 29x + 0 = 145 x = 5 3(5) - 15 = y 15 - 15 = y 0 = y
	The solution for the gratem of equations is (5.0)	

283. Multiply the second equation by -3 and add it to the first equation to eliminate y. $-3(2y + 6x = 0)$ $-6y - 18x = 0$ $0 - 15x = 30$ Additive identity. Divide both sides by -15 . Substitute the value of x into one of the equations in the system and solve for y. $2y + 6(-2) = 0$ $2y - 12 = 0$ $2y - 12 = 0$ $2y - 12 = 0$ $2y - 12 + 12 = 0 + 12$ $2y = 12$ $y = 6$ 284. Transform the first equation into familiar form $(ax + by = c)$. Add 7y to both sides. Simplify. $3x = 5 - 7y$ $3x + 7y = 5$ 284. Transform the second equation into familiar form $(ax + by = c)$. Subtract x from both sides. Simplify. $2y = -6$ $x + 2y = x - x - 6$ $x + 2y = -6$ $3(x + 3 (2y) = 3(-6))$ $3(x + 3 (2y) = 3(-6))$ $3(x + 3 (2y) = 3(-6))$ $3(x + 3 (2y) = -13)$ y = -1Add the transformed first equation. $3x + 7y = 5$ $-3x + 6y = -18$ Add the transformed first equation.Additive identity. Divide both sides by 13. Substitute the value of y into one of the equations in the system and solve for x. $3x = 5 - 7(-1)$ $3x = 5 + 7$ $3x = 12$ $x = 4$	to the first equation to eliminate y. The solution for the system and solve for y. Add 12 to both sides. Simplify. Transform the first equation into familiar form $(ax + by = c)$. Subtract x from both sides. Simplify. Transform the second equation into familiar form $(ax + by = c)$. Subtract x from both sides. Simplify. Transform the second equation. Add the transformed first equation. Add the transf		501 Algebra Questions	
Additive identity. Divide both sides by $^{-15}$. $x = ^{-2}$ Substitute the value of x into one of the equations in the system and solve for y. $2y + 6(^{-2}) = 0$ $2y - 12 = 0$ $2y - 12 = 0$ $2y - 12 + 12 = 0 + 12$ $2y = 12$ $y = 6$ Add 12 to both sides. $2y - 12 + 12 = 0 + 12$ $2y = 12$ $y = 6$ Divide both sides by 2. $y = 6$ The solution for the system of equations is ($^{-2}$,6). 284. Transform the first equation into familiar form $(ax + by = c)$.familiar form $(ax + by = c)$.Simplify.Transform the second equation into familiar form $(ax + by = c)$.Subtract x from both sides.Simplify.Multiply equation by 3.Add the transformed first equation.Add the transformed first equation.Additive identity. Divide both sides by 13.Substitute the value of y into one of the equations in the system and solve for x. $y = -1$ Divide both sides by 3.	Additive identity. Divide both sides by $^{-15}$. $x = ^2$ Substitute the value of x into one of the equations in the system and solve for y. $2y + 6(^2) = 0$ $2y - 12 = 0$ $2y - 12 = 0$ $2y - 12 + 12 = 0 + 12$ $2y = 12$ $y = 6$ Add 12 to both sides. $2y - 12 + 12 = 0 + 12$ $2y = 12$ $y = 6$ Divide both sides by 2. $y = 6$ The solution for the system of equations is ($^{-2}$,6). 284. Transform the first equation into familiar form $(ax + by = c)$. $3x = 5 - 7y$ $3x + 7y = 5 - 7y + 7y$ $3x + 7y = 5$ Transform the second equation into familiar form $(ax + by = c)$. $3x = 5 - 7y + 7y$ $3x + 7y = 5$ Subtract x from both sides. $3x - 7y = 5$ $x + 2y = x - x - 6$ $x + 2y = x - x - 6$ $3(x) + 3 (2y) = 3(^{-6})$ Simplify. $3(x + 7y = 5)$ $0 + 13y = ^{-1}3$ $y = ^{-1}$ Additive identity. Divide both sides by 13. Substitute the value of y into one of the equations in the system and solve for x. $3x = 5 - 7(^{-1})$ $3x = 5 + 7$ $3x = 12$ Divide both sides by 3.	283.		-6y - 18x = 0 -6y + 3x = 30
The solution for the system of equations is (-2,6). 284. Transform the first equation into familiar form $(ax + by = c)$. Add 7y to both sides. Simplify. $3x = 5 - 7y$ $3x + 7y = 5 - 7y + 7y$ $3x + 7y = 5$ Transform the second equation into familiar form $(ax + by = c)$. Subtract x from both sides. Simplify. $3x = 5 - 7y$ $3x + 7y = 5$ Nultiply equation by 3. $2y = x - 6$ $x + 2y = x - x - 6$ $3(x + 2y = -6)$ $3(x) + 3 (2y) = 3(-6)$ $-3x + 6y = -18$ Add the transformed first equation. $3x + 7y = 5$ $0 + 13y = -13$ $y = -1$ Additive identity. Divide both sides by 13. Substitute the value of y into one of the equations in the system and solve for x. $3x = 5 - 7(-1)$ $3x = 5 + 7$ $3x = 12$ $x = 4$	The solution for the system of equations is (-2,6). 284. Transform the first equation into familiar form $(ax + by = c)$. Add 7y to both sides. Simplify. $3x = 5 - 7y$ $3x + 7y = 5 - 7y + 7y$ $3x + 7y = 5$ Transform the second equation into familiar form $(ax + by = c)$. Subtract x from both sides. Simplify. Multiply equation by 3. $3x = 5 - 7y$ $3x + 7y = 5$ Simplify. Multiply equation by 3. $2y = x - 6$ $x + 2y = x - x - 6$ 		Substitute the value of x into one of the equations in the system and solve for y.Add 12 to both sides.Simplify.	x = -2 2y + 6(-2) = 0 2y - 12 = 0 2y - 12 + 12 = 0 + 12 2y = 12
284. Transform the first equation into familiar form $(ax + by = c)$. $3x = 5 - 7y$ $3x + 7y = 5 - 7y + 7y$ $3x + 7y = 5$ Add 7y to both sides. Simplify. $3x + 7y = 5 - 7y + 7y$ $3x + 7y = 5$ Transform the second equation into familiar form $(ax + by = c)$. Subtract x from both sides. Simplify. Multiply equation by 3. $2y = x - 6$ $x + 2y = x - x - 6$ $3(-x + 2y = -6)$ $3(-x) + 3 (2y) = 3(-6)$ 	284. Transform the first equation into familiar form $(ax + by = c)$. $3x = 5 - 7y$ $3x + 7y = 5 - 7y + 7y$ $3x + 7y = 5$ Add 7y to both sides. Simplify. Transform the second equation into familiar form $(ax + by = c)$. Subtract x from both sides. Simplify. Multiply equation by 3. $3x = 5 - 7y$ $3x + 7y = 5$ Simplify. Multiply equation by 3. $2y = x - 6$ $x + 2y = x - x - 6$ $3(-x + 2y = -6)$ $3(-x) + 3 (2y) = 3(-6)$ $-3x + 6y = -18$ Add the transformed first equation. $3x = 7y = 5$ $0 + 13y = -13$ $y = -1$ Additive identity. Divide both sides by 13. Substitute the value of y into one of the equations in the system and solve for x. $3x = 5 - 7(-1)$ $3x = 5 + 7$ $3x = 12$ $x = 4$		•	y = 6
Additive identity. Divide both sides by 13. Substitute the value of y into one of the equations in the system and solve for x. $\overline{0 + 13y} = -13$ $y = -1$ $3x = 5 - 7(-1)$ $3x = 5 + 7$ $3x = 12$ Divide both sides by 3. $x = 4$	Additive identity. Divide both sides by 13. Substitute the value of y into one of the equations in the system and solve for x. $\overline{0 + 13y = -13}$ $y = -1$ Divide both sides by 3. $\overline{0 + 13y = -13}$ $y = -1$	284.	 Transform the first equation into familiar form (ax + by = c). Add 7y to both sides. Simplify. Transform the second equation into familiar form (ax + by = c). Subtract x from both sides. Simplify. Multiply equation by 3. Simplify terms. 	3x + 7y = 5 - 7y + 7y 3x + 7y = 5 2y = x - 6 x + 2y = x - x - 6 $x + 2y = ^{-6}$ $3(^{-}x + 2y = ^{-6})$ $3(^{-}x) + 3(2y) = 3(^{-6})$ $^{-3}x + 6y = ^{-1}8$
Divide both sides by 3. $3x = 12$ x = 4	Divide both sides by 3. $3x = 12$ x = 4	的	Additive identity. Divide both sides by 13. Substitute the value of y into one of the	$\overline{0 + 13y} = \overline{13}$ $y = \overline{1}$
				3x = 12

285.	Transform the second equation into familiar form $(ax + by = c)$.	
	Multiply the equation by 3.	$3(\frac{x}{3} + 10 = y)$
	Use the distributive property.	$3(\frac{x}{3}) + 3(10) = 3(y)$
	Simplify terms.	x + 30 = 3y
	Subtract 30 from each side.	x + 30 - 30 = 3y - 30
	Simplify.	x = 3y - 30
	Subtract 3 <i>y</i> from both sides.	x - 3y = 3y - 3y - 30
	Simplify.	x - 3y = -30
	Multiply the first equation by 3 and add to the	
	second equation to eliminate <i>y</i> .	3(3x + y = 20)
	Use the distributive property.	3(3x) + 3(y) = 3(20)
	Simplify terms.	9x + 3y = 60
	Add the transformed second equation to the first.	x - 3y = -30
		10x + 0 = 30
	Additive identity. Divide both sides by 10.	<i>x</i> = 3
	Substitute the value of <i>x</i> into one of the equations	(3)
	in the system and solve for <i>y</i> .	$\frac{(3)}{3} + 10 = y$
	Simplify terms.	1 + 10 = y
	The solution for the system of equations is $(3,11)$.	11 = y
286.	Transform the first equation by multiplying by 3, the second by multiplying by ⁻ 2, and eliminate the <i>x</i> variable by adding the	
	equations together.	3(2x + 7y = 45)
	Use the distributive property.	3(2x) + 3(7y) = 3(45)
	Simplify terms.	6x + 21y = 135
	Second equation.	-2(3x + 4y = 22)
	Use the distributive property.	-2(3x) - 2(4y) = -2(22)
	Simplify terms.	-6x - 8y = -44
	Add the transformed first equation to the	
	second equation.	6x + 21y = 135
		0 + 13y = 91
	Additive identity. Divide both sides by 13.	y = 7
	Substitute the value of <i>y</i> into one of the	
	equations in the system and solve for <i>x</i> .	3x + 4(7) = 22
	Simplify terms.	3x + 28 = 22
	Subtract 28 from both sides.	3x + 28 - 28 = 22 - 28
	Simplify.	3x = -6
	Divide both sides by 3.	x = -2
	The solution for the system of equations is $(-2,7)$.	n = 2

287.	Transform the second equation into a	
	similar form to the first equation. Use the distributive property of multiplication.	2(2y) - 2(x) = 16
	Simplify terms. Commutative property of addition. Multiply the first equation by 2 and the second equation by 3, and add the transformed equations to eliminate	4y - 2x = 16 -2x + 4y = 16
	the variable <i>x</i> . Distributive property. Simplify terms.	2(3x - 5y = -21) 6x - 10y = -42
	Distributive property. Simplify terms. Add the first equation to the second.	3(-2x + 4y = 16)-6x + 12y = 486x - 10y = -42
	Divide both sides by 2. Substitute the value of y into one of the	$\overline{2y = 6}$ $y = 3$
	equations in the system and solve for x . Simplify terms and add 15 to each side. Combine like terms on each side. Divide both sides by 3. The solution for the system of equations is (-2,3).	3x - 5(3) = -21 3x - 15 + 15 = -21 + 15 3x = -6 x = -2
288.	Transform the second equation by multiplying it b Then, add the equations together to eliminate <i>y</i> . Use the distributive property of multiplication. Simplify terms. Add the first equation to the second.	y 3. $3(2x - \frac{1}{3}y = 21)$ $3(2x) - 3(\frac{1}{3}y) = 3(21)$ $6x - y = 63$ $\frac{\frac{1}{4}x + y = 12}{6\frac{1}{4}x + 0 = 75}$
	Additive identity.	$6\frac{1}{4}x = 75$
	Divide both sides by $6\frac{1}{4}$. Simplify.	$\frac{\frac{6^{1}_{4}x}{6^{1}_{4}}}{x} = \frac{75}{6^{1}_{4}}$ $x = 12$
	Substitute the value of x into one of the equations in the system and solve for y.Simplify the first term and subtract from both side Simplify.The solution for the system of equations is (12,9).	s. $\frac{1}{4}(12) + y = 12$ 3 - 3 + y = 12 - 3 y = 9

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289.	 The first equation tells you that y = 5x. Substitute 5x for y in the second equation and then solve for x. Simplify term and add like terms. Divide both sides by 29. Substitute 3 for x in one of the equations. The solution for the system of equations is (3,15) 	$4x + 5(5x) = 87 4x + 25x = 87 29x = 87 x = \frac{87}{29} = 3 y = 5 \cdot (3) = 15$
290.	 Transform the first equation so that the value of is expressed in terms of <i>y</i>. Subtract <i>y</i> from both sides of the equation. Simplify. Substitute 3 - <i>y</i> for <i>x</i> in the second equation 	x $x + y - y = 3 - y$ $x = 3 - y$
Ia	 and solve for y. Use the distributive property of multiplication. Use the commutative property of addition. Add like terms. Add 3y to both sides. Combine like terms. Divide both sides by 10. Substitute the value of y into one of the equation in the system and solve for x. 	3(3 - y) + 101 = 7y 9 - 3y + 101 = 7y 9 + 101 - 3y = 7y 110 - 3y + 3y = 7y + 3y 110 = 10y 11 = y x + (11) = 3
291.	Subtract 11 from both sides. Combine like terms on each side. The solution for the system of equations is (~8,1) Transform the first equation so that y is	
	 Substitute the value of <i>y</i> into the second equation. Combine like terms. Subtract 3.6 from both sides. Combine like terms on each side. Divide both sides by 16. Substitute the value of <i>x</i> into one of the equations in the system and solve for <i>y</i>. Simplify terms. Subtract 1.5 from both sides. 	5x + y = 3.6 5x - 5x + y = 3.6 - 5x y = 3.6 - 5x (3.6 - 5x) + 21x = 8.4 3.6 + 16x = 8.4 3.6 - 3.6 + 16x = 8.4 - 3.6 16x = 4.8 x = 0.3 5(0.3) + y = 3.6 1.5 + y = 3.6 1.5 - 1.5 + y = 3.6 - 1.5 y = 2.1 2.1).

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292.	Transform the first equation so that y is expressed in terms of x . Add y to both sides of the equation. Combine like terms on each side and simplify. Substitute the value of y into the second equation. Combine like terms. Divide both sides by 18. Substitute the value of x into one of the equations in the system and solve for y . Simplify terms. Add y to both sides of the equation. Simplify. The solution for the system of equations is $(\frac{3}{2}, 12)$.	$8x - y = 08x + y - y = y + 08x = y10x + 8x = 2718x = 27x = \frac{3}{2}8(\frac{3}{2}) - y = 012 - y = 012 - y + y = 0 + y12 = y$
293. Ig	 Transform the first equation so that the value of x is expressed in terms of y. Multiply the equation by 3. Use the distributive property. Simplify. Substitute the value of x into the second equation in the system and solve for y. Use the distributive property of multiplication. Use the commutative property of addition. Combine like terms. Subtract 12 from both sides. Combine like terms on each side. Divide both sides by 2. Substitute the value of y into one of the equations in the system and solve for x. Simplify and add 40 to both sides. Combine like terms. Divide both sides by 2. The solution for the system of equations is (36,10). 	$3\left(\left(\frac{x}{3}\right) = y + 2\right)$ $3\left(\frac{x}{3}\right) = 3y + 6$ x = 3y + 6 2(3y + 6) - 4y = 32 6y + 12 - 4y = 32 6y - 4y + 12 = 32 2y + 12 - 12 = 32 - 12 2y = 20 y = 10 2x - 4(10) = 32 2x - 40 + 40 = 32 + 40 2x = 72 x = 36
294.	 Express y in terms of x in the first equation. Subtract 3x from both sides. Combine like terms and simplify. Substitute the value of y into the second equation in the system and solve for x. Combine like terms. Divide both sides by ⁻⁶. Substitute the found value for x into one of the equations and solve for y. Simplify. Add 12 to both sides. The solution for the system of equations is (⁻⁴,12). 	y + 3x = 0 y + 3x - 3x = 0 - 3x y = -3x (-3x) - 3x = 24 -6x = 24 x = -4 y + 3(-4) = 0 y - 12 = 0 y = 12

295.	Transform the first equation so that the value of <i>y</i> is expressed in terms of <i>x</i>. Subtract 5<i>x</i> from both sides of the equation.Combine like terms.Substitute the value of <i>y</i> into the second equation in the system and solve for <i>x</i>.Use the distributive property of multiplication.	5x - 5x + y = 20 - 5x y = 20 - 5x $3x = \frac{1}{2}(20 - 5x) + 1$ $3x = 10 - \frac{5}{2}x + 1$
	Combine like terms.	$3x = 11 - \frac{5}{2}x$
	Add $\frac{5}{2}x$ to both sides.	$3x + \frac{5}{2}x = 11 + \frac{5}{2}x - \frac{5}{2}x$
	Combine like terms.	$5\frac{1}{2}x = 11$
	Divide both sides by $5\frac{1}{2}$.	$\frac{5\frac{1}{2}x}{5\frac{1}{2}} = \frac{11}{5\frac{1}{2}}$
	Simplify terms.Substitute the found value for <i>x</i> into one of the equations and solve for <i>y</i>.Simplify.Subtract 10 from both sides.The solution for the system of equations is (2)	x = 2 5(2) + y = 20 10 + y = 20 y = 10 ,10).
296.	 value of x is expressed in terms of y. Add y to both sides of the equation. Combine like terms on each side. Substitute the value of x into the second equation in the system and solve for y. Use the distributive property of multiplication. Add 5y to both sides of the equation. Combine like terms on each side. Subtract 10 from both sides. Combine like terms on each side. Divide both sides by 8. Substitute the found value for y into one of the equations and solve for x. 	x - y + y = 5 + y x = 5 + y 2(5 + y) + y = 2 - 5y 10 + 2y + y = 2 - 5y 10 + 2y + y + 5y = 2 - 5y + 5y 10 + 8y = 2 10 - 10 + 8y = 2 - 10 $8y = {}^{-8}y = {}^{-1}$ $x - ({}^{-1}) = 5$ x + 1 = 5 x = 4
297.	The solution for the system of equations is (4) Transform the first equation by eliminating the denominators.	<u>,-1).</u>
	Multiply both sides of the equation by 10.	$10(\frac{2x}{10} + \frac{y}{5}) = 10(1)$
	Use the distributive property of multiplication Simplify terms.	n. $10(\frac{2x}{10}) + 10(\frac{y}{5}) = 10$ 2x + 2y = 10
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Divide both sides by 2. $\frac{2x+2x}{x+y=5}$ Now express x in terms of y. Subtract y from both sides of the equation. $x + y = 5$ Now express x in terms of y. Subtract y from both sides of the equation. $x + y - y = 5 - y$ Simplify. $x = 5 - y$ Substitute the value of x into the second equation and solve for y. $3(5 - y) + 2y = 12$ Use the distributive property of multiplication. Combine like terms on each side. $3(5 - y) + 2y = 12$ Add y to both sides. $15 - y + y = 12 + y$ Subtract 12 from both sides. $15 - y + y = 12 + y$ Subtract 12 from both sides. $3x + 2(3) = 12$ in the system and solve for x. $3x + 6 - 6 = 12 - 6$ Combine like terms on each side. $3x = 6$ Divide both sides by 3. $3x = 2$ The solution for the system of equations is (2,3).298.Transform the second equation so that the value of x is expressed in terms of y. Add 3 to both sides. $x = 2y + 3$ Substitute the value of x into the first equation in the system and solve for y. $(2y + 3) + 6y = 11$ Use the commutative property of addition. $2y + 6y + 3 = 11$ Subtract 3 from both sides.Subtract 6 from both sides.The solution for the system of equations is (5,1).299.Transform the second equation so that the equation and solve for x.Subtract 5 from both sides.Subtract 6 from both sides.The solution for the system of equations is (5,1).299.Transform the second equation so f.x.Subtract 6 from both sides.<		our Algebra Questions	
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Use the distributive property of multiplication. $4(3x) - 4(10) + 31 = 3x$			4(3x - 10) + 31 = 3x
		-	
Combine like terms on each side. $12x - 9 = 3x$		· ·	
Add 9 to both sides of the equation. $12x - 9 + 9 = 3x + 9$			
		rad / to both sides of the equation.	

 Combine like terms on each side. Subtract 3x from both sides. Combine like terms on each side. Divide both sides by 9. Substitute the value of x into the second equation and solve for y. Subtract 10 from both sides. Combine like terms on each side. The solution for the system of equations is 	12x = 3x + 9 12x - 3x = 3x - 3x + 9 9x = 9 x = 1 y + 10 = 3(1) y + 10 - 10 = 3 - 10 y = -7 (1,-7).
 Begin with the second equation and express x in terms of y. Use the distributive property of multiplication. Subtract 9 from both sides. Combine like terms on each side. Divide both sides by 3. Substitute the value of x into the second equation and solve for y. First, use the distributive property to simplify the equation. Multiply the numerator by the factor 2. Multiply both sides of the equation by 3 to eliminate the denominator. Use the distributive property of multiplication. Simplify each term. Simplify the second term and the – sign. Combine like terms on each side. Subtract 8y from both sides. Combine like terms on each side. Subtract 8y from both sides. Combine like terms on each side. Substitute the value of y into the first equation in the system and solve for x. Distributive property of multiplication. Subtract 4 from both sides. Simplify. Divide both sides by ⁻2. The solution for the system of equations is 	3x + 9 = 20 - 4y 3x = 11 - 4y $x = \frac{11 - 4y}{3}$ 4 - 2x = 3y - 2 $4 - 2(\frac{11 - 4y}{3}) = 3y - 2$ $4 - (\frac{22 - 8y}{3}) = 3y - 2$ $3(4 - (\frac{22 - 8y}{3})) = 3(3y - 2)$ $3(4) - 3(\frac{22 - 8y}{3}) = 3(3y) - 3(2)$ 12 - (22 - 8y) = 9y - 6 12 - 22 + 8y = 9y - 6 10 + 8y = 9y - 6 6 - 10 + 8y = 9y - 8y -4 + 8y - 8y = 9y - 8y -4 = y 2(2 - x) = 3(-4) - 2 4 - 2x = -12 - 2 4 - 4 - 2x = -12 - 2 - 4 -2x = -18 x = 9 (9,-4).
Combine like terms. Add 6 to both sides. Combine like terms on each side. Subtract 8y from both sides. Combine like terms on each side. Substitute the value of y into the first equation in the system and solve for x. Distributive property of multiplication. Subtract 4 from both sides. Simplify. Divide both sides by -2.	-10 + 8y = 9y - 6 6 - 10 + 8y = 9y + 6 - 6 -4 + 8y = 9y -4 + 8y - 8y = 9y - 8y -4 = y 2(2 - x) = 3(-4) - 2 4 - 2x = -12 - 2 4 - 4 - 2x = -12 - 2 - 4 -2x = -18 x = 9

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Working with Exponents

In this chapter, you will practice adding, subtracting, multiplying, and dividing expressions that contain variables with exponents. You will follow all the rules you have learned about operating with variables, but in this chapter, the variables have exponents.

Tips for Working with Exponents

Add and subtract like terms:

$$3n + 5n = 8n$$
, or $5x^2y - 3x^2y = 2x^2y$.

When multiplying variables with exponents, if the variables are the same, add the exponents and write the base only once:

$$\begin{aligned} (a^4)(a^3) &= a^{(4+3)} = a^7 \\ (x^2y^3)(axy^5) &= ax^{(2+1)}y^{(3+5)} = ax^3y^8 \end{aligned}$$

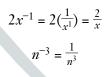
When dividing variables with exponents, if the variables are the same, you subtract the exponents:

$$\frac{n^{5}}{n^{2}} = \frac{n \cdot n \cdot n \cdot n \cdot n}{n \cdot n} = n^{5-2} = n^{3}$$

If the exponent of a similar term in the denominator is larger than the one in the numerator, the exponent will have a negative sign:

$$\frac{2x^3}{x^4} = 2x^{-1}$$
$$\frac{n^5}{x^8} = n^{5-8} = n^{-3}$$

A negative numerator becomes positive when the variable is moved into the denominator.



When the result of a division leaves an exponent of zero, the term raised to the power of zero equals 1:

When a variable with an exponent is raised to a power, you multiply the exponent to form the new term:

 $z^{0} = 1$ $3\frac{r^{2}}{r^{2}} = 3r^{0} = 3(1) = 3$

$$(b^2)^3 = b^2 \cdot b^2 \cdot b^2 = b^{(2+2+2)} = b^6$$

$$(2x^2y)^2 = 2x^2y \cdot 2x^2y = 2 \cdot 2 \cdot x^2 \cdot x^2 \cdot y \cdot y = 2^2x^{2+2}y^{1+1} = 4x^4y^2$$

Remember order of operations: PEMDAS. Generally, list terms in order from highest power to lowest power.

501 Algebra Questions Simplify the following expressions: **301.** $5x^2 + 8x^2$ **302.** $5ab^4 - ab^4$ **303.** $9mn^3 + 8mn + 2mn^3$ **304.** $5c^2 + 3c - 2c^2 + 4 - 7c$ **305.** $3x^2 + 4ax - 8a^2 + 7x^2 - 2ax + 7a^2$ **306.** $(5n^2)(2n^5 - 2n^3 + 3n^7)$ **307.** $5xy \cdot 6xy + 7x^2y^2$ **308.** $(5a^2 \cdot 3ab) + 2a^3b$ **309.** $\frac{8xy^2}{2xy}$ **310.** $(4a^2)^3 + (2a^3)^2 - 11a^6$ **311.** $\frac{(3x)^3}{x^2 \cdot x^4}$ **312.** $\frac{(12s^2)(2s^4)}{3s^3}$ **313.** $\frac{7a^3b^5}{28ab^2}$ **314.** $(3xy^5)^2 - 11x^2y^2(4y^4)^2$ **315.** $\frac{2(3x^2y)^2(xy)^3}{3(xy)^2}$ **316.** $\frac{2x^2y^5}{x^5y^3}$ **317.** $4x^{-2}(3ax)^5$ **318.** $\frac{3x^{-2}}{x^5} - \frac{2x}{x^8}$ **319.** $(5a^2x^3y)^3$ **320.** $\frac{24x^3}{(2x)^2} + \frac{3x^5}{x^4} - \frac{(3ax)^2}{a^2x}$ **321.** $(4x^2y)^3 + \frac{(2x^2y)^4}{2x^2y}$ **322.** $\frac{8ax^2}{(a^2x)^3}$ **323.** $(ab^2)^3 + 2b^2 - (4a)^3b^6$ **324.** $\frac{(4b)^2 x^{-2}}{(2ab^2 x)^2}$ **325.** $(2xy \cdot \frac{4}{x})^2 + \frac{9y^2}{(3y)^2}$

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), {}, or [], perform operations in the innermost parentheses first and work outward.

<u>Underlined</u> expressions show the simplified result.

	301.	Add like terms.	$5x^2 + 8x^2 = 13x^2$
	302.	Subtract like terms.	$5ab^4 - ab^4 = 4ab^4$
	303.	Use the commutative property of addition. Combine like terms.	$9mn^3 + 2mn^3 + 8mn$ $11mn^3 + 8mn$
	304.	Use the commutative property of addition. Combine like terms.	$\frac{5c^2 - 2c^2 - 7c + 3c + 4}{3c^2 - 4c + 4}$
j	305.	Use the commutative property of addition. Combine like terms.	$\frac{3x^2 + 7x^2 + 4ax - 2ax - 8a^2 + 7a^2}{10x^2 + 2ax - a^2}$
1	306.	Use the distributive property. Use the commutative property	$(5n^2)(2n^5) - (5n^2)(2n^3) + (5n^2)(3n^7)$
		of multiplication. $(5 \cdot 2 \cdot 2)$	$ \frac{n^2 n^5) - (5 \cdot 2 \cdot n^2 n^3) + (5 \cdot 3 \cdot n^2 n^7)}{0 \cdot n^{2+5}) - (10 \cdot n^{2+3}) + (15 \cdot n^{2+7})} \\ \frac{10 n^7 - 10 n^5 + 15 n^9}{15 n^9 + 10 n^7 - 10 n^5} $
	307.	Use the commutative property of multiplication. When the same variables are multiplied, add the exponents of the variables. Combine like terms.	$5 \cdot 6xxyy + 7x^2y^2$ $(30x^2y^2) + 7x^2y^2$ $37x^2y^2$
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308.	Use the commutative property of multiplication. When the same variables are multiplied, add the exponents of the variables. Combine like terms.	$(5 \cdot 3a^{2}ab) + 2a^{3}b$ $15a^{3}b + 2a^{3}b$ $17a^{3}b$
309.		$\frac{8xy^2}{2xy} = \frac{4xy^2}{xy}$ divided,
	Simplify.	$\frac{4x^0y^1 = 4(1)y = 4y}{4x^0y^1 = 4(1)y = 4y}$
310.	Terms within parentheses are the base of the exponent outside the parentheses.	$(4a^2)(4a^2)(4a^2)$ + $(2a^3)(2a^3) - 11a$
	Use the distributive property of multiplic When the same variables are multiplied, a the exponents of the variables.	ation. $(4 \cdot 4 \cdot 4)(a^2 \cdot a^2 \cdot a^2) + (2 \cdot 2)(a^3 \cdot a^3) - 11a$
	Simplify. Combine like terms. Another way of solving this problem is to multiply the exponents of each factor inside the parentheses by the exponent outside of the parentheses. Simplify the expressions in the exponents	$\frac{57a^6}{4^{(1)3}a^{(2)3} + 2^{(1)2}a^{(3)2} - 11a^6}$
	Simplify terms. Combine like terms.	$\frac{64a^6 + 4a^6 - 11a^6}{57a^6}$
311.	In the denominator, multiply the exponer factor inside the parentheses by the exp outside of the parentheses.	
	In the numerator, add the exponents of si When similar factors, or bases, are being you subtract the exponent in the denor	divided, [*]
	from the exponent in the numerator. A base with a negative exponent in the nu is equivalent to the same variable or ba denominator with the inverse sign for t	se in the
312.	Commutative property of multiplication. When similar factors, or bases, are multip the exponents of the variables.	blied, add $ \frac{12 \cdot 2s^2 \cdot s^4}{3s^3} $ $ \frac{12 \cdot 2s^{2+4}}{3s^3} $ $ \frac{8s^6}{s^3} $
	Simplify the exponent and coefficients.	<u>856</u>

	When similar factors, or bases, are being divided, subtract the exponent in the denominator from the exponent in the numerator. $8s^{6-3} = 8s^3$
313.	Divide out the common factor of 7 in the numerator and denominator. $\frac{1 \cdot 7a^3b^5}{4 \cdot 7ab^2} = \frac{1a^3b^5}{4ab^2}$ When similar factors, or bases, are being divided, subtract the exponent in the denominator from the exponent in the numerator. $\frac{1a^3b^5}{4ab^2} = \frac{1a^3-1b^5-2}{4}$
	Simplify exponents. $\frac{1a^2b^3}{4}$
	Separate the coefficient from the variable. Either expression is an acceptable answer. $\frac{\frac{1a^2b^3}{4} = \frac{1}{4}a^2b^3}{4}$
314.	Multiply the exponents of each factor inside the parentheses by the exponent outside the parentheses. $3^2x^2y^{10} - 11x^2y^24^2y^8$ Use the commutative property of multiplication. When similar factors, or bases, are multiplied,
315.	Multiply the exponents of each factor inside the parentheses by the exponent outside the parentheses. $\frac{2(3^2x^4y^2)(x^3y^3)}{3(x^2y^2)}$
羽	Use the commutative property of multiplication. $\frac{2 \cdot 9 \cdot x^4 x^3 y^2 y^3}{3x^2 y^2}$ When similar factors, or bases, are multiplied, add the exponents of the variables. $\frac{2 \cdot 9 \cdot x^4 x^3 y^2 y^3}{3x^2 y^2}$ Factor out like numerical terms in the fraction, and simplify exponents with operations. $\frac{6x^7 y^5}{x^2 y^2}$ When similar factors, or bases, are being divided, subtract the exponent in the denominator from the exponent in the numerator. $\frac{6x^7 - 2y^5 - 2}{6x^5 y^3}$
316.	When similar factors, or bases, are being divided, subtract the exponent in the denominator from the exponent in the numerator. $\frac{2x^2y^5}{x^5y^3} = 2x^{2-5}y^{5-3}$
	Simplify the operations in the exponents. A base with a negative exponent in the numerator is equivalent to the same variable or base in the denominator with the inverse sign for the exponent. $2x^{-3}y^2 = \frac{2y^2}{x^3}$
317.	Multiply the exponents of each factor inside the parentheses by the exponent outside the parentheses. $4x^{-2}(2^3a^3x^3)$ Use the commutative property of multiplication. $4 \cdot 3^3 \cdot a^3x^3x^{-2}$

	501 Algebra Questions	
	Evaluate numerical terms. When similar factors, or bases, are being multiplied, add the exponents. Simplify the operations in the exponents.	$ \begin{array}{r} 108a^3x^3x^{-2} \\ 108a^3x^{3-2} \\ 108a^3x \\ \end{array} $
318.	When similar factors, or bases, are being divided, subtract the exponent in the denominator from the exponent in the numerator.Simplify the operations in the exponents.Subtract like terms.A base with a negative exponent in the numerator is equivalent to the same variable or base in the denominator with the inverse sign for the exponent.	$3x^{-2-5} - 2x^{1-8}$ $3x^{-7} - 2x^{-7}$ x^{-7} $\frac{x^{-7} = \frac{1}{x^{7}}}{x^{-7}}$
319.	Multiply the exponents of each factor inside the parentheses by the exponent outside the parentheses. Evaluate the numerical coefficient.	$\frac{5^3 a^6 x^9 y^3}{125 a^6 x^9 y^3}$
320.	the parentheses by the exponent outside the parentheses. Evaluate the numerical coefficients and divide out common numerical factors in the terms. When similar factors, or bases, are being divided, subtract the exponent in the denominator from the exponent in the numerator. -1 $6x^3$ $x^2 + 3x^2$	$\frac{3x^{5}}{x^{4}} - \frac{3^{2}a^{2}x^{2}}{a^{2}x}$ $\frac{3x^{5}}{x^{4}} - \frac{9a^{2}x^{2}}{a^{2}x}$ $\frac{3x^{5}}{x^{4}} - \frac{9a^{2}x^{2}}{a^{2}x}$ $\frac{3x^{5}-4}{3x^{5}-4} - 9a^{2}-2x^{2}$ $\frac{3x^{1}-9a^{0}x^{1}}{a^{2}x}$
家	Any term to the power of zero equals 1. $6x + 3$	$3x^2 - 9a^2x^2$ $3x - 9(1)x$ $3x - 9x = 0x = 0$
321.	When similar factors, or bases, are being divided, subtract the exponent in the denominator from the exponent in the numerator. 4^3x Simplify the operations in the exponents. 4^3x Evaluate the numerical coefficients. $64x$	$\frac{x^{6}y^{3} + \frac{2^{4}x^{8}y^{4}}{2x^{2}y}}{x^{6}y^{3} + 2^{4} - \frac{1}{x^{8}} x^{8} - \frac{2}{y^{4}} - \frac{1}{x^{6}}}{x^{6}y^{3} + 2^{3}x^{6}y^{3}}$
322.	Multiply the exponents of each factor inside the parentheses by the exponent outside the parentheses. When similar factors, or bases, are being divided, subtract the exponent in the denominator from the exponent in the numerator. Simplify the operations in the exponents.	$\frac{8ax^2}{a^6x^3} \\ 8a^{1-6}x^{2-3} \\ 8a^{-5}x^{-1} \\ 8a^{-5}x^{-1}$
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		A base with a negative exponent in the numerator is equivalent to the same variable or base in the denom- inator with the inverse sign for the exponent.	$8a^{-5}x^{-1} = \frac{8}{a^5x^1} = \frac{8}{a^5x}$
	323.	Multiply the exponents of each factor inside the paren- theses by the exponent outside the parentheses. Evaluate the numerical coefficients. Use the commutative property of addition. Combine like terms in the expression.	$ \begin{array}{r} a^{3}b^{6} + 2b^{2} - 4^{3}a^{3}b^{6} \\ a^{3}b^{6} + 2b^{2} - 64a^{3}b^{6} \\ 2b^{2} - 64a^{3}b^{6} + a^{3}b^{6} \\ 2b^{2} - 63a^{3}b^{6} \\ \end{array} $
	324.	Multiply the exponents of each factor inside the parenth by the exponent outside the parentheses.	$\frac{4^{2}b^{2}x^{2}}{2^{2}a^{2}b^{4}x^{2}}$
		Evaluate the numerical coefficients.Simplify the numerical factors in the numerator and the denominator.When similar factors, or bases, are being divided, subtrative the exponent in the denominator from the exponent in the numerator.	$\frac{\frac{4b^2x^2}{a^2b^4x^2}}{a^2b^4x^2}$
	Ia	Simplify the operations in the exponents. A base with a negative exponent in the numerator is equ to the same variable or base in the denominator with inverse sign for the exponent.	
	325.	Multiply the exponents of each factor inside the parentheses by the exponent outside the parentheses.	
		Repeat the previous step.	$(2^2 x^2 y^2)(\frac{4^2}{x^2}) + \frac{9y^2}{3^2 y^2}$
Ę		Evaluate numerical factors.	$(4x^2y^2)(\frac{16}{x^2}) + \frac{9y^2}{9y^2}$
	53	The last term is equivalent to 1.	$(4x^2y^2)(\frac{16}{x^2}) + 1$
		Multiply the fraction in the first term by the factor in the first term.	$\left(\frac{(4x^2y^2)16}{x^2}\right) + 1$
		Use the commutative property of multiplication.	$\left(\frac{4 \cdot 16x^2y^2}{x^2}\right) + 1$
		Evaluate numerical factors. Divide out the common factor of x^2 in the	$\frac{64x^2y^2}{x^2} + 1$ $\frac{64y^2 + 1}{x^2}$
		numerator and denominator.	$64y^2 + 1$

Multiplying Polynomials

This chapter will present problems for you to solve in the multiplication of polynomials. Specifically, you will practice solving problems multiplying a monomial (one term) and a polynomial, multiplying binomials (expressions with two terms), and multiplying a trinomial and a binomial.

Tips for Multiplying Polynomials

When multiplying a polynomial by a monomial, you use the distributive property of multiplication to multiply each term in the polynomial by the monomial.

a(b+c+d+e) = ab + ac + ad + ae

When multiplying a binomial by a binomial, you use the mnemonic FOIL to remind you of the order with which you multiply				
terms in the binomials.	(a+b)(c+d)			
F is for first . Multiply the first terms				
of each binomial.	([a] + b)([c] + d) gives the term <i>ac</i> .			
O is for outer . Multiply the outer				
terms of each binomial.	([a] + b)(c + [d]) gives the term <i>ad</i> .			
I is for inner . Multiply the inner terms				
of each binomial.	(a + [b])([c] + d) gives the term <i>bc</i> .			
L is for last . Multiply the last terms				
of each binomial.	(a + [b])(c + [d]) gives the term bd .			
Then you combine the terms.	ac + ad + bc + bd			

Multiplying a trinomial by a binomial is relatively easy. You proceed similarly to the way you would when using the distributive property of multiplication. Multiply each term in the trinomial by the first and then the second term in the binomial. Then add the results.

$$(a + b)(c + d + e) = (ac + ad + ae) + (bc + bd + be)$$

Multiply the following polynomials.

326. x(5x + 3y - 7) **327.** $2a(5a^2 - 7a + 9)$ **328.** $4bc(3b^2c + 7b - 9c + 2bc^2 - 8)$ **329.** $3mn(-4m + 6n + 7mn^2 - 3m^2n)$ **330.** $4x(9x^3 + \frac{3}{x^2} - x^4 + \frac{6x - 1}{x^2})$ **331.** (x + 3)(x + 6) **332.** (x - 4)(x - 9) **333.** (2x + 1)(3x - 7) **334.** (x + 2)(x - 3y) **335.** (7x + 2y)(2x - 4y) **336.** (5x + 7)(5x - 7) **337.** $(28x + 7)(\frac{x}{7} - 11)$ **338.** $(3x^2 + y^2)(x^2 - 2y^2)$ **339.** $(4 + 2x^2)(9 - 3x)$ **340.** $(2x^2 + y^2)(x^2 - y^2)$ **341.** $(x + 2)(3x^2 - 5x + 2)$ **342.** $(2x - 3)(x^3 + 3x^2 - 4x)$ **343.** $(4a + b)(5a^2 + 2ab - b^2)$ **344.** $(3y - 7)(6y^2 - 3y + 7)$ **345.** $(3x + 2)(3x^2 - 2x - 5)$ **346.** (x + 2)(2x + 1)(x - 1) **347.** (3a - 4)(5a + 2)(a + 3) **348.** (2n - 3)(2n + 3)(n + 4) **349.** $(5r - 7)(3r^4 + 2r^2 + 6)$ **350.** $(3x^2 + 4)(x - 3)(3x^2 - 4)$

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501 Algebra Questions

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

<u>Underlined</u> expressions show the simplified result.

- **326.** Multiply each term in the trinomial by *x*. Simplify terms.
- **327.** Multiply each term in the trinomial by 2*a*. Simplify terms.
- **328.** Multiply each term in the polynomial by 4*bc*. Simplify terms.

- x(5x) + x(3y) x(7) $5x^{2} + 3xy - 7x$ $2a(5a^{2}) - 2a(7a) + 2a(9)$ $10a^{3} - 14a^{2} + 18a$
- $4bc(3b^{2}c) + 4bc(7b) 4bc(9c) + 4bc(2bc^{2}) 4bc(8)$ $12b^{3}c^{2} + 28b^{2}c - 36bc^{2} + 8b^{2}c^{3} - 32bc$
- **329.** Multiply each term in the polynomial by 3mn. 3mn(-4m) Simplify terms. $-12m^2n + 2m^2$

 $+ 28b^2c - 36bc^2 + 8b^2c^3 - 32bc$

 $nn. \quad 3mn(^{-}4m) + 3mn(6n) + 3mn(7mn^2) - 3mn(3m^2n) \\ -12m^2n + 18mn^2 + 21m^2n^3 - 9m^3n^2$

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330.	Multiply each term in the		
	polynomial by $4x$.	$4x(9x^3) + 4x(\frac{3}{x^2}) -$	$4x(x^4) + 4x(\frac{6x-1}{x^2})$
	Simplify terms.	$36x^4 + \frac{12x}{x^2} - 4x^5$	$+\frac{4x(6x-1)}{x^2}$
	Use the distributive property in the	x	x
	numerator of the fourth term.	$36x^4 + \frac{12x}{x^2} - 4x^5 - $	$+\frac{24x^{2}-4x}{x^{2}}$
	When similar factors, or bases, are	- 4	
	being divided, subtract the exponent in the denominator from the	lt	
	exponent in the numerator.	$36x^4 + 12x^{1-2} - 4$	$x^5 + 24x^{2-2} - 4x^{1-2}$
	Simplify operations in the		
	exponents.	$36x^4 + 12x^{-1} - 4x$	$x^{5} + 24x^{0} - 4x^{-1}$
	Use the associative property	$36x^4 + 12x^{-1} - 4x$	-1 4 5 34 0
	of addition. Combine like terms.	$36x^{4} + 8x^{-1} - 4x^{5}$	
	A base with a negative exponent	904 + 04 HA	T 2 14
	in the numerator is equivalent		
	to the same variable or base in		
	the denominator with the	26.4 8 4.5	04.0
	inverse sign for the exponent. A variable to the power of zero	$36x^4 + \frac{8}{x} - 4x^5 + 2$	$24x^{\circ}$
	equals 1.	$36x^4 + \frac{8}{x} - 4x^5 + 2$	24(1)
6	Simplify and put in order. $-4x^5 + 36x^4 + \frac{8}{x} + 24$		· · /
331.			
001.	Multiply the first terms in each binor	nial.	([x] + 3)([x] + 6)
			x^2
	Multiply the outer terms in each bind	omial.	([x] + 3)(x + [6])
	Multiply the image to provide such him	mial	+6x
L J J	Multiply the inner terms in each bind	omiai.	(x + [3])([x] + 6) +3x
	Multiply the last terms in each binon	nial.	(x + [3])(x + [6])
			+18
	Add the products of FOIL together.		$x^2 + 6x + 3x + 18$
	Combine like terms.		$\frac{x^2 + 9x + 18}{100}$
332.	1 2		
	Multiply the first terms in each binor	nial.	([x] - 4)([x] - 9)
	Multiply the outer terms in each bin	amial	
	Multiply the outer terms in each bind	Jiiiai.	([x] - 4)(x - [9]) -9x
	Multiply the inner terms in each bind	omial.	(x - [4])([x] - 9)
			-4x
	Multiply the last terms in each binon	nial.	(x - [4])(x - [9])
	Add the products of FOIL together.		+36 $x^2 - 9x - 4x + 36$
	Combine like terms.		$x^2 - 13x + 36$

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33	3. Use FOIL to multiply binomials. Multiply the first terms in each binomial.	([2x] + 1)([3x] - 7)
	Multiply the outer terms in each binomial.	$ \begin{array}{c} 6x^2 \\ ([2x] + 1)(3x - [7]) \end{array} $
	Multiply the inner terms in each binomial.	$^{-14x}$ (2x + [1])([3x] - 7) $^{+3x}$
	Multiply the last terms in each binomial.	(2x + [1])(3x - [7])
	Add the products of FOIL together. Combine like terms.	$ \begin{array}{r} 4x^2 - 14x + 3x - 7 \\ 6x^2 - 11x - 7 \end{array} $
334	 Use FOIL to multiply binomials. Multiply the first terms in each binomial. 	([x] + 2)([x] - 3y)
	Multiply the outer terms in each binomial.	([x] + 2)(x - [3y])
	Multiply the inner terms in each binomial.	(x + [2])([x] - 3y) +2x
	Multiply the last terms in each binomial.	(x + [2])(x - [3y])
IT.	Add the products of FOIL together.	$\frac{x^2-3xy+2x-6y}{2x-6y}$
- 33	5. Use FOIL to multiply binomials. Multiply the first terms in each binomial.	([7x] + 2y)([2x] - 4y) $14x^2$
	Multiply the outer terms in each binomial.	([7x] + 2y)(2x - [4y])
铴	Multiply the inner terms in each binomial.	$^{-28xy}$ (7x + [2y])([2x] - 4y)
133	Multiply the last terms in each binomial.	$^{+4xy}_{(7x + [2y])(2x - [4y])}$
	Add the products of FOIL together. Combine like terms.	$\frac{3y}{14x^2 - 28xy + 4xy - 8y^2}$ $\frac{14x^2 - 24xy - 8y^2}{14x^2 - 24xy - 8y^2}$
33	6. Use FOIL to multiply binomials. Multiply the first terms in each binomial.	([5x] + 7)([5x] - 7) $25x^2$
	Multiply the outer terms in each binomial.	([5x] + 7)(5x - [7]) -35x
	Multiply the inner terms in each binomial.	(5x + [7])([5x] - 7) +35x
	Multiply the last terms in each binomial.	(5x + [7] (5x - [7])) -49
	Add the products of FOIL together. Combine like terms.	$\frac{25x^2 - 35x + 35x - 49}{25x^2 - 49}$

	337.	Use FOIL to multiply binomials. Multiply the first terms in each binomial.	$([28x] + 7)([\frac{x}{7}] - 11) 4x^2$	
		Multiply the outer terms in each binomial.	$([28x] + 7)(\frac{x}{7} - [11])$	
		Multiply the inner terms in each binomial.	$^{-308x}$ (28x + [7])([$\frac{x}{7}$] - 11)	
		Multiply the last terms in each binomial.	$(28x + [7])(\frac{x}{7} - [11])$	
		Add the products of FOIL together. Combine like terms.	$\frac{4x^2 - 308x + x - 77}{4x^2 - 307x - 77}$	
	338.	Use FOIL to multiply binomials. Multiply the first terms in each binomial.	$([3x^2] + y^2)([x^2] - 2y^2)$ $3x^4$	
		Multiply the outer terms in each binomial.	$([3x^2] + y^2)(x^2 - [2y^2])$	
		Multiply the inner terms in each binomial.	([3x2] + y2)(x2 - [2y2])-6x2y2(3x2 + [y2])([x2] - 2y2+x2y2(x - 2 - 2y2)	
		Multiply the last terms in each binomial.	$(3x^{2} + [y^{2}])(x^{2} - [2y^{2}])$ $-2y^{4}$ $3x^{4} - 6x^{2}y^{2} + x^{2}y^{2} - 2y^{4}$	
		Add the products of FOIL together. Combine like terms.	$\frac{3x^4 - 6x^2y^2 + x^2y^2 - 2y^4}{3x^4 - 5x^2y^2 - 2y^4}$	
J	339.	Use FOIL to multiply binomials. Multiply the first terms in each binomial.	$([4] + 2x^2)([9] - 3x)$ +36	
đ		Multiply the outer terms in each binomial.	$([4] + 2x^2)(9 - [3x])$ -12x	
9		Multiply the inner terms in each binomial.	$(4 + [2x^2])([9] - 3x) + 18x^2$	
		Multiply the last terms in each binomial.	$(4 + [2x^2])(9 - [3x])$ $^{-3}x^3$	
		Add the products of FOIL together. Simplify and put them in order from the	$36 - 12x + 18x^2 - 3x^3$	
	240	highest power.	$\frac{-3x^3 + 18x^2 - 12x + 36}{-12x + 36}$	
	340.	Use FOIL to multiply binomials. Multiply the first terms in each binomial.	$([2x^2] + y^2)([x^2] - y^2)$	
		Multiply the outer terms in each binomial.	([2x2] + y2)([x2] - y2)2x4([2x2] + y2)(x2 - [y2])-2x2y2	
		Multiply the inner terms in each binomial.	$(2x^{2} + [y^{2}])([x^{2}] - y^{2}) + x^{2}y^{2}$	
		Multiply the last terms in each binomial.	$(2x^2 + [y^2])(x^2 - [y^2])$	
		Add the products of FOIL together. Combine like terms.	$\frac{2x^4 - 2x^2y^2 + x^2y^2 - y^4}{2x^4 - x^2y^2 - y^4}$	
- 1		200		

341.	Multiply the trinomial by the first	erm
3 7 1.	in the binomial, <i>x</i> .	$[x(3x^2 - 5x + 2)]$
	in the binomial, <i>x</i> .	$[x(3x^2) - x(5x) + x(2)]$
	Simplify torms	$[3x^{3} - 5x^{2} + 2x]$
	Simplify terms.	L J
	Multiply the trinomial by the second	
	term in the binomial, 2.	$[2(3x^2 - 5x + 2)]$
		$[2(3x^2) - 2(5x) + 2(2)]$
	Simplify terms.	$[6x^2 - 10x + 4]$
	Add the results of multiplying by the	
	terms in the binomial together.	$[3x^3 - 5x^2 + 2x] + [6x^2 - 10x + 4]$
	Use the commutative property of a	ddition. $3x^3 - 5x^2 + 6x^2 + 2x - 10x + 4$
	Combine like terms.	$3x^3 + x^2 - 8x + 4$
342.	Multiply the trinomial by the first	
J72.	term in the binomial, $2x$.	$[2x(x^3 + 3x^2 - 4x)]$
	Use the distributive property of	$\left[2x(x + 3x - 1x)\right]$
		$[2x(x^3) + 2x(3x^2) - 2x(4x)]$
	multiplication.	$[2x(x^{2}) + 2x(3x^{2}) - 2x(4x)]$ $[2x^{4} + 6x^{3} - 8x^{2}]$
	Simplify terms.	L J
	Multiply the trinomial by the second	
	term in the binomial, -3 .	$[-3(x^3 + 3x^2 - 4x)]$
	Use the distributive property of	
	multiplication.	$[^{-3}(x^3) - 3(3x^2) - 3(^{-4}x)]$
61	Simplify terms.	$[-3x^3 - 9x^2 + 12x]$
	Add the results of multiplying by the	ne de la companya de
	terms in the binomial together.	$[2x^4 + 6x^3 - 8x^2] + [-3x^3 - 9x^2 + 12x)]$
	Use the commutative property	
~	of addition.	$2x^4 + 6x^3 - 3x^3 + 8x^2 - 9x^2 + 12x$
	Combine like terms.	$\frac{2x^4 + 3x^3 - 17x^2 + 12x}{12x}$
343.	Multiply the trinomial by the first	
010.	term in the binomial, 4 <i>a</i> .	$[4a(5a^2 + 2ab - b^2)]$
	Use the distributive property of	$[\mp u(5u^{2} + 2uv - v^{2})]$
	multiplication.	$[4a(5a^2) + 4a(2ab) - 4a(b^2)]$
	Simplify terms.	$[20a^3 + 8a^2b - 4ab^2]$
	Multiply the trinomial by the	
	second term in the binomial, <i>b</i> .	$[b(5a^2+2ab-b^2)]$
	Use the distributive property of	
	multiplication.	$[b(5a^2) + b(2ab) - b(b^2)]$
	Simplify terms.	$[5a^2b + 2ab^2 - b^3]$
	Add the results of multiplying by	
	the terms in the binomial	
	together.	$[20a^3 + 8a^2b - 4ab^2] + [5a^2b + 2ab^2 - b^3)]$
	Use the commutative property of	
	addition.	$20a^3 + 8a^2b + 5a^2b - 4ab^2 + 2ab^2 - b^3$
	uddition	

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344.	Multiply the trinomial by the first term in the binomial, 3 <i>y</i> .	$[3\gamma(6\gamma^2 - 3\gamma + 7)]$
	Use the distributive property of	
	multiplication.	$[3y(6y^2) - 3y(3y) + 3y(7)]$ [18y ³ - 9y ² + 21y]
	Multiply the trinomial by the second term in the binomial, ⁻ 7.	$[-7(6y^2 - 3y + 7)]$
		$[-7(6y^2) - 7(-3y) - 7(7)]$
	Add the results of multiplying	$[-42y^2 + 21y - 49]$
	8	$[18y^3 - 9y^2 + 21y] + [-42y^2 + 21y - 49]$
		$18y^{3} - 9y^{2} - 42y^{2} + 21y + 21y - 49$ $18y^{3} - 51y^{2} + 42y - 49$
345.	Multiply the trinomial by the first ter	<u> </u>
343.	in the binomial, 3 <i>x</i> . Use the distributive property	$[3x(3x^2 - 2x - 5)]$
	of multiplication. Simplify terms.	$[3x(3x^2) - 3x(2x) - 3x(5)]$ $[9x^3 - 6x^2 - 15x]$
9	Multiply the trinomial by the second term in the binomial, 2.	$[2(3x^2-2x-5)]$
	Use the distributive property of multiplication.	$[2(3x^2) - 2(2x) - 2(5)]$
	Simplify terms.	[2(3x) - 2(2x) - 2(3)] [6x ² - 4x - 10]
	Add the results of multiplying by the	
33	terms in the binomial together. Use the commutative property	$[9x^3 - 6x^2 - 15x] + [6x^2 - 4x - 10]$
	of addition.	$9x^3 - 6x^2 + 6x^2 - 15x - 4x - 10$
	Combine like terms.	$9x^3 - 19x - 10$
346.	Multiply the first two parenthetical te in the expression using FOIL .	rms
	Multiply the first terms in each binor	nial. $([x] + 2)([2x] + 1)$ $2x^2$
	Multiply the outer terms in each	
	binomial.	([x] + 2)(2x + [1]) +x
	Multiply the inner terms in each	
	binomial.	(x + [2])([2x] + 1)
	Multiply the last terms in each binom	$\begin{array}{c} +4x \\ \text{iial.} (x + [2])(2x + [1]) \\ +2 \end{array}$
	Add the products of FOIL together. Combine like terms.	$ 2x^{2} + x + 4x + 2 2x^{2} + 5x + 2 $

		 Multiply the resulting trinomial by the last binomial in the original expression. Multiply the trinomial by the first term in the binomial, <i>x</i>. Use the distributive property of multiplication. Simplify terms. Multiply the trinomial by the second term in the binomial, ⁻¹. Use the distributive property of multiplication. Add the results of multiplying by the terms in the binomial together. Use the commutative property of addition. Combine like terms. 	$(x - 1)(2x^{2} + 5x + 2)$ $[x(2x^{2} + 5x + 2)]$ $[x(2x^{2} + 5x + 2)]$ $[x(2x^{2}) + x(5x) + x(2)]$ $[2x^{3} + 5x^{2} + 2x]$ $[^{-1}(2x^{2} + 5x + 2)]$ $[^{-2}x^{2} - 5x - 2]$ $[2x^{3} + 5x^{2} + 2x] + [^{-2}x^{2} - 5x - 2]$ $2x^{3} + 5x^{2} - 2x^{2} + 2x - 5x - 2$ $\frac{2x^{3} + 3x^{2} - 3x - 2}{2x^{3} + 3x^{2} - 3x - 2}$	
101	347.	 Multiply the first two parenthetical t in the expression using FOIL. Multiply the first terms in each binomial. Multiply the outer terms in each binomial. Multiply the inner terms in each binomial. Multiply the last terms in each binomial. 	erms $([3a] - 4)([5a] + 2)$ $15a^{2}$ $([3a] - 4)(5a + [2])$ $+6a$ $(3a - [4])([5a] + 2)$ $-20a$ $(3a - [4])(5a + [2])$	
		 Add the products of FOIL together. Combine like terms. Multiply the resulting trinomial by the last binomial in the original expression. Multiply the trinomial by the first term in the binomial, <i>a</i>. Use the distributive property of multiplication. Simplify terms. Multiply the trinomial by the second term in the binomial, 3. Use the distributive property of multiplication. 	$-\frac{8}{15a^{2} + 6a - 20a - 8}$ $15a^{2} - 14a - 8$ $(a + 3)(15a^{2} - 14a - 8)$ $[a(15a^{2} - 14a - 8)]$ $[a(15a^{2} - 14a - 8)]$ $[a(15a^{2} - a(14a) - a(8)]$ $[15a^{3} - 14a^{2} - 8a]$ $[3(15a^{2}) - 3(14a) - 3(8)]$ $[45a^{2} - 42a - 24]$	

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		Add the results of multiplying by the	he	
		terms in the binomial together.		$[8a] + [45a^2 - 42a - 24]$
		Use the commutative property	L	
		of addition.		$5a^2 - 8a - 42a - 24$
		Combine like terms.	$\frac{15a^3 + 31a^2 - 5}{2}$	0a - 24
	348.	Multiply the first two parenthetical	l terms	
		in the expression using FOIL .		
		Multiply the first terms in each bir	nomial.	([2n] - 3)([2n] + 3)
				$4n^2$
		Multiply the outer terms in each b	inomial.	([2n] - 3)(2n + [3])
				+6n
		Multiply the inner terms in each b	inomial.	(2n - [3])([2n] + 3)
		A<i>x</i> 1 1 1 1 1 1 1 1 1 1	• 1	-6n
		Multiply the last terms in each bin	omial.	(2n - [3])(2n + [3])
		Add the products of FOIL togethe	r	$\frac{-9}{4n^2+6n-6n-9}$
		Combine like terms.	1.	$4n^2 - 9$
		Now we again have two binomials.	Use FOIL	
		to find the solution.		$(n + 4)(4n^2 - 9)$
ł		Multiply the first terms in each bir	nomial.	$([n] + 4)([4n^2] - 9)$ $4n^3$
				172
		Multiply the outer terms in each b	inomial.	$([n] + 4)(4n^2 - [9])$
		37.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1		-9n
		Multiply the inner terms in each b	inomiai.	$(n + [4])([4n^2] - 9)$ +16n ²
J		Multiply the last terms in each bin	omial.	$(n + [4])(4n^2 - [9])$
ļ				-36
ł		Add the products of FOIL togethe	r.	$4n^3 - 9n + 16n^2 - 36$
ł	ĽĽ	Order terms from the highest to lo	west power.	$\frac{4n^3 + 16n^2 - 9n - 36}{4n^3 + 16n^2 - 9n - 36}$
1	349.	Multiply the trinomial by the		
		first term in the binomial, $5r$.	$[5r(3r^4 + 2r^2 + 6)$	
		Use the distributive property of		
		multiplication.	$[5r(3r^4) + 5r(2r^2)]$	
		Simplify terms.	$[15r^5 + 10r^3 + 30]$	<i>r</i>]
		Multiply the trinomial by the sec-	[-7/2 4 2 2]	,
		ond term in the binomial, ⁻⁷ . Use the distributive property of	$[-7(3r^4 + 2r^2 + 6)]$]
		multiplication.	$[-7(3r^4) - 7(2r^2) -$	- 7(6)]
		Simplify terms.	$[-21r^4 - 14r^2 - 42r^2]$	
		Add the results of multiplying		·
		by the terms in the binomial		
		together.	$[15r^5 + 10r^3 + 30]$	r] + [$-21r^4 - 14r^2 - 42$]
		Use the commutative property	<i>.</i> .	
		of addition.	$\frac{15r^{5} - 21r^{4} + 10r}{10r}$	$3^{3} - 14r^{2} + 30r - 42$

350. Multiply the first two parenthetical terms in the expression using FOIL. $([3x^2] + 4)([x] - 3)$ $3x^3$ Multiply the **first** terms in each binomial. $([3x^2] + 4)(x - [3])$ $^{-9x^2}$ Multiply the **outer** terms in each binomial. $(3x^2 + [4])([x] - 3)$ Multiply the **inner** terms in each binomial. +4x $(3x^2 + [4])(x - [3])$ Multiply the **last** terms in each binomial. -12 $(3x^3 - 9x^2 + 4x - 12)$ Add the products of FOIL together. Multiply the resulting trinomial by the last $(3x^2 - 4)(3x^3 - 9x^2 + 4x - 12)$ binomial in the original expression. Multiply the trinomial by the first term $[3x^2(3x^3 - 9x^2 + 4x - 12)]$ in the binomial, $3x^2$. Use the distributive property $[3x^2 (3x^3) - 3x^2(9x^2)]$ of multiplication. $+ 3x^{2}(4x) - 3x^{2}(12)]$ $[9x^{5} - 27x^{4} + 12x^{3} - 36x^{2}]$ Simplify terms. Multiply the trinomial by the second term in the binomial, -4. $[-4(3x^3 - 9x^2 + 4x - 12)]$ Use the distributive property $[-12x^3 + 36x^2 - 16x + 48]$ of multiplication. Add the results of multiplying by the $[9x^5 - 27x^4 + 12x^3 - 36x^2]$ terms in the binomial together. $+ [-12x^3 + 36x^2 - 16x + 48]$ $9x^5 - 27x^4 + 12x^3 - 12x^3 -$ Use the commutative property of addition. $36x^2 + 36x^2 - 16x + 48$ $9x^5 - 27x^4 - 16x + 48$ Combine like terms.

Factoring Polynomials



This chapter will present algebraic expressions for you to factor. You can use three different techniques to factor polynomials. In the first technique, you look for common factors in the terms of the polynomial. In the second, you will factor polynomials that are the difference of two perfect squares. The third technique, called the trinomial factor method, will allow you to factor algebraic expressions that have three terms. The trinomial expressions in this chapter will be in the form of $x^2 \pm ax \pm b$, where *a* and *b* are whole numbers. The problems will be presented in random order to give you practice at recognizing which method or combination of methods will be required to factor the polynomial. Complete explanations of the solutions will follow.

Tips for Factoring Polynomials

<u>Factoring using the greatest common factor</u>: Look for a factor common to every term in the polynomial. Put that factor outside a set of parentheses and the polynomial inside with the factor removed from each term, e.g. $2x^2 + 8 = 2(x^2 + 4)$

<u>Factoring using the difference of two perfect squares</u>: Polynomials in the form $x^2 - y^2$ can be factored into two terms: (x + y)(x - y).

<u>Factoring using the trinomial method</u>: This method requires you to factor the first and third terms and put the factors into the following

factored form: ([] ± [])([] ± []). The factors of the first term go in the first position in the parentheses and the factors of the third term go in the second position in each factor, e.g. $x^2 + 2x + 1 = (x + 1)(x + 1)$.

Factor the following polynomials.

351. 9*a* + 15 **352.** $3a^2x + 9ax$ **353.** $x^2 - 16$ **354.** $4a^2 - 25$ **355.** $7n^2 - 28n$ **356.** $7x^4y^2 - 35x^2y^2 + 14x^2y^4$ **357.** $x^2 + 3x + 2$ **358.** $9r^2 - 49$ **359.** $x^2 - 2x - 8$ **360.** $x^2 + 5x + 6$ **361.** $x^2 + x - 6$ **362.** $b^2 - 100$ **363.** $x^2 + 7x + 12$ **364.** $x^2 - 3x - 18$ **365.** $b^2 - 6b + 8$ **『**字 **366.** $b^2 - 4b - 21$ **367.** $a^2 + 11a - 12$ **368.** $x^2 + 10x + 25$ **369.** $36y^4 - 4z^2$ **370.** $x^2 + 20x + 99$ **371.** $c^2 - 12c + 32$ **372.** $b^2 - 12b + 11$ **373.** $m^2 - 11m + 18$ **374.** $v^4 - 13v^2 - 48$ **375.** $x^2 - 20x + 36$

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

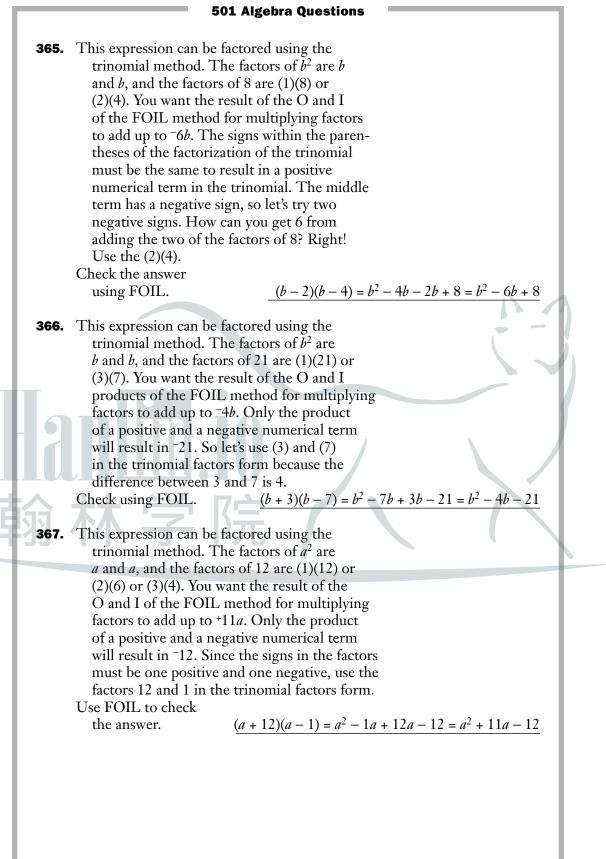
Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

<u>Underlined</u> expressions show the original algebraic expression as an equation with the expression equal to its simplified result.

351.	The terms have a common factor of 3.Factor 3 out of each term and write the expression in factored form. $9a + 15 = 3(3a + 5)$	
9	The terms have a common factor of $3ax$. Factor $3ax$ out of each term and write the expression in factored form. $3a^2x + 9ax = 3ax(a + 3)$ Both terms in the polynomial are perfect squares. Use the form for factoring the difference of two perfect squares and put the roots of each factor in the proper place. $x^2 - 16 = (x + 4)(x - 4)$ Check using FOIL.	
354.	Both terms in the polynomial are perfect squares. $4a^2 = (2a)^2$, and $25 = 5^2$. Use the form for factoring the difference of two perfect squares and put the roots of each factor in the proper place. $4a^2 - 25 = (2a + 5)(2a - 5)$ Check using FOIL. $(2a + 5)(2a - 5) = 4a^2 - 10a + 10a - 25 = 4a^2 - 25$	
355.	The terms have a common factor of $7n$. Factor $7n$ out of each term and write the expression in factored form. $\underline{7n^2 - 28n = 7n(n-4)}$	
356.	The terms have a common factor of $7x^2y^2$. Factor $7x^2y^2$ out of each term in the expression and write it in factored form. $\frac{7x^2y^2(x^2 - 5 + 2y^2)}{x^2y^2(x^2 - 5 + 2y^2)}$	

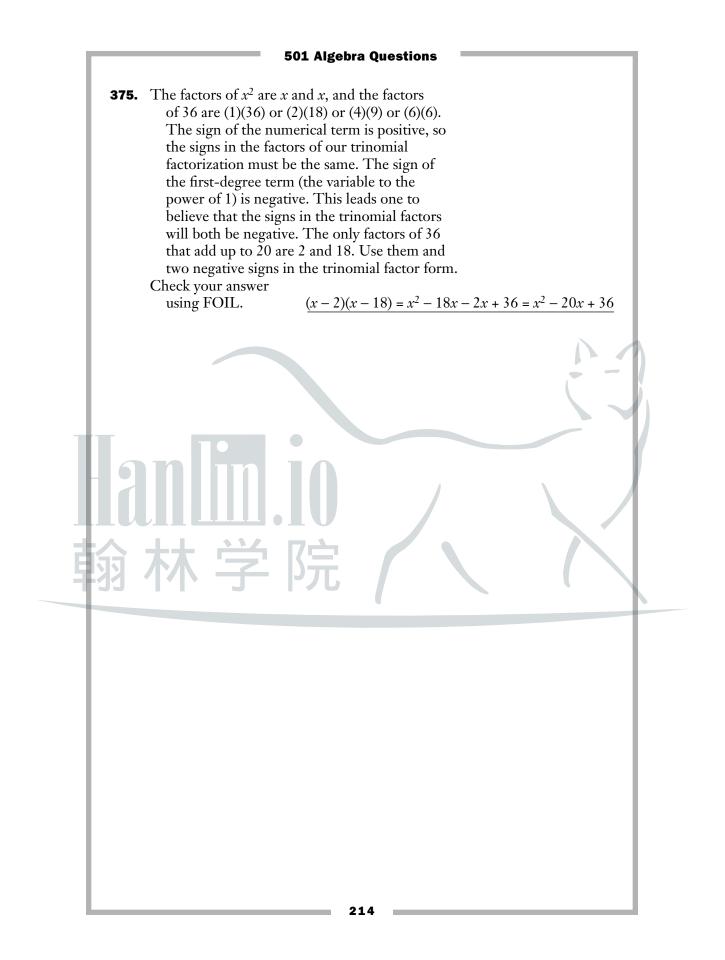
	501 Algebra Questions
357.	This expression can be factored using the trinomial method. The factors of x^2 are x and x , and the factors of 2 are 1 and 2. Place the factors into the trinomial factor form and check using FOIL. $(x + 2)(x + 1) = x^2 + x + 2x + 2 = x^2 + 3x + 2$ The factors are correct.
358.	Both terms in the polynomial are perfect squares. $9r^2 = (3r)^2$ and $49 = 7^2$. Use the form for factoring the difference of two perfect squares and put the roots of each factor in the proper place. $9r^2 - 36 = (3r + 7)(3r - 7)$
359.	 This expression can be factored using the trinomial method. The factors of x² are x and x, and the factors of 8 are (1)(8) and (2)(4). You want the result of the O and I of the FOIL method for multiplying factors to add up to ⁻2x. Only terms with opposite signs will result in a negative numerical term, which is what you need, since the third term is ⁻8. Place the factors (2)(4) into the trinomial factor form and check using FOIL. (x + 4)(x - 2) = x² - 2x + 4x - 8 = x² + 2x - 8 Almost correct! Change the position of the factors of the numerical term and check using FOIL. (x + 2)(x - 4) = x² - 4x + 2x - 8 = x² - 2x - 8 The factors of the trinomial are now correct.
	<i>x</i> and <i>x</i> , and the factors of 6 are (1)(6) and (2)(3). Since the numerical term of the polynomial is positive, the signs in the factor form for trinomials will be the same because only two like signs multiplied together will result in a positive. Now consider the second term in the trinomial. In order to add up to 5 <i>x</i> , the result of multiplying the Inner and Outer terms of the trinomial factors will have to be positive. Try using two positive signs and the factors 2 and 3, which add up to 5. Check using FOIL. $(x + 2)(x + 3) = x^2 + 2x + 3x + 6 = x^2 + 5x + 6$
	209

361.	This expression can be factored using the
	trinomial method. The factors of x^2 are
	x and x, and the factors of 6 are $(1)(6)$ and
	(2)(3). You want the result of the O and I of
	the FOIL method for multiplying factors
	to add up to $^{+}1x$. Only terms with opposite
	signs will result in a negative numerical
	term that you need with the third term
	being a -6 . Place the factors (2)(3) into
	the trinomial factor form and check
	using FOIL. $(x+3)(x-2) = x^2 - 2x + 3x - 6 = x^2 + x - 6$
	The factors of the trinomial are now correct.
362.	Both terms in the polynomial are perfect squares.
	$b^2 = (b)^2$ and $100 = 10^2$. Use the form for
	factoring the difference of two perfect squares
	and put the roots of each factor in the
	proper place. $b^2 - 100 = (b + 10)(b - 10)$
	Check using FOIL. $(b + 10)(b - 10) = b^2 - 10b + 10b - 100 = b^2 - 100$
363.	This expression can be factored using the
	trinomial method. The factors of x^2 are
	x and x, and the factors of 12 are $(1)(12)$ or
	(2)(6) or $(3)(4)$. You want the result of the
	O and I of the FOIL method for multiplying
	factors to add up to $+7x$. The factors (3)(4)
\wedge	would give terms that add up to 7. Since
	all signs are positive, use positive signs
JJ	in the factored form
	for the trinomial. $(x + 3)(x + 4) = x^2 + 3x + 4x + 12 = x^2 + 7x + 12$
	The result is correct. This is not just luck. You
	can use logical guesses to find the correct combination of factors and signs.
364.	This expression can be factored using the
	trinomial method. The factors of x^2 are
	x and x, and the factors of 18 are $(1)(18)$ or (2)(0) or $(2)(6)$ Only the gradient of a positive
	(2)(9) or (3)(6). Only the product of a positive
	and a negative numerical term will result in -18 . The sum of the results of multiplying
	⁻ 18. The sum of the results of multiplying the Outer and Inner terms of the trinomial
	factors needs to add up to a ^{-3}x . So use
	(3)(6) in the trinomial factors form and check
	using FOIL. $(x + 3)(x - 6) = x^2 - 6x + 3x - 18 = x^2 - 3x - 18$
	using 1 G12. $(u + 5)(u - 0) - u - 0u + 5u - 10 - u - 5u - 10$



	501 Algebra Questions
368.	This expression can be factored using the trinomial method. The factors of x^2 are x and x , and the factors of 25 are (1)(25) or (5)(5). To get a positive 25 after multiplying the factors of the trinomial expression, the signs in the two factors must both be positive or both be negative. The sum of the results of multiplying the Outer and Inner terms of the trinomial factors needs to add up to a +10x. So let's use (5)(5) in the trinomial factors form and check using FOIL. $(x + 5)(x + 5) = x^2 + 5x + 5x + 25 = x^2 + 10x + 25$
369.	Both terms in the polynomial are perfect squares. $36y^2 = (6y^2)^2$ and $4z^2 = (2z)^2$ Use the form for factoring the difference of two perfect squares and put the roots of each factor in the proper place. $(6y^2 + 2z)(6y^2 - 2z)$ Check using FOIL. $(6y^2 + 2z)(6y^2 - 2z) = 36y^4 - 12y^2z + 12y^2z - 4z^2 = 36y^4 - 4z^2$
370.	This expression can be factored using the trinomial method. The factors of x^2 are x and x , and the factors of 99 are (1)(99) or (3)(33) or (9)(11). To get a positive 99 after multiplying the factors of the trinomial expression, the signs in the two factors must both be positive or both are negative. The sum of the results of multiplying the Outer and Inner terms of the trinomial factors needs to add up to a $*20x$. So let's use (9)(11) in the trinomial factors form because $9 + 11 = 20$.
371.	Check using FOIL. $(x + 9)(x + 11) = x^2 + 9x + 11x + 99 = x^2 + 20x + 99$
	are 4 and 8. Check using FOIL. $(c-4)(c-8) = c^2 - 8c - 4c + 32 = c^2 - 12c + 32$

	501 Algebra Questions
372.	The factors of b^2 are <i>b</i> and <i>b</i> , and the factors of 11 are (1)(11). The sign of the numerical term is positive, so the signs in the factors of our trinomial factorization must be the same. The sign of the first-degree term (the variable to the power of 1) is negative. So use negative signs in the trinomial factors. Check your answer. $(b-1)(b-11) = b^2 - 11b - 1b + 11 = b^2 - 12b + 11$
373.	



Using Factoring



This chapter will present polynomial expressions for you to factor. In the previous chapter, all the coefficients of the second-degree terms were 1. In this chapter, the coefficients of the second-degree terms will often be whole numbers greater than 1. This will complicate the process of factoring by adding more possibilities to check. In some cases, you will find that you can factor using more than one of the three methods of factoring polynomials on the given expression.

Always look to factor algebraic expressions using the greatest common factor method first. Then analyze the remaining expression to determine if other factoring methods can be used. The three methods for factoring polynomial expressions are:

- 1. Greatest common factor method
- 2. Difference of two perfect squares method
- 3. Trinomial method

When presented with a polynomial with a coefficient greater than 1 for the second-degree term, use the trinomial factor form $(ax \pm ())(bx \pm ())$ where $a \cdot b$ = the coefficient of the second-degree term. List the factors of the numerical term of the trinomial and consider the choices of factors and signs that will result in the correct trinomial factorization.

After choosing terms to try in the trinomial factors form, use FOIL to check your guesses for the trinomial factors. You will want to do a partial check by first completing the O and the I part of FOIL to determine if you have the first-degree term right.

Tips for Using Factoring

When factoring a trinomial expression, first determine the signs that will be used in the two factors.

Next, list the possible factors of the second-degree term.

Then list the factors of the numerical term.

Finally, place the factors into the trinomial factor form in all possible ways and use FOIL to check for the correct factorization.

Be systematic in your attempts to be sure you try all possible choices. You will become better at factoring as you learn to look for the combinations of factors that will give you the required results for the first-degree term.

```
Factor the following expressions.
```

377. $3x^2 + 13x + 12$ **378.** $5x^2 - 14x - 3$ **379.** $9x^2 + 15x + 4$ **380.** $9x^2 + 34x - 8$ **381.** $3x^2 - 3x - 18$ **382.** $4a^2 - 16a - 9$ **383.** $6a^2 - 13a - 15$ **384.** $6a^2 - 5a - 6$ **385.** $16y^2 - 100$ **386.** $6x^2 + 15x - 36$ **387.** $4bc^2 + 22bc - 42b$

376. $2x^2 + 7x + 6$

388.
$$2a^6 + a^3 - 21$$

389.
$$6a^2x - 39ax - 72x$$

390. $8x^2 - 6x - 9$

391. $5c^2 - 9c - 2$ **392.** $9x^3 - 4x$ **393.** $8r^2 + 46r + 63$ **394.** $4x^4 - 37x^2 + 9$ **395.** $12d^2 + 7d - 12$ **396.** $4xy^3 + 6xy^2 - 10xy$ **397.** $4ax^2 - 38ax - 66a$ **398.** $3c^2 + 19c - 40$ **399.** $2a^2 + 17a - 84$

400. $4x^4 + 2x^2 - 30$

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Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

<u>Underlined</u> expressions show the original algebraic expression as an equation with the expression equal to its simplified result.

376. Both signs in the trinomial are positive, so use positive signs in the trinomial factor form.

(ax + ())(bx + ())

The factors of the second-degree term are $2x^2 = (2x)(x)$.

The numerical term 6 = (1)(6) = (2)(3).

You want to get 7x from adding the result of the Outer and Inner multiplications when using FOIL. You could make the following guesses for the factors of the original expression.

(2x + (1))(x + (6))

$$(2x + (6))(x + (1))$$

```
(2x + (2))(x + (3))
```

(2x + (3))(x + (2))

Now just consider the results of the Outer and Inner products of the terms for each guess. The one that results in a first-degree term of 7x is the factorization you want to fully check.

(2x + (1))(x + (6)) will result in Outer product plus Inner product: 2x(6) + (1)x = 12x + x = 13x.

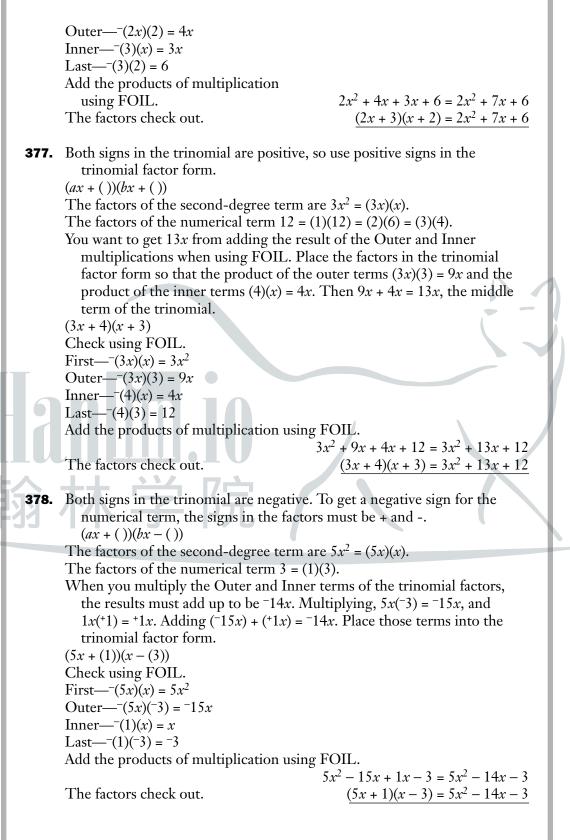
- (2x + (6))(x + (1)) will result in Outer product plus Inner product: 2x(1) + (6)x = 2x + 6x = 8x.
- (2x + (2))(x + (3)) will result in Outer product plus Inner product: 2x(3) + (2)x = 6x + 2x = 8x.
- (2x + (3))(x + (2)) will result in Outer product plus Inner product: 2x(2) + (3)x = 4x + 3x = 7x.

Place the factors in the trinomial factor form so that the product of the outer terms (2x)(2) = 4x and the product of the inner terms (3)(x) = 3x. That way, 4x + 3x = 7x, the middle term of the trinomial.

(2x + (3))(x + (2))

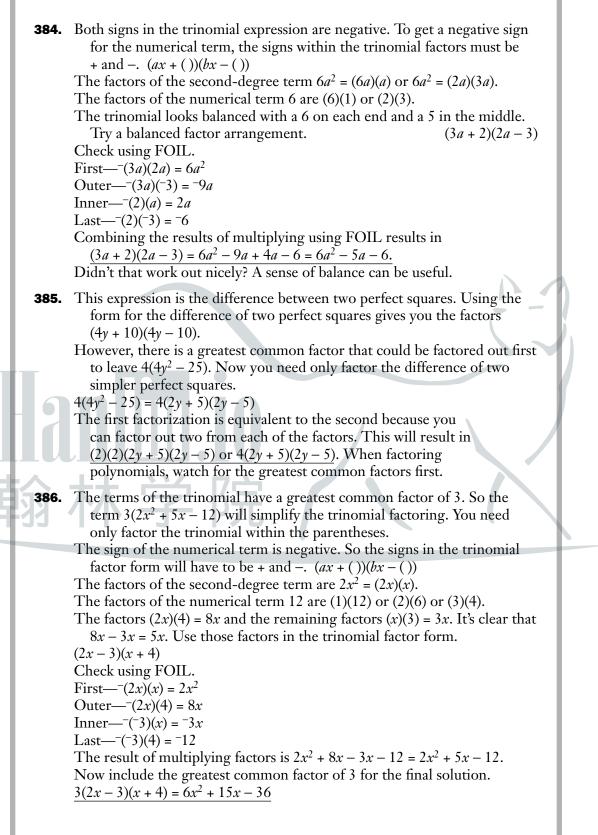
Check using FOIL.

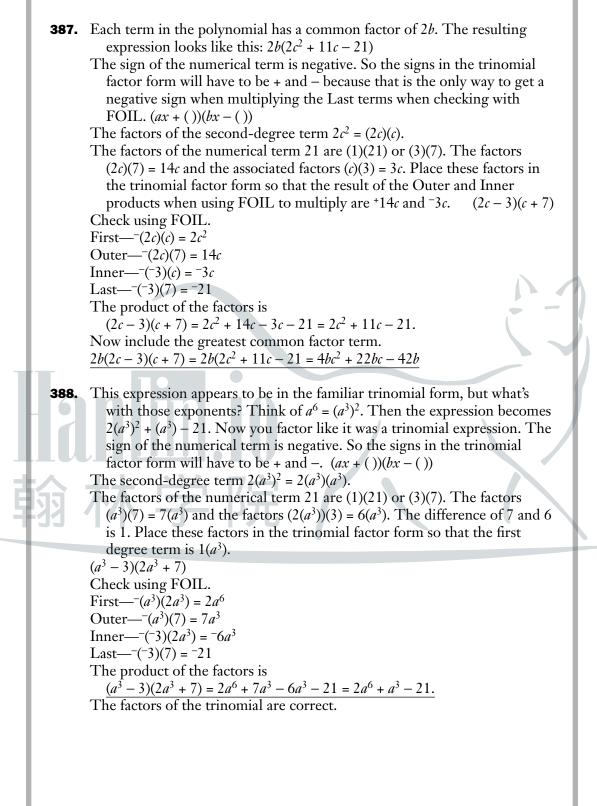
 $First - (2x)(x) = 2x^2$

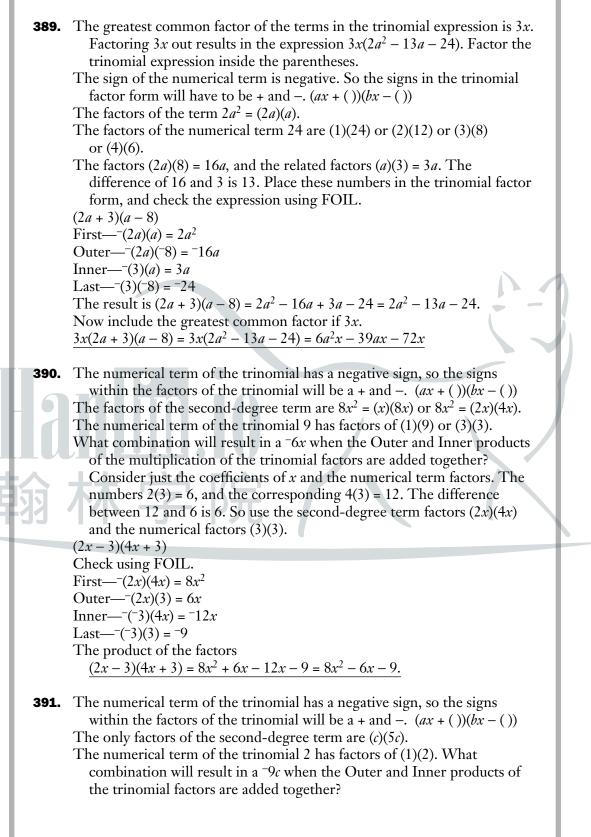


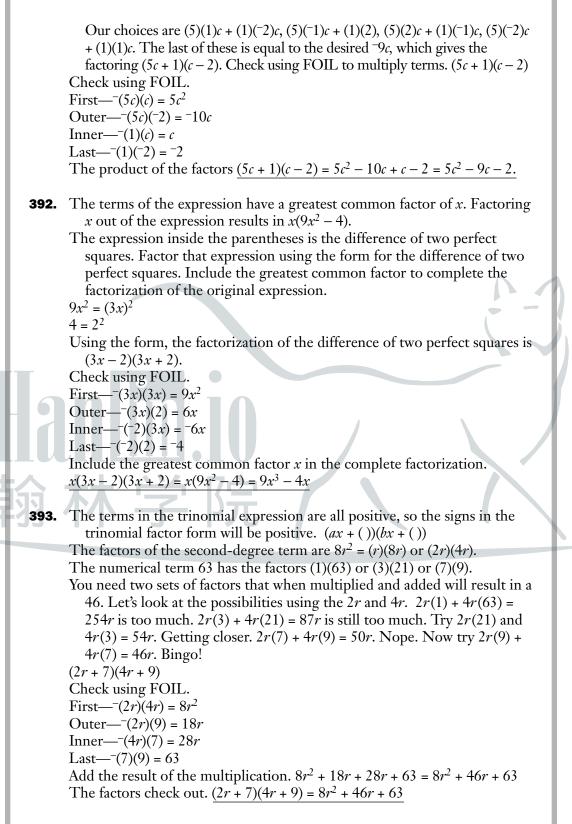
379.	Both signs in the trinomial are positive, so use positive signs in the trinomial factor form. $(ax + ())(bx + ())$ The factors of the second-degree term $9x^2 = (9x)(x)$ or $9x^2 = (3x)(3x)$. The factors of the numerical term $4 = (1)(4)$ or $4 = (2)(2)$ To get 15 <i>x</i> from adding the result of the Outer and Inner multiplications when using FOIL, place the factors in the trinomial factor form so that the product of the outer terms $(3x)(1) = 3x$ and the product of the inner terms $(4)(3x) = 12x$. Then $3x + 12x = 15x$, the middle term of the trinomial. $(3x + 4)(3x + 1)$ Check using FOIL. First— $(3x)(3x) = 9x^2$ Outer— $(4)(3x) = 12x$ Last— $(4)(1) = 4$ The factors check out. $(3x + 2)(3x + 1) = 9x^2 + 3x + 6x + 2 = 9x^2 + 9x + 2)$
380.	The sign of the numerical term is negative. So the signs in the trinomial factor form will have to be + and –. That is the only way to get a negative sign by multiplying the Last terms when checking with FOIL. $(ax + ())(bx - ())$ The factors of the second-degree term are $9x^2 = (9x)(x)$ or $9x^2 = (3x)(3x)$. The factors of the numerical term $8 = (1)(8)$ or $(2)(4)$. Let's try putting in factors in the trinomial factor form and see what we get. $(9x + 1)(x - 8)$ Using FOIL to check, we get $9x^2 - 72x + 1x - 8 = 9x^2 - 71x - 8$. No, that doesn't work. You are looking for a positive x term in the middle of the expression. Changing position of the signs would help but not with these factors because the term would be $+71x$. Try different factors
匑	of 8. $(9x-2)(x+4)$ Check using FOIL. There it is! And on only the second try. Be persistent and learn from your mistakes.
381.	The three terms have a common factor of 3. You can factor out 3 and represent the trinomial as $3(x^2 - x - 6)$. Now factor the trinomial in the parentheses, and don't forget to include the factor 3 when you are done. The sign of the numerical term is negative. So the signs in the trinomial factor form will have to be + and -, because that is the only way to get a negative sign when multiplying the Last terms when checking with FOIL. $(ax + ())(bx - ())$ The factors of the second-degree term are $3x^2 = (3x)(x)$. The sign of the second term is negative. That tells you that the result of adding the products of the Outer and Inner terms of the trinomial factors must result in a negative sum for the <i>x</i> term. The factors of the numerical term 6 are $(1)(6)$ or $(2)(3)$. Put the + with the 2 and the - with the 3. $(x + 2)(x - 3)$ Check using FOIL.
	220

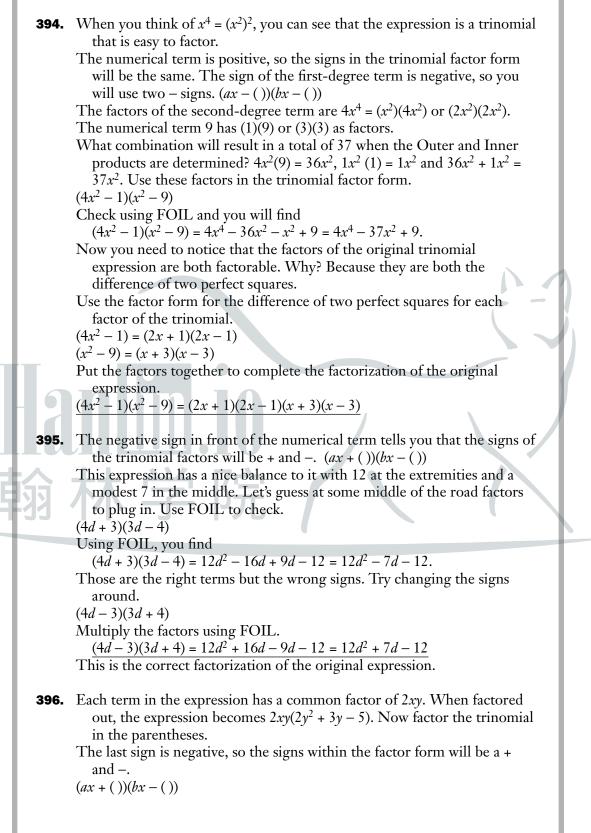
 $First - (x)(x) = x^2$ Outer—(x)(-3) = -3xInner—(2)(x) = 2xLast—(2)(-3) = -6 $(x + 2)(x - 3) = x^{2} - 3x + 2x - 6 = x^{2} - x - 6$ The factors check out. Include the common factor of 3 so that $3(x+2)(x-3) = 3(x^2 - x - 6) = 3x^2 - 3x - 18.$ Both signs in the trinomial expression are negative. To get a negative sign 382. for the numerical term, the signs within the trinomial factors must be + and -. (ax + ())(bx - ())The factors of the second-degree term $4a^2 = (4a)(a)$ or $4a^2 = (2a)(2a)$. The factors of the numerical term 9 are (1)(9) or (3)(3). The coefficient of the first-degree term is 2 less than 18. You can multiply 2a and (9) to get 18a leaving the factors 2a and (1) to get a 2a. Use this information to place factors within the trinomial factor form. (2a + 1)(2a - 9)Check using FOIL. First— $(2a)(2a) = 4a^2$ Outer—(2a)(-9) = -18aInner—(1)(2a) = 2aLast—(1)(-9) = -9The result of multiplying the factors is $(2a + 1)(2a - 9) = 4a^2 - 18a + 2a - 9 = 4a^2 - 16a - 9.$ **383.** Both signs in the trinomial expression are negative. To get a negative sign for the numerical term, the signs within the trinomial factors must be + and -. (ax + ())(bx - ())The factors of the second-degree term $6a^2 = (6a)(a)$ or (2a)(3a). The factors of the numerical term 15 are (1)(15) or (3)(5). We can predict that 13 = 18 - 5. The factors (6a)(3) = 18a. The remaining factors (a)(5) = 5a. But we need the 13 to be negative, so arrange the 6aand the (3) so their product is -18a. (6a + 5)(a - 3)Check using FOIL. $First - (6a)(a) = 6a^2$ Outer—(6a)(-3) = -18aInner—(5)(a) = 5aLast—(5)(-3) = -15Combining the results of multiplying using FOIL results in $(6a+5)(a-3) = 6a^2 - 18a + 5a - 15 = 6a^2 - 13a - 15.$ The factors check out.











The factors of the second-degree term are $2y^2 = y(2y)$. The numerical term 5 has factors (5)(1). Place the factors of the second degree and the numerical terms so that the result of the Outer and Inner multiplication of terms within the factor form of a trinomial expression results in a +3x. $(2\gamma + 5)(\gamma - 1)$ Multiply using FOIL. $(2y + 5)(y - 1) = 2y^2 - 2y + 5x - 5 = 2y^2 + 3x - 5$ The factors of the trinomial expression are correct. Now include the greatest common factor to complete the factorization of the original expression. $\frac{2xy(2y+5)(y-1) = 2xy(2y^2 - 2y + 5x - 5)}{2xy(2y^2 + 3x - 5)} = 2xy(2y^2 + 3x - 5)$ The terms of the trinomial have a greatest common factor of 2a. When 397. factored out, the resulting expression is $2a(2x^2 - 19x - 33)$. The expression within the parentheses is a trinomial and can be factored. The signs within the terms of the factor form will be + and – because the numerical term has a negative sign. Only a (+)(-) = (-). (ax + ())(bx - ())The factors of the second-degree term are $2a^2 = a(2a)$. The numerical term 33 has (1)(33) or (3)(11) as factors. Since 2a(11) = 22a, and a(3) = 3a, and 22a - 3a = 19a, use those factors in the trinomial factor form so that the result of the multiplication of the Outer and Inner terms results in -19x. (2x+3)(x-11)Check using FOIL. $(2x + 3)(x - 11) = 2x^2 - 22x + 3x - 33 = 2x^2 - 19x - 33$ The factorization of the trinomial factor is correct. Now include the greatest common factor of the original expression to get the complete factorization of the original expression. $2a(2x+3)(x-11) = 2a(2x^2 - 22x + 3x - 33) = 2a(2x^2 - 19x - 33)$ The signs within the terms of the factor form will be + and – because the 398. numerical term has a negative sign. (ax + ())(bx - ())The factors of the second-degree term are $3c^2 = c(3c)$. The numerical term 40 has (1)(40) or (2)(20) or (4)(10) or (5)(8) as factors. You want the result of multiplying and then adding the Outer and Inner terms of the trinomial factor form to result in a +19c when the like terms are combined. Using trial and error, you can determine that 3c(8) = 24c, and c(5) = 5c, and 24c - 5c = 19c. Use those factors in the factor form in such a way that you get the result you seek. $(3c-5)(c+8) = 3c^2 + 24c - 5c - 40 = 3c^2 + 19c - 40$ The complete factorization of the original expression is (3c - 5)(c + 8).

- **399.** The signs within the terms of the factor form will be + and because the numerical term has a negative sign. (ax + ())(bx ())
 - The factors of the second-degree term are $2a^2 = a(2a)$.
 - The numerical term 84 has (1)(84) or (2)(42) or (3)(28) or (4)(21) or (6)(14) or (7)(12) as factors. You want the result of multiplying and then adding the Outer and Inner terms of the trinomial factor form to result in a +17a when the like terms are combined.
 - 2a(12) = 24a, and a(7) = 7a, and 24a 7a = 17a. Use the factors 2a and a as the first terms in the factor form and use (12) and (7) as the numerical terms. Place them in position so you get the result that you want.

 $(2a-7)(a+12) = 2a^2 + 24a - 7a - 84 = 2a^2 + 17a - 84$

The complete factorization of the original expression is (2a - 7)(a + 12).

- **400.** This expression is in trinomial form. If you think of the variable as x^2 , you can see that the expression is in the trinomial form. Use x^2 where you usually put a first-degree variable. The trinomial you will be factoring looks like this: $4(x^2)^2 + 2(x^2) 30$.
 - The signs within the terms of the factor form will be + and because the numerical term has a negative sign.

(ax + ())(bx - ())

The term $(4x^2)^2$ can be factored as $(4x^2)^2 = x^2(4x^2)$ or $(2x^2)(2x^2)$.

The numerical term 30 can be factored as (1)(30) or (2)(15) or (3)(10) or (5)(6).

The factors $(4x^2)(3) = 12x^2$ and $x^2(10) = 10x^2$ will give you $12x^2 - 10x^2 = 2x^2$ when you perform the Inner and Outer multiplications and combine like terms using FOIL with the terms in the trinomial factor form. The factors of the expression will be $(4x^2 - 10)(x^2 + 3)$.

Check using FOIL.

 $(4x^2 - 10)(x^2 + 3) = 4x^4 + 12x^2 - 10x^2 - 30 = 4x^4 + 2x^2 - 30$ The expression $(4x^2 - 10)(x^2 + 3)$ is the correct factorization of the original expression. However, the first factor has a greatest common factor of 2. So a complete factorization would be $2(2x^2 - 5)(x^2 + 3)$.

Did you notice that you could have used the greatest common factor method to factor out a 2 from each term in the original polynomial? If you did, you would have had to factor the trinomial expression

 $2x^4 + x^2 - 15$ and multiply the result by the factor 2 to equal the original expression. Let's see:

 $2(2x^4 + x^2 - 15) = 2(2x^2 - 5)(x^2 + 3) = (4x^2 - 10)(x^2 + 3) = 4x^4 + 2x^2 - 30$

It all comes out the same, but if you left the factor of 2 in the term $(4x^2 - 10)$, you wouldn't have done a complete factorization of the original trinomial expression.

Solving Quadratic Equations

This chapter will give you practice in finding solutions to quadratic equations. Quadratic equations are those equations that can be written in the form $ax^2 + bx + c = 0$, where $a \neq 0$. While there are several methods for solving quadratic equations, solutions for all the equations presented here can be found by factoring.

In the previous chapter, you practiced factoring polynomials by using the greatest common factor method, the difference of two perfect squares method, and the trinomial factor method. Use these methods to factor the equations that have been transformed into quadratic equations. Then, using the zero product property (if (a)(b) = 0, then a = 0 or b = 0 or both = 0), let each factor equal zero and solve for the variable. There will be two solutions for each quadratic equation. (Ignore numerical factors such as the 3 in the factored equation 3(x + 1)(x + 1) = 0 when finding solutions to quadratic equations. The solutions will be the same for equations with or without the numerical factors.)

Find the solutions to the following quadratic equations.

401. $x^2 - 25 = 0$ **402.** $n^2 - 169 = 0$ **403.** $a^2 + 12a + 32 = 0$ **404.** $y^2 - 15y + 56 = 0$ **405.** $b^2 + b - 90 = 0$ **406.** $4x^2 = 49$ **407.** $25r^2 = 144$ **408.** $2n^2 + 20n + 42 = 0$ **409.** $3c^2 - 33c - 78 = 0$ **410.** $100r^2 = 144$ **411.** $3x^2 - 36x + 108 = 0$ **412.** $7a^2 - 21a - 28 = 0$ **413.** $8y^2 + 56y + 96 = 0$ **414.** $2x^2 + 9x = -10$ **415.** $4x^2 + 4x = 15$ **416.** $9x^2 + 12x = -4$ **417.** $3x^2 = 19x - 20$ 13字 **418.** $8b^2 + 10b = 42$ **419.** $14n^2 = 7n + 21$ **420.** $6b^2 + 20b = -9b - 20$ **421.** $15x^2 - 70x - 120 = 0$ **422.** $7x^2 = 52x - 21$ **423.** $36z^2 + 78z = -36$ **424.** $12r^2 = 192 - 40r$ **425.** $24x^2 = 3(43x - 15)$

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), { }, or [], perform operations in the innermost parentheses first and work outward.

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The solutions are <u>underlined</u>.

	401.	The expression is the difference of two perfect squares		
l		The equation factors into	(x+5)(x-5) = 0.	
l		Applying the zero product property (if $(a)(b) = 0$,		
1		then $a = 0$ or $b = 0$ or both = 0), the first factor		
l		or the second factor or both must equal zero.	(x + 5) = 0	
l		Subtract 5 from both sides of the equation.	x + 5 - 5 = 0 - 5	
l		Combine like terms on each side.	x = -5	
l		Let the second factor equal zero.	x - 5 = 0	
l		Add 5 to both sides of the equation.	x - 5 + 5 = 0 + 5	
l		Combine like terms on each side.	x = 5	
I		The solutions for the equation are $x = 5$ and $x = -5$.		
1				
1	402.	The expression is the difference of two perfect		
ł	-33	squares.		
]		The equation factors into	(n+13)(n-13) = 0.	
		Applying the zero product property (if $(a)(b) = 0$,		
l		then $a = 0$ or $b = 0$ or both $= 0$), the first factor		
l		or the second factor or both must equal zero.	(n + 13) = 0	
l		Subtract 13 from both sides of the equation.	n + 13 - 13 = 0 - 13	
l		Combine like terms on each side.	n = -13	
l		Let the second factor equal zero.	n - 13 = 0	
l		Add 13 to both sides of the equation.	n - 13 + 13 = 0 + 13	
l		Combine like terms on each side.	n = 13	
l		The solutions for the equation are $n = 13$ and $n = -13$.		
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Combine like terms on each side. $2x = -7$			
$2_{m} = -7$			
Divide both sides by 2. $\overline{2} = \overline{2}$			$\frac{2x}{2x} = \frac{7}{7}$
		Divide bour sides by 2.	$\frac{1}{2} = \frac{1}{2}$

	Simplify. Let the second factor equal zero.	$x = {}^{-3}\frac{1}{2}$ (2x - 7) = 0
	Add 7 to both sides of the equation.	2x - 7 + 7 = 0 + 7
	Combine like terms on both sides. Divide both sides by 2.	$2x = 7$ $x = 3\frac{1}{2}$
	The solutions for the quadratic equation $4x^2 = 81$ a	
	and $x = 3\frac{1}{2}$.	
407.	Transform the equation so that all terms are on one side and are equal to zero.	
	Subtract 144 from both sides.	$25r^2 - 144 = 144 - 144$
	Combine like terms on each side. The expression is the difference of two perfect squares.	$25r^2 - 144 = 0$
	The equation factors into Applying the zero product property (if $(a)(b) = 0$,	(5r+12)(5r-12) = 0.
	then $a = 0$ or $b = 0$ or both = 0), the first factor	(5r + 12) = 0
	or the second factor or both must equal zero. Subtract 12 from both sides of the equation.	(3r + 12) = 0 5r + 12 - 12 = 0 - 12
	Combine like terms on each side.	5r = -12
	Divide both sides by 5.	$\frac{5r}{5} = \frac{-12}{5}$
6	Simplify.	$r = -2\frac{2}{5}$
	Let the second factor equal zero. Add 12 to both sides of the equation.	(5r - 12) = 0 5r - 12 + 12 = 0 + 12
	Combine like terms on each side.	5r = 12 + 12 = 0 + 12 5r = 12
	Divide both sides by 5.	$\frac{5r}{5} = \frac{12}{5}$
	Simplify.	$r = 2\frac{2}{5}$
	The solution for the quadratic equation $25r^2 = 144$	$t ext{ is } r = \pm 2\frac{2}{5}.$
408.	Factor the trinomial expression using the	
	trinomial factor form.	(2n+6)(n+7) = 0
	Using the zero product property, subtract 6 from both sides.	(2n+6) = 0
	bour sides.	(2n + 6) = 0 2n + 6 - 6 = 0 - 6
	Combine like terms on each side.	2n = -6
	Divide both sides by 2.	$\frac{2n}{2} = \frac{-6}{2}$
	Simplify terms.	$n = -3^{2}$
	Let the second factor equal zero.	(n+7)=0
	Subtract 7 from both sides.	n + 7 - 7 = 0 - 7
	Combine like terms on each side. The solutions for the guadratic equation $2\pi^2 + 20\pi^2$	n = -7
	The solutions for the quadratic equation $2n^2 + 20n$ and $n = -7$.	n + +2 = 0 are $n = -3$
	and $n = /$.	

409.	Use the greatest common factor method.	$3(c^2 - 11c - 26) = 0$
	Factor the trinomial expression using the trinomial factor form.	3(c-13)(c+2) = 0
	Ignore the factor 3 in the expression.	
	Using the zero product property, add 13 to both side	es. $(c-13) = 0$
	8	c - 13 + 13 = 0 + 13
	Combine like terms on each side.	c = 13
	Let the second factor equal zero.	(c+2) = 0
	Subtract 2 from both sides.	c + 2 - 2 = 0 - 2
	Combine like terms on each side.	c = -2
	The solutions for the quadratic equation $3c^2 - 33c - 3c^2 - 3c$	
	and $c = -2$.	
410.	Transform the equation so that all terms are on	
	one side and are equal to zero.	
		$00r^2 - 144 = 144 - 144$
		$00r^2 - 144 = 0$
	The expression is the difference of two	
	perfect squares.	
		(0r + 12)(10r - 12) = 0.
- C	Applying the zero product property (if $(a)(b) = 0$,	
	then $a = 0$ or $b = 0$ or both = 0), the first factor	
	·	10r + 12) = 0
		0r + 12 - 12 = 0 - 12
		0r = -12
	Divide both sides by 10. $\frac{10}{10}$	$\frac{0r}{0} = \frac{-12}{10} = \frac{-6}{5}$
$\mathbf{\Lambda}$	Simplify terms.	$= -1\frac{1}{5}$
17		
XX		(0r - 12) = 0
	1	0r - 12 + 12 = 0 + 12
		0r = 12
	Divide both sides by 10. $\frac{10}{1}$	$\frac{0r}{0} = \frac{12}{10} = \frac{6}{5}$
	Simplify terms. r	$=1\frac{1}{5}$
	The solution for the quadratic equation $100r^2 = 144$	
	The solution for the quadratic equation $100r^2 = 144$	$15 \ r = -1 \frac{1}{5}.$
411.	Use the greatest common factor method.	$3(x^2 - 12x + 36) = 0$
	Factor the trinomial expression using the trinomial	
	factor form.	3(x-6)(x-6) = 0
	Ignore the factor 3 in the expression.	
	Using the zero product property, add 6 to both sides	(x-6) = 0
	e shing the zero product property, and o to both sides	x - 6 + 6 = 0 + 6
	Combine like terms on each side.	$\begin{array}{c} x = 0 + 0 = 0 + 0 \\ x = 6 \end{array}$
	Since both factors of the trinomial expression are the	
	for the quadratic equation $3x^2 - 36x + 108 = 0$ is $x =$	
	101 the quadratic equation $J_{\lambda} = J_{0\lambda} + 100 = 0.18 \lambda = 1$	U .

412.	Use the greatest common factor method.	$7(a^2 - 3a - 4) = 0$		
	Factor the trinomial expression using the trinomial	· · ·		
	factor form.	7(a-4)(a+1) = 0		
	Ignore the factor 7 in the expression.			
	Using the zero product property, add 4 to both sides.			
		a - 4 + 4 = 0 + 4		
	Combine like terms on each side.	<i>a</i> = 4		
	Let the second factor equal zero.	(a+1)=0		
	Subtract 2 from both sides.	a + 1 - 1 = 0 - 1		
	Combine like terms on each side.	a = -1		
	The solutions for the quadratic equation $7a^2 - 21a - 70 = 0$ are $a = -2$			
	and $a = 5$.			
413	Use the greatest common factor method.	$8(y^2 + 7y + 12) = 0$		
713.	Factor the trinomial expression using the trinomial	0(y + iy + 12) = 0		
	factor form.	8(y+4)(y+3) = 0		
	Ignore the factor 8 in the expression.	0(y + 1)(y + 5) = 0		
	Using the zero product property, subtract 4 from			
	both sides.	(y+4)=0		
	both sides.	y + 4 - 4 = 0 - 4		
	Combine like terms on each side.	y = -4		
TT	Let the second factor equal zero.	(y+3) = 0		
	Subtract 3 from both sides.	y + 3 - 3 = 0 - 3		
	Simplify.	y = -3		
	The solutions for the quadratic equation $8y^2 + 56y + y^2$			
	and $y = -3$.	<u> </u>		
414.	Transform the equation into the familiar trinomial			
	equation form.	$2x^2 + 9x + 10 = -10 + 10$		
LOO -		$2x^{2} + 9x + 10 = 10 + 10$ $2x^{2} + 9x + 10 = 0$		
	Factor the trinomial expression using the trinomial	2x + 9x + 10 = 0		
	1 0	(2x+5)(x+2) = 0		
	Using the zero product property, subtract 5 from	(2x + 3)(x + 2) = 0		
		(2x+5)=0		
		2x + 5 - 5 = 0 - 5		
		$2x = 5^{-5}$		
	Divide both sides by 2.	$\frac{2x}{2} = \frac{-5}{2}$		
	Simplify terms.	$x = -2\frac{1}{2}$		
	Let the second term equal zero.	x + 2 = 0		
		x + 2 - 2 = 0 - 2		
		x = -2		
	The solutions for the quadratic equation $2x^2 + x = 10$) are $x = -2\frac{1}{2}$		
	and $x = -2$.	<u> </u>		

	501 Algebra Questions	
415.	 Transform the equation into the familiar trinomial equation form. Subtract 15 from both sides of the equation. Combine like terms on each side. Factor the trinomial expression using the trinomial factor form. Using the zero product property, subtract 5 from both sides. Simplify. 	$4x^{2} + 4x - 15 = 15 - 15$ $4x^{2} + 4x - 15 = 0$ (2x - 3)(2x + 5) = 0 (2x + 5) = 0 2x + 5 - 5 = 0 - 5 2x = -5
	Divide both sides by 2.	$\frac{2x}{2} = \frac{-5}{2}$
416.	Simplify terms. Let the second factor equal zero. Add 3 to both sides. Simplify. Divide both sides by 2. Simplify terms. The solutions for the quadratic equation $4x^2 + 4x$ and $x = 1\frac{1}{2}$. Transform the equation into the familiar trinomial equation form. Add 4 to both sides of the equation. Combine like terms on each side. Factor the trinomial expression using the trinom factor form. Using the zero product property, subtract 2 from both sides.	$9x^{2} + 12x + 4 = ^{-}4 + 4$ $9x^{2} + 12x + 4 = 0$ ial (3x + 2)(3x + 2) = 0
	Simplify.	3x = -2
	Divide both sides by 3. Simplify terms. Since both factors of the trinomial are the same, <u>quadratic equation $9x^2 + 12x = -4$ is $x = \frac{-2}{3}$.</u>	$\frac{3x}{3} = \frac{-2}{3}$ $x = \frac{-2}{3}$ the solution to the
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417.	Transform the equation into the familiar trinomial equation form. Subtract $19x$ from both sides. Combine like terms. Add 20 to both sides. Combine like terms on each side. Factor the trinomial expression using the trinomial factor form. Using the zero product property, add 4 to both sides. Simplify. Divide both sides by 3. Simplify terms. Now let the second term equal zero. Add 5 to both sides. Simplify. The solutions for the quadratic equation $3x^2 = 1$	$3x^{2} - 19x = 19x - 19x - 20$ $3x^{2} - 19x = -20$ $3x^{2} - 19x + 20 = -20 + 20$ $3x^{2} - 19x + 20 = 0$ (3x - 4)(x - 5) = 0 (3x - 4) = 0 3x - 4 + 4 = 0 + 4 3x = 4 $\frac{3x}{3} = \frac{4}{3}$ $x = 1\frac{1}{3}$ x - 5 = 0 x - 5 + 5 = 0 + 5 x = 5 $19x - 20 \text{ are } x = 1\frac{1}{3}$		
	 and x = 5. Transform the equation into the familiar trinomial equation form. Subtract 42 from both sides of the equation. Simplify. Use the greatest common factor method to factor out 2. Factor the trinomial expression using the trinomial factor form. Ignore the factor 2 in the expression. Using the zero product property, add 7 to both sides. Simplify. 	$8b^{2} + 10b - 42 = 42 - 42$ $8b^{2} + 10b - 42 = 0$ $2(4b^{2} + 5b - 21) = 0$ 2(4b - 7)(b + 3) = 0 (4b - 7) = 0 4b - 7 + 7 = 0 + 7 4b = 7		
	Divide both sides by 4. Simplify terms. Now let the second term equal zero. Subtract 3 from both sides. Simplify. The solutions for the quadratic equation $8b^2 + 1$ and $b = -3$.	$\frac{4b}{4} = \frac{7}{4}$ $b = 1\frac{3}{4}$ (b + 3) = 0 b + 3 - 3 = 0 - 3 b = -3		

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419.	Transform the equation into the familiar trinomial equation form.	
	Subtract $7n$ from both sides of the equation.	$14n^2 - 7n = 7n - 7n + 21$
	Simplify and subtract 21 from both sides.	$14n^2 - 7n - 21 = 21 - 21$
	Simplify the equation.	$14n^2 - 7n - 21 = 0$
	Factor the greatest common factor from	
	each term.	$7(2n^2 - n - 3) = 0$
	Factor the trinomial expression using the	,(211 11 3)) 0
	trinomial factor form.	7(2n-3)(n+1) = 0
	Ignore the factor 7 in the expression.	
	Using the zero product property, add 3 to	
	both sides.	(2n-3) = 0
		2n - 3 + 3 = 0 + 3
	Simplify.	2n = 3
	Divide both sides by 2.	$\frac{2n}{2} = \frac{3}{2}$
	Simplify terms.	$n = 1\frac{1}{2}$
	Now set the second equal to zero.	n + 1 = 0
	Subtract 1 from both sides.	n + 1 - 1 = 0 - 1
	Simplify.	n = 1
	The solutions for the quadratic equation 14n	$n^2 = 7n + 21$ are $n = 1\frac{1}{2}$
6	and $n = \overline{1}$.	
420,	Transform the equation into the familiar	
	trinomial equation form.	
	Add $9b$ to both sides of the equation.	$6b^2 + 20b + 9b = -9b + 9b - 20$
	Simplify and add 20 to both sides of the	
77	equation.	$6b^2 + 29b + 20 = 20 - 20$
	Simplify.	$6b^2 + 29b + 20 = 0$
	Factor the trinomial expression using the	
	trinomial factor form.	(6b + 5)(b + 4) = 0
	Using the zero product property, subtract 5	
	from both sides.	(6b+5) = 0
		6b + 5 - 5 = 0 - 5
	Simplify.	6b = -5
	Divide both sides by 6.	$\frac{6b}{6} = \frac{-5}{6}$
	Simplify terms.	$b = \frac{-5}{6}$
	Now set the second factor equal to zero.	b + 4 = 0
	Subtract 4 from both sides.	b + 4 - 4 = 0 - 4
	Simplify.	<i>b</i> = ⁻ 4
	The solutions for the quadratic equation $6b^2$	+20b = -9b - 20 are
	$b = \frac{-5}{6}$ and $b = -4$.	
	v = 6 and $v = 1$.	

421.	Factor the greatest common factor from	
	each term. Now factor the trinomial expression using the	$5(3x^2 - 14x - 24) = 0$
	trinomial factor form.	5(3x+4)(x-6) = 0
	Using the zero product property, subtract 4 from	
	both sides.	(3x + 4) = 0 3x + 4 - 4 = 0 - 4
	Simplify.	3x + 1 = 1 = 0 = 1 3x = -4
	Divide both sides by 3.	$\frac{3x}{3} = \frac{-4}{3}$
	Simplify terms.	$x = \frac{-4}{3}$
	Add 6 to both sides.	x - 6 + 6 = 0 + 6
	Simplify.	x = 6
	The solutions for the quadratic equation $15x^2 - \frac{1}{2}$	-70x - 120 = 0 are
	$x = \frac{4}{3}$ and $x = 6$.	
422.	Transform the equation into the familiar trinomial equation form.	
	Subtract $52x$ from both sides of the equation.	$7x^2 - 52x = 52x - 52x - 21$
E de	Simplify and add 21 to both sides of the	$7x^2 - 52x + 21 = 21 - 21$
	equation. Simplify.	$7x^2 - 52x + 21 = 21 - 21$ $7x^2 - 52x + 21 = 0$
	Factor the trinomial expression using the	
	trinomial factor form.	(7x-3)(x-7) = 0
	Using the zero product property, add 3 to both sides.	(7w - 3) = 0
		(7x-3) = 07x-3+3 = 0+3
	Simplify.	7x = 3
	Divide both sides by 7.	$\frac{7x}{7} = \frac{3}{7}$
	Simplify terms.	$\mathcal{X} = \frac{3}{7}$
	Now set the second factor equal to zero.	x - 7 = 0
	Add 7 to both sides of the equation.	x - 7 + 7 = 0 + 7
	Simplify. The solutions for the quadratic equation $7x^2 = 5$	x = 7 52r - 21 are $r = \frac{3}{7}$
	and $x = 7$.	$\frac{1}{2}$
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 $\frac{-4}{3}$

501 Algebra Questions 423. Transform the equation into the familiar trinomial equation form. $36z^2 + 78z + 36 = -36 + 36$ Add 36 to both sides of the equation. $36z^2 + 78z + 36 = 0$ Combine like terms. Factor out the greatest common factor from $6(6z^2 + 13z + 6) = 0$ each term. Factor the trinomial expression into two factors. 6(2z+3)(3z+2) = 0Ignore the numerical factor and set the first (2z + 3) = 0factor equal to zero. 2z + 3 - 3 = 0 - 3Subtract 3 from both sides. Simplify terms. 2z = -3 $\frac{2z}{2} = \frac{-3}{2}$ Divide both sides by 2. $z = -1\frac{1}{2}$ Simplify terms. (3z + 2) = 0Now let the second factor equal zero. Subtract 2 from both sides. 3z + 2 - 2 = 0 - 23z = -2Simplify terms. $\frac{3z}{3} = \frac{-2}{3}$ Divide both sides by 3. $z = \frac{-2}{2}$ Simplify terms. The solutions for the quadratic equation $36z^2 + 78z = -36$ are $z = -1\frac{1}{2}$ and $z = \frac{-2}{3}$. **424.** Transform the equation into the familiar trinomial equation form. Add (40r - 192) to both sides $12r^2 + 40r - 192 = 192 - 40r + 40r - 192$ of the equation. $12r^2 + 40r - 192 = 0$ Combine like terms. Factor the greatest common factor, 4, out of each term. $4(3r^2 + 10r - 48) = 0$ Now factor the trinomial expression. 4(r+6)(3r-8) = 0Ignoring the numerical factor, set one factor equal to zero. (r + 6) = 0Subtract 6 from both sides. r + 6 - 6 = 0 - 6Simplify. r = -6Now set the second factor 3r - 8 = 0equal to zero. 3r - 8 + 8 = 0 + 8Add 8 to both sides. 3r = 8Simplify. $\frac{3r}{3} = \frac{8}{3}$ Divide both sides by 3. $r = 2\frac{2}{3}$ Simplify terms. The solutions for the quadratic equation $12r^2 = 192 - 40r$ are r = -6and $r = 2\frac{2}{3}$.

425.	 Divide both sides of the equation by 3. Simplify terms. Add (15 - 43x) to both sides of the equation. Combine like terms. Use the commutative property to move terms. Factor the trinomial expression. Using the zero product property, add 3 to both sides and divide by 8. 	$\frac{24x^2}{3} = \frac{3(43x - 15)}{3}$ $8x^2 = 43x - 15$ $8x^2 + 15 - 43x = 43x - 15 + 15 - 43x$ $8x^2 + 15 - 43x = 0$ $8x^2 - 43x + 15 = 0$ (8x - 3)(x - 5) = 0 8x - 3 = 0 $\frac{8x}{8} = \frac{3}{8}$	
	Simplify terms.	$x = \frac{3}{8}$	
	Now let the second factor equal zero	0	
	Add 5 to both sides.	<i>x</i> = 5	
	The solutions for the quadratic equa	$\frac{1}{100} \frac{24x^2}{4x^2} = 3(43x - 15) \text{ are}$	ĺ,
	$x = \frac{3}{8}$ and $x = 5$.		
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J.B Simplifying Radicals

This chapter will give you practice in operating with radicals. You will not always be able to factor polynomials by factoring whole numbers and whole number coefficients. Nor do all trinomials with whole numbers have whole numbers for solutions. In these last chapters, you will need to know how to operate with radicals.

The radical sign $\sqrt{}$ tells you to find the root of a number. The number under the radical sign is called the *radicand*. Generally, a number has two roots, one positive and one negative. It is understood in mathematics that $\sqrt{}$ or $\sqrt{}$ is telling you to find the positive root. The symbol $\sqrt{}$ tells you to find the negative root. The symbol $\sqrt{}$ asks for both roots.

Tips for Simplifying Radicals

Simplify radicals by completely factoring the radicand and taking out the square root. The most thorough method for factoring is to do a prime factorization of the radicand. Then you look for square roots that can be factored out of the radicand.

e.g.,
$$\sqrt{28} = \sqrt{2 \cdot 2 \cdot 7} = \sqrt{2 \cdot 2} \cdot \sqrt{7} = 2\sqrt{7}$$

or $\sqrt{4x^3} = \sqrt{2 \cdot 2 \cdot x \cdot x \cdot x} = \sqrt{2 \cdot 2} \cdot \sqrt{x \cdot x} \cdot \sqrt{x} = 2x\sqrt{x}$

You may also recognize perfect squares within the radicand. Then you can simplify their roots out of the radical sign.

It is improper form for the radicand to be a fraction. If you get rid of the denominator within the radical sign, you will no longer have a fractional radicand. This is known as *rationalizing* the denominator.

e.g.,
$$\sqrt{\frac{2x}{5}} = \sqrt{\frac{2x}{5} \cdot \frac{5}{5}} = \sqrt{\frac{10x}{5^2}} = \sqrt{\frac{1}{5^2} \cdot 10x} = \frac{1}{5}\sqrt{10x}$$

When there is a radical in the denominator, you can rationalize the expression as follows:

$$\frac{3}{\sqrt{6}} = \frac{3}{\sqrt{6}} \cdot \frac{\sqrt{6}}{\sqrt{6}} = \frac{3\sqrt{6}}{6} = \frac{1}{2}\sqrt{6}$$

If the radicands are the same, radicals can be added and subtracted as if the radicals were variables.

e.g.,
$$3\sqrt{3} + 2\sqrt{3} = 5\sqrt{3}$$
 or $5\sqrt{x} - 2\sqrt{x} = 3\sqrt{x}$

Product property of radicals

When multiplying radicals, multiply the terms in front of the radicals, then multiply the radicands and put that result under the radical sign.

e.g.,
$$4\sqrt{3} \cdot 7\sqrt{5} = 4 \cdot 7\sqrt{3 \cdot 5} = 28\sqrt{15}$$

Quotient property of radicals

When dividing radicals, first divide the terms in front of the radicals, and then divide the radicands.

e.g.,
$$\frac{6\sqrt{10}}{3\sqrt{2}} = \frac{6}{3}\sqrt{\frac{10}{2}} = 2\sqrt{5}$$

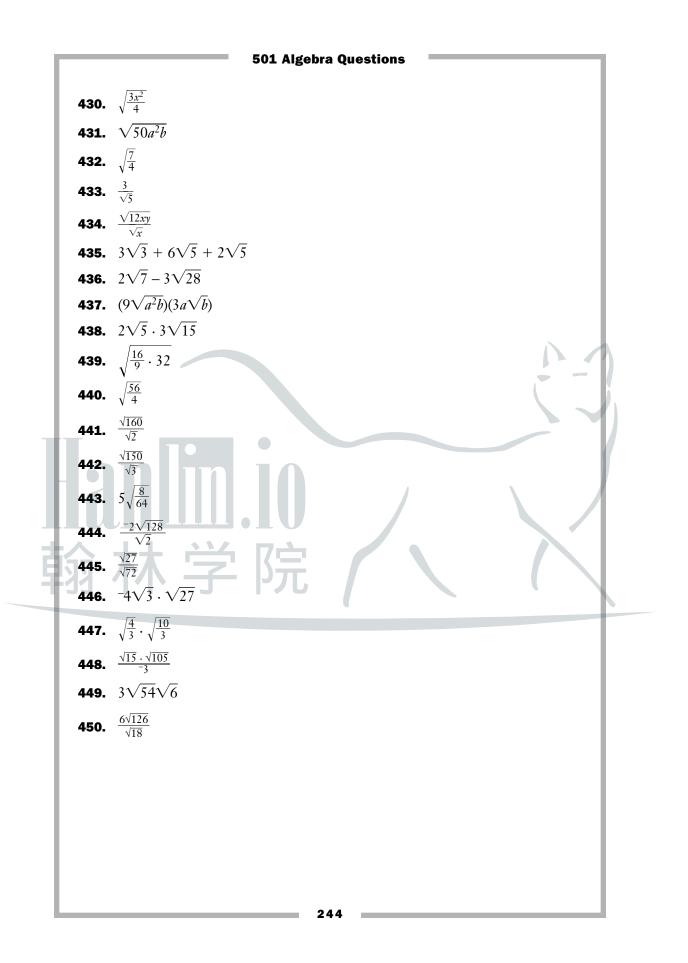
Simplify the following radical expressions.

426.
$$\sqrt{12}$$

427. $\sqrt{500}$

428.
$$\sqrt{3n^2}$$

429.
$$\sqrt{24x^5}$$



Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), {}, or [], perform operations in the innermost parentheses first and work outward.

<u>Underlined</u> expressions show simplified result.

426. First, factor the radicand. Now take out the square root of any pair of factors or any perfect squares you recognize.

- **427.** First, factor the radicand.
 - Now take out the square root.
- **428.** First, factor the radicand. Now take out the square root.
- **429.** First, factor the radicand and look for squares. Now take out the square root.

 $\sqrt{3n^2} = \sqrt{3 \cdot n \cdot n}$ $\frac{\sqrt{3 \cdot n \cdot n} = n\sqrt{3}}{\sqrt{24x^5}} = \sqrt{6 \cdot 2 \cdot 2 \cdot x \cdot x \cdot x \cdot x \cdot x}$

$$\sqrt{6 \cdot 2 \cdot 2 \cdot x \cdot x \cdot x \cdot x \cdot x} = 2x \cdot x\sqrt{6x} = 2x^2\sqrt{6x}$$

430. Although it looks complex, you can still begin by factoring the terms in the radical sign.

Factoring out the squares leaves

This result can be written a few different ways.

431. First, factor the radicand and look for squares.

Take out the square roots.

$$\sqrt{\frac{3x^2}{4}} = \sqrt{\frac{3 \cdot x \cdot x}{2 \cdot 2}} = \sqrt{3 \cdot \frac{x \cdot x}{2 \cdot 2}}$$
$$\sqrt{3 \cdot \frac{x \cdot x}{2 \cdot 2}} = \frac{x}{2}\sqrt{3}.$$

 $\sqrt{12} = \sqrt{2 \cdot 2 \cdot 3}$

 $\sqrt{2 \cdot 2 \cdot 3} = 2\sqrt{3}$

 $\sqrt{500} = \sqrt{5 \cdot 10 \cdot 10}$

 $\sqrt{5 \cdot 10 \cdot 10} = 10\sqrt{5}$

$$\frac{\frac{x}{2}\sqrt{3}}{\frac{1}{2}} = \frac{\sqrt{3}x}{\frac{1}{2}} = \frac{\sqrt{3}}{2}x = \frac{1}{2}x\sqrt{3}$$

$$\sqrt{50a^2b} = \sqrt{2} \cdot 5 \cdot 5 \cdot a \cdot a \cdot b$$
$$\sqrt{2 \cdot 5 \cdot 5 \cdot a \cdot a \cdot b} = 5a\sqrt{2b}$$

432.	Use the quotient property of radicals and rationalize the denominator.	$\sqrt{\frac{7}{4}} = \frac{\sqrt{7}}{\sqrt{4}} = \frac{\sqrt{7}}{\sqrt{2 \cdot 2}} = \frac{\sqrt{7}}{2}$
433.	For this expression, you must rationalize the denominator. Use the identity property of multiplication and multiply the expression by 1 in a form useful for your purposes. In this case, that is to get the radical out of the denominator.	$\frac{3}{\sqrt{5}} = \frac{3}{\sqrt{5}} \frac{\sqrt{5}}{\sqrt{5}} = \frac{3\sqrt{5}}{5}$
434.	First, rationalize the denominator for this expression. Then see if it can be simplified any further. As in the previous problem, multiply the expression by 1 in a form suitable for this purpose.Use the product property of radicals to combine the radicands in the numerator. In the denominator, a square root times itself is the radicand by itself.	$\frac{\sqrt{12xy}}{\sqrt{x}} = \frac{\sqrt{12xy}}{\sqrt{x}} \cdot \frac{\sqrt{x}}{\sqrt{x}}$ $\frac{\sqrt{12xy}}{\sqrt{x}} \cdot \frac{\sqrt{x}}{\sqrt{x}} = \frac{\sqrt{12xyx}}{x}$
r i	Now factor the radicand.	$\frac{\sqrt{12xyx}}{x} = \frac{\sqrt{3 \cdot 4x^2y}}{x}$
9	Factoring out the square roots results in The <i>x</i> in the numerator and the denominator divides out, leaving	$\frac{\sqrt{3} \cdot 4x^2 y}{x} = \frac{2x\sqrt{3y}}{x}.$ $\frac{2\sqrt{3y}}{x}.$
435.	In this expression, add the "like terms" as if the similar radicals were similar variables. $3\sqrt{3} + 6$ The radical terms cannot be added further because the radicands are different.	$5\sqrt{5} + 2\sqrt{5} = 3\sqrt{3} + 8\sqrt{5}$
436.	.,	$-3\sqrt{28} = 2\sqrt{7} - 3\sqrt{4 \cdot 7}$ $3\sqrt{4 \cdot 7} = 2\sqrt{7} - 3 \cdot 2\sqrt{7}$ $2\sqrt{7} - 6\sqrt{7} = -4\sqrt{7}$
437.	For this expression, use the product property of radicals and combine the factors in the radicand and outside the radical signs. $(9\sqrt{a^2b})(3a\sqrt{b}) = 9 \cdot 3a\sqrt{a^2b \cdot b} = 2^{2}$	
438.	Use the product property of radicals to simplify the expression. 2	$\sqrt{5} \cdot 3\sqrt{15} = 2 \cdot 3\sqrt{5 \cdot 15}$

	SOT Algebia Questions
	Now look for a perfect square in the radicand. You can multiply and then factor or just factor first. $6\sqrt{5 \cdot 15} = 6\sqrt{75} = 6\sqrt{25 \cdot 3} = 6 \cdot 5\sqrt{3} = 30\sqrt{3}$ Or if you just factor the radicand, you will see the perfect square as 5 times 5. $6\sqrt{5 \cdot 15} = 6\sqrt{5 \cdot 5 \cdot 3} = 6 \cdot 5\sqrt{3} = 30\sqrt{3}$
439.	You can start by using the product property to simplify the expression. Now use the quotient property to simplify the first radical. You should recognize the perfect squares 9 and 16. Simplify the fraction and factor the radicand of the second radical term. $\frac{\sqrt{16}}{\sqrt{9}} \cdot \sqrt{32} = \frac{\sqrt{16}}{\sqrt{9}} \cdot \sqrt{32}$
440.	Use the quotient property to get the denominator out of the radicand. Now simplify the radicand by factoring so that any perfect squares will come out of the radical sign. The common factor in both the numerator and denominator divides out, and you are left with $\frac{\sqrt{56}}{2} = \frac{\sqrt{4 \cdot 14}}{2} = \frac{2\sqrt{14}}{2}$
41.	For this term, factor the radicand in the numerator and look for perfect squares. $\frac{\sqrt{160}}{\sqrt{2}} = \frac{\sqrt{4 \cdot 4 \cdot 2 \cdot 5}}{\sqrt{2}} = \frac{4\sqrt{2 \cdot 5}}{\sqrt{2}}$ Use the product property in the numerator. Divide out the common factor in the numerator and the denominator. $\frac{4\sqrt{2} \cdot \sqrt{5}}{\sqrt{2}} = 4\sqrt{5}$
442.	You could proceed in the same way as the previous solution, but let's try another way. Rationalize the denominator. $\sqrt{150}$ $\sqrt{3}$ $\sqrt{3}$ $\sqrt{3}$ $\sqrt{150} \cdot \sqrt{3}$ $\sqrt{3}$ $\sqrt{150} \cdot \sqrt{3}$
	numerator and denominator and you're done. $\frac{5 \cdot 3\sqrt{2}}{3} = 5\sqrt{2}$

112	You use the quotient property to begin
773.	rationalizing the denominator. $5\sqrt{\frac{8}{64}} = 5\frac{1}{2}$
	The 5 becomes part of the numerator. Factor
	the numerator and simplify the perfect square $\sqrt{8}$
	in the denominator. $5\frac{\sqrt{8}}{\sqrt{64}} = \frac{5\sqrt{4}}{8}$
	Simplify the numerator. $\frac{5\sqrt{4\cdot 2}}{8} = \frac{5\cdot 2}{8}$
	Factor 2 out of the numerator and denominator. $\frac{5 \cdot 2\sqrt{2}}{8} = \frac{5}{8}$
444.	Begin simplifying this term by rationalizing the denominator. $\frac{-2\sqrt{128}}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{-2 \cdot \sqrt{128}}{\sqrt{2} \cdot \sqrt{2}}$
	denominator. $\frac{-2\sqrt{128}}{\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{-2\sqrt{128}}{\sqrt{2}} \cdot \sqrt{2}$
	Using the product property, simplify the numerator and write the product of the
	term in the denominator. $\frac{-2 \cdot \sqrt{128} \cdot \sqrt{2}}{\sqrt{2} \cdot \sqrt{2}} = \frac{-2 \cdot \sqrt{128}}{2}$
	Divide out the common factor in the numerator $\sqrt{2 \cdot \sqrt{2}}$
	and denominator. Then factor the
	radicand looking for perfect squares. $\frac{-2\sqrt{128}}{2} = -\sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2} = -2 \cdot 2 \cdot 2 = -2 \cdot 2 = -2 \cdot 2 \cdot 2 = -2 \cdot 2 = -2 \cdot 2 \cdot$
445.	You will have to rationalize the denominator,
	but first factor the radicands and look for
6	perfect squares. $\frac{\sqrt{27}}{\sqrt{72}} = \frac{\sqrt{9 \cdot 3}}{\sqrt{36 \cdot 2}} = -$
	You can simplify the whole numbers in the numerator and denominator by a factor of 3. $\frac{3\sqrt{3}}{6\sqrt{2}} = -\frac{3\sqrt{3}}{6\sqrt{2}}$
	Now rationalize the denominator. $\frac{\sqrt{3}}{2\sqrt{2}} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \frac{\sqrt{3}}{2} \cdot \frac{\sqrt{3}}{\sqrt{2}}$
	Simplify terms by using the product property
	in the numerator and multiplying terms $\sqrt{3}$, $\sqrt{2}$, $\sqrt{3+2}$
1.7	in the denominator. $\frac{\sqrt{3} \cdot \sqrt{2}}{2 \cdot \sqrt{2} \cdot \sqrt{2}} = \frac{\sqrt{3} \cdot 2}{2 \cdot 2} =$
446.	Factor the radicand in the last radical. $-4\sqrt{3} \cdot \sqrt{27} = -4\sqrt{3} \cdot \sqrt{9}$
	Simplify the perfect square. $-4\sqrt{3} \cdot \sqrt{9 \cdot 3} = -4\sqrt{3} \cdot 3^{-1}$
	Use the commutative property of
	multiplication. $-4\sqrt{3} \cdot 3\sqrt{3} = -4 \cdot 3 \cdot \sqrt{3} \cdot 7$
	Now simplify terms. $-4 \cdot 3 \cdot \sqrt{3} \cdot \sqrt{3} = -12 \cdot 3 = \frac{1}{2}$
447.	Using the product property, put all terms $\sqrt{4}$ $\sqrt{10}$ $\sqrt{4}$
	in one radical sign. $\sqrt{\frac{4}{3}} \cdot \sqrt{\frac{10}{3}} = \sqrt{\frac{4}{3}}$
	Now use the quotient property to continue simplifying. $\sqrt{\frac{4 \cdot 10}{3 \cdot 3}} = \frac{\sqrt{4}}{\sqrt{3}}$
	Simplify the perfect squares in the numerator
	and denominator. $\frac{\sqrt{4 \cdot 10}}{\sqrt{9}} = \frac{2}{\sqrt{10}}$
	The expression is fine the way it is,
	or it could be written as $\frac{2}{3}$

448. Begin by factoring the radicand of the second radical. $\sqrt{15 \cdot \sqrt{105}} = \sqrt{15 \cdot \sqrt{15 \cdot 7}}$ Now use the product property to separate the factors of the second radical term into two radical terms. Why? Because you will then have the product of two identical radicals. $\sqrt{15 \cdot \sqrt{15 \cdot 7}} = \sqrt{15 \cdot \sqrt{15 \cdot 7}} = \frac{\sqrt{15 \cdot \sqrt{15 \cdot 7}}}{3} = \frac{15\sqrt{7}}{3}$ Now simplify the whole numbers. $\sqrt{15 \cdot \sqrt{15 \cdot 7}} = \sqrt{15 \cdot \sqrt{15 \cdot 7}} = \frac{\sqrt{15 \cdot \sqrt{15 \cdot 7}}}{3} = \frac{15\sqrt{7}}{3}$ 449. There is more than one way to simplify an expression. Start this one by using the product property to combine the radicands. $\frac{15\sqrt{7}}{3} = -5\sqrt{7}$ 449. There is more than one way to simplify an expression. Start this one by using the product property to combine the radicands. $\frac{15\sqrt{7}}{3} = -5\sqrt{7}$ 449. There is more than one way to simplify an expression. Start this one by using the product property to combine the radicands. $3\sqrt{54\sqrt{6}} = 3\sqrt{54\sqrt{6}} = 3\sqrt{54 \cdot 6}$ Now factor the terms in the radicand and look for perfect squares. $3\sqrt{54 \cdot 6} = 3\sqrt{9 \cdot 6 \cdot 6} = 3\sqrt{3 \cdot 3 \cdot 6 \cdot 6}$ Simplify the radical. $3\sqrt{54 \cdot 6} = 3\sqrt{9 \cdot 6 \cdot 6} = 3\sqrt{3 \cdot 3 \cdot 6 \cdot 6}$ Simplify the radical. $3\sqrt{54 \cdot 6} = 3\sqrt{3 \cdot 3 \cdot 6 \cdot 6} = \frac{3\sqrt{3 \cdot 3 \cdot 6 \cdot 6}}{18}$ 450. Begin by rationalizing the denominator. Use the product property to simplify the numerator. $\frac{6\sqrt{126} \cdot \sqrt{18}}{18} = \frac{6\sqrt{126 \cdot 18}}{18}$ Simplify the whole numbers in the numerator and denominator. Then factor the radicand and look for perfect squares. $\frac{6\sqrt{126 \cdot 18}}{18} = \frac{\sqrt{9 \cdot 9 \cdot 2 \cdot 2 \cdot 7}}{3} = \frac{\sqrt{9 \cdot 9 \cdot 2 \cdot 2 \cdot 7}}{3}$ Simplify the numerator and divide out common factors in the numerator and denominator. $\sqrt{$		501 Algebra Questions
identical radicals. Now simplify the whole numbers. 449. There is more than one way to simplify an expression. Start this one by using the product property to combine the radicands. Now factor the terms in the radicand and look for perfect squares. 3 $\sqrt{54} \sqrt{6} = 3\sqrt{54 \cdot 6}$ Simplify the radical. Another way is to multiply 6 and 54 to get 324, another perfect square. Then 3 times 18 equals 54. 450. Begin by rationalizing the denominator. Use the product property to simplify the numerator. Simplify the whole numbers in the numerator and denominator. Then factor the radicand and look for perfect squares. Simplify the numerator and divide out common factors in the out common factors in the	448.	second radical. Now use the product property to separate the factors of the second radical term into two radical terms. Why? Because
449. There is more than one way to simplify an expression. Start this one by using the product property to combine the radicands. Now factor the terms in the radicand and look for perfect squares. Simplify the radical. Another way is to multiply 6 and 54 to get 324, another perfect square. Then 3 times 18 equals 54. 450. Begin by rationalizing the denominator. Use the product property to simplify the numerator. Simplify the whole numbers in the numerator and denominator. Then factor the radicand and look for perfect squares. Simplify the numerator and divide out common factors in the		identical radicals. $\frac{\sqrt{15} \cdot \sqrt{15} \cdot 7}{-3} = \frac{\sqrt{15} \cdot \sqrt{15} \cdot \sqrt{7}}{-3} = \frac{15\sqrt{7}}{-3}$
Now factor the terms in the radicand and look for perfect squares. Simplify the radical. Another way is to multiply 6 and 54 to get 324, another perfect square. Then 3 times 18 equals 54. 450. Begin by rationalizing the denominator. Use the product property to simplify the numerator. Simplify the whole numbers in the numerator and denominator. Then factor the radicand and look for perfect squares. Simplify the numerator and divide out common factors in the	449.	There is more than one way to simplify an expression. Start this one by using the product property to combine the
Another way is to multiply 6 and 54 to get 324, another perfect square. Then 3 times 18 equals 54. 450. Begin by rationalizing the denominator. Use the product property to simplify the numerator. Simplify the whole numbers in the numerator and denominator. Then factor the radicand and look for perfect squares. Simplify the numerator and divide out common factors in the		Now factor the terms in the radicand and look for perfect $3\sqrt{54 \cdot 6} = 3\sqrt{9 \cdot 6 \cdot 6} = 3\sqrt{3 \cdot 3 \cdot 6 \cdot 6}$
Use the product property to simplify the numerator. Simplify the whole numbers in the numerator and denominator. Then factor the radicand and look for perfect squares. Simplify the numerator and divide out common factors in the		Another way is to multiply 6 and 54 to get 324, another perfect square. Then 3 times 18 equals 54.
Then factor the radicand and look for perfect squares. Simplify the numerator and divide out common factors in the	450.	Use the product property to simplify the numerator. Simplify the whole numbers in the $\frac{6\sqrt{126} \cdot \sqrt{18}}{18} = \frac{6\sqrt{126} \cdot 18}{18}$
numerator and denominator. $\frac{\sqrt{9 \cdot 9 \cdot 2 \cdot 2 \cdot 7}}{3} = \frac{9 \cdot 2\sqrt{7}}{3} = \frac{18\sqrt{7}}{3} = \frac{6\sqrt{7}}{3}$	匑	Then factor the radicand and look for perfect squares. Simplify the numerator and divide $\frac{6\sqrt{126 \cdot 18}}{18} = \frac{\sqrt{9 \cdot 7 \cdot 2 \cdot 2 \cdot 9}}{3} = \frac{\sqrt{9 \cdot 9 \cdot 2 \cdot 2 \cdot 7}}{3}$
		numerator and denominator. $\frac{\sqrt{9 \cdot 9 \cdot 2 \cdot 2 \cdot 7}}{3} = \frac{9 \cdot 2\sqrt{7}}{3} = \frac{18\sqrt{7}}{3} = \frac{6\sqrt{7}}{3}$

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Solving Radical Equations

This chapter will give you more practice operating with radicals. However, the focus here is to use radicals to solve equations. An equation is considered a *radical equation* when the radicand contains a variable. When you use a radical to solve an equation, you must be aware of the positive and negative roots. You should always check your results in the original equation to see that both solutions work. When one of the solutions does not work, it is called an *extraneous solution*. When neither solution works in the original equation, there is said to be no solution.

Tips for Solving Radical Equations

- Squaring both sides of an equation is a valuable tool when solving radical equations. Use the following property: When *a* and *b* are algebraic expressions, if *a* = *b*, then *a*² = *b*².
- Isolate the radical on one side of an equation before using the squaring property.
- Squaring a radical results in the radical symbol disappearing, e.g., $(\sqrt{x+5})^2 = x+5$.

• For second-degree equations, use the radical sign on both sides of the equation to find a solution for the variable. Check your answers.

Solve the following radical equations. Watch for extraneous solutions.

451.
$$x^2 = 49$$

452. $x^2 = 135$
453. $\sqrt{n} = 11$
454. $2\sqrt{a} = 24$
455. $\sqrt{2x} - 4 = 4$
456. $\sqrt{4x + 6} = 8$
457. $\sqrt{3x + 4} + 8 = 12$
458. $\sqrt{5x - 4} + 3 = 12$
459. $\sqrt{4x + 9} = -13$
460. $\sqrt{5x - 6} + 3 = 11$
461. $\sqrt{9 - x} + 14 = 25$
462. $3\sqrt{3x + 1} = 15$
463. $3\sqrt{-x} + 7 = 25$
464. $3 = 10 - \sqrt{100x - 1}$
465. $\sqrt{3x + 46} + 24 = 38$
466. $-7 = 10 - \sqrt{25x + 39}$
467. $3\sqrt{13x + 43} - 4 = 29$
468. $\frac{28}{\sqrt{5x + 1}} = 7$
469. $x = \sqrt{8 - 2x}$
470. $x = \sqrt{3x + 4}$
471. $x = \sqrt{x + 12}$
472. $x = \sqrt{7x - 10}$
473. $\sqrt{4x + 3} = 2x$
476. $x = \sqrt{\frac{3}{2}x + 10}$

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), {}, or [], perform operations in the innermost parentheses first and work outward.

 $(7)^2 = 49$

49 = 49

 $\sqrt{x^2} = \sqrt{135}$

 $(3\sqrt{15})^2 = 135$

 $3^{2}(\sqrt{15})^{2} = 135$ 9(15) = 135135 = 135

 $(-3\sqrt{15})^2 = 135$

 $(^{-3})^2(\sqrt{15})^2 = 135$ (9)(15) = 135 135 = 135

 $x = \sqrt{135} = \sqrt{9 \cdot 15} = \pm 3\sqrt{15}$

 $(-7)^2 = 49$ 49 = 49

The solution is <u>underlined</u>.

451. Use the radical sign on both sides of the equation. Show both solutions for the square root of 49. Check the first solution in the original equation.

Check the second solution in the original equation.

Both solutions, $x = \pm 7$, check out.

452. Use the radical sign on both sides of the equation. Simplify the radical.

Check the first solution in the original equation.

Check the second solution in the original equation.

Both solutions, $x = \pm 3\sqrt{15}$, check out.

453. First, square both sides of the equation. $(\sqrt{n})^2 = 11^2$ Simplify both terms.n = 121Check by substituting in the original equation. $\sqrt{121} = 11$ The original equation asks for only the positive root $\sqrt{121} = 11$ of *n*. So when you substitute 121 into the originalequation, only the positive rootof *n*. So when you substitute 121 into the originalequation, only the positive root $\sqrt{n} = 11$ is to beconsidered. 11 = 11 checks out. Although this mayseem trivial at this point, as the radical equationsbecome more complex, this will become important.

	501 Algebra Questions	
454.	Isolate the radical on one side of the equation. Divide both sides by 2.	$\frac{2\sqrt{a}}{2} = \frac{24}{2}$
	Simplify terms.	$\sqrt{a} = 12$
	Now square both sides of the equation. Simplify terms.	$(\sqrt{-a})^2 = 12^2$ a = 144
	Check the solution in the original equation.	$2\sqrt{144} = 24$
	The solution $a = 144$ checks out.	2(12) = 24 24 = 24
455.	Begin by adding 4 to both sides to isolate the radical.	$\sqrt{2x} - 4 + 4 = 4 + 4$
	Combine like terms on each side. Square both sides of the equation.	$\sqrt{2x} = 8$ $(\sqrt{2x})^2 = 8^2$
	Simplify terms.	2x = 64
	Divide both sides by 2. Check the solution in the original equation.	$x = 32$ $\sqrt{2(32)} - 4 = 4$
	Check the solution in the original equation.	$\sqrt{2(32)} - 4 = 4$
	The solution $x = 32$ checks out.	8 - 4 = 4, 4 = 4
456.	Square both sides of the equation.	$(\sqrt{4x+6})^2 = 8^2$ 4x+6=64
Γ.	Subtract 6 from both sides of the equation.	4x + 6 = 64 $4x = 58$
6	Divide both sides by 4 and simplify.	$x = \frac{58}{4} = 14.5$
	Check the solution in the original equation.	$\sqrt{4(14.5) + 6} = 8$
LU	Simplify terms.	$\sqrt{64} = 8$ $8 = 8$
457.	The solution $x = 14.5$ checks out. Subtract 8 from both sides in order to isolate the	0 = 0
437.	radical.	$\sqrt{3x+4} = 4$
	Square both sides of the equation.	$(\sqrt{3x+4})^2 = 4^2$
	Simplify terms. Subtract 4 from both sides and divide by 3.	3x + 4 = 16 $x = 4$
	Check your solution in the original equation.	$\sqrt[n]{3(4) + 4} + 8 = 12$
	Simplify terms.	$\sqrt{16} + 8 = 12$
		4 + 8 = 12 12 = 12
	The solution $x = 4$ checks out.	1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 - 1 -

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458.	 Subtract 3 from both sides of the equation isolating the radical. Square both sides of the equation. Simplify terms on both sides. Add 4 to both sides and then divide by 5. Check your solution in the original equation. Simplify terms under the radical sign. Find the positive square root of 81. Simplify. The solution x = 17 checks out. Square both sides of the equation. Simplify terms on both sides of the equation. Subtract 9 from both sides and then divide by 4. Substitute the solution in the original equation. Simplify the expression under the radical sign. The radical sign calls for the positive square root. There is no solution for this equation. 	$\sqrt{5x-4} = 9$ $(\sqrt{5x-4})^2 = 9^2$ 5x-4 = 81 $x = \frac{85}{5} = 17$ $\sqrt{5(17)-4} + 3 = 12$ $\sqrt{81} + 3 = 12$ 9 + 3 = 12 12 = 12 $(\sqrt{4x+9})^2 = (-13)^2$ 4x + 9 = 169 x = 40 $\sqrt{4(40+9)} = -13$ $\sqrt{169} = -13$ $13 \neq -13$
460.	Subtract 3 from both sides isolating the radical. Square both sides of the equation. Simplify terms. Add 6 to both sides and divide the result by 5. Check the solution in the original equation. Simplify the expression under the radical. Find the positive square root of 64 and add 3. The solution $x = 14$ checks out.	$\sqrt{5x-6} = 8$ $(\sqrt{5x-6})^2 = 8^2$ 5x-6 = 64 x = 14 $\sqrt{5(14)-6} + 3 = 11$ $\sqrt{64} + 3 = 11$ 8 + 3 = 11 11 = 11 $\sqrt{9-x} = 121$ x = 112 x = -112 $\sqrt{9-(-112)} + 14 = 25$ $\sqrt{121} + 14 = 25$ 25 = 25

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462.	 To isolate the radical, divide both sides by 3. Square both sides of the equation. Simplify terms. Subtract 1 from both sides of the equation and divide by 3. Check the solution in the original equation. Simplify the expression under the radical sign. Multiply 3 by the positive root of 25. The solution <i>x</i> = 8 checks out. 	$\sqrt{3x + 1} = 5$ $(\sqrt{3x + 1})^2 = 5^2$ 3x + 1 = 25 x = 8 $3\sqrt{3(8) + 1} = 15$ $3\sqrt{25} = 15$ 3(5) = 15 15 = 15
	Subtract 7 from both sides of the equation. Divide both sides by 3 to isolate the radical. Square both sides of the equation. Simplify terms. Multiply both sides by negative 1. Check the solution in the original equation. Simplify terms under the radical. Use the positive square root of 25. The solution $x = -25$ checks out. Add $\sqrt{100x - 1}$ to both sides of the equation. $3 + \sqrt{100x - 1} = 10 - $ Combine like terms and simplify the equation. Now subtract 3 from both sides. Square both sides of the equation. Add 1 to both sides of the equation and divide by 100. Check the solution in the original equation.	$3\sqrt{-x} = 18$ $\sqrt{-x} = 6$ $(\sqrt{-x})^2 = 6^2$ -x = 36 $3\sqrt{-(-36)} + 7 = 25$ $3\sqrt{36} + 7 = 25$ 3(6) + 7 = 25 18 + 7 = 25 25 = 25 $\sqrt{100x - 1} + \sqrt{100x - 1}$ $3 + \sqrt{100x - 1} = 10$ $\sqrt{100x - 1} = 7$ 100x - 1 = 49 x = 0.5 $3 = 10 - \sqrt{100(0.5) - 1}$ $3 - 10 - \sqrt{40}$
465.	 Simplify the expression under the radical sign. The equation asks you to subtract the positive square root of 49 from 10. The solution x = 0.5 checks out. Subtract 24 from both sides to isolate the radical. Square both sides of the equation. Subtract 46 from both sides of the equation and divide by 3. Check the solution in the original equation. Simplify the expression under the radical sign. The solution x = 50 checks out. 	$3 = 10 - \sqrt{49}$ 3 = 10 - 7 3 = 3 $\sqrt{3x + 46} = 14$ 3x + 46 = 196 x = 50 $\sqrt{3(50) + 46} + 24 = 38$ $\sqrt{196} + 24 = 38$ 14 + 24 = 38 38 = 38

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466.	Add $\sqrt{25x + 39}$ to both sides of the equation. $\sqrt{25x + 39} - 7 = 10 - \sqrt{25x + 39} + \sqrt{25x + 39}$ Combine like terms and simplify the equation. $\sqrt{25x + 39} - 7 = 10$
	Add 7 to both sides of the equation. $\sqrt{25x + 39} = 17$
	Square both sides. $25x + 39 = 289$
	Subtract 39 from both sides and divide
	the result by 25. $x = 10$
	Check the solution in the original equation. $-7 = 10 - \sqrt{25(10) + 39}$
	Simplify the expression under the radical sign. $^{-7} = 10 - \sqrt{289}$ The equation asks you to subtract the positive
	square root of 289 from 10. $^{-7} = 10 - 17$
	The solution $x = 10$ checks out. $-7 = -7$
467.	To isolate the radical on one side of the equation,
	add 4 to both sides and divide the result by 3. $\sqrt{13x + 43} = 11$ Square both sides of the equation. $13x + 43 = 121$
	Subtract 43 from both sides and divide by 13. $x = 6$
	Check the solution in the original equation. $3\sqrt{13(6) + 43} - 4 = 29$
	Simplify the expression under the radical sign. $3\sqrt{121} - 4 = 29$
T	Evaluate the left side of the equation. $3(11) - 4 = 29$
	The solution $x = 6$ checks out. $29 = 29$
468.	To isolate the radical on one side of the equation,
	multiply both sides by $\sqrt{5x+1}$. $28 = 7\sqrt{5x+1}$
	Divide both sides of the equation by 7. $4 = \sqrt{5x+1}$
	Square both sides of the equation. $16 = 5x + 1$ Subtract 1 from both sides and divide the result by 5. $3 = x$
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	Simplify the expression under the radical sign. $\frac{28}{\sqrt{16}} = 7$
	Divide the numerator by the positive square root of 16. $\frac{28}{4} = 7$
	The solution $3 = x$ checks out. $7 = 7$
469.	The radical is alone on one side. Square
	both sides. $x^2 = 8 - 2x$ Transform the equation by putting all terms
	on one side. $x^2 + 2x - 8 = 0$
	The result is a quadratic equation. Solve
	for x by factoring using the trinomial
	factor form and setting each factor equal to zero and solving for r . (Refer to
	to zero and solving for <i>x</i> . (Refer to Chapter 16 for practice and tips for
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	factoring quadratic equations.) It will be important to check each solution. Let the first factor equal zero and solve for x . Subtract 4 from both sides. Check the solution in the original equation. Evaluate the expression under the radical sign. The radical sign calls for a positive root. Therefore, x cannot equal ⁻⁴ . $x = ^{-4}$ is an example of an <i>extraneous root</i> . Let the second factor equal zero and solve for x . Subtract 2 from both sides. Check the solution in the original equation. Evaluate the expression under the radical sign. The positive square root of 4 is 2. Therefore, the only solution for the equation is $x = 2$.	$-4 = \sqrt{16}$ $-4 \neq 4$ $x - 2 = 0$ $x = 2$
fid 家	With the radical alone on one side of the equation, square both sides. The resulting quadratic equation may have up to two solutions. Put it into standard form and factor the equation using the trinomial factor form to find the solutions. Then check the solutions in the original equation. Letting each factor equal zero and solving for <i>x</i> results in two possible solutions, $x = 4$ and/or ⁻¹ . Check the first possible solution in the original equation. The solution checks out. Now check the second possible solution in the original equation in the original equation in the original equation in the original equation. Therefore, $x \neq -1$. $x = -1$ is an <i>extraneous root</i> . The only solution for the original equation is $x = 4$.	$x^{2} = 3x + 4$ $x^{2} - 3x - 4 = (x - 4)(x + 1) = 0$ $(4) = \sqrt{3(4) + 4} = \sqrt{16} = 4$ $(-1) = \sqrt{3(-1) + 4} = \sqrt{1} = 1$ $-1 \neq 1$

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471.	Square both sides of the equation.	$x^2 = x + 12$
	Subtract $(x + 12)$ from both sides of the equation	$x^2 - x - 12 = 0$
	the equation. The resulting quadratic equation may have	x - x - 12 = 0
	up to two solutions. Factor the equation	
	to find the solutions and check in the	
	original equation.	$x^2 - x - 12 = (x - 4)(x + 3) = 0$
	Let the first factor equal zero and	
	solve for <i>x</i> .	x - 4 = 0, so $x = 4$
	Let the second factor equal zero and solve for <i>x</i> .	<i>u</i> · 2 · 0 · · · · · ⁻²
	Check each solution in the original	x + 3 = 0, so $x = -3$
	equation to rule out an extraneous solution	on. $(4) = \sqrt{(4) + 12}$
	Simplify the expression under the radical sig	
	The solution $x = 4$ checks out.	
	Now check the second possible solution	
	in the original equation.	$(-3) = \sqrt{(-3) + 12}$
	You could simplify the expression under the	
	radical sign to get the square root of 9. However, the radical sign indicates that	
	the positive solution is called for, and the	
	left side of the original equation when	
H	x = -3 is a negative number. So, $x = -3$ is	
	not a solution.	
472.	Square both sides of the equation.	$x^2 = 7x - 10$
	Subtract $(7x - 10)$ from both sides of the	
177		$x^2 - 7x + 10 = 0$
F33	Factor the quadratic equation to find the solutions, and check each in the original	
	equation to rule out any extraneous	
		$x^2 - 7x + 10 = (x - 5)(x - 2) = 0$
	The first factor will give you the solution	
	x = 5. The second factor will give the	
	solution $x = 2$. Check the first solution for the quadratic equation in the	
	original equation.	$(5) = \sqrt{7(5) - 10}$
	Simplify the expression under the	
	radical sign.	$5 = \sqrt{25} \text{ or } 5 = 5$
	The solution $x = 5$ is a solution to the	I
	original equation.	I
	Now check the second solution to the quadratic equation in the original.	$(2) = \sqrt{7(2) - 10}$
	Simplify the expression under the	
	radical sign.	$2 = \sqrt{4}$ or $2 = 2$
	There are two solutions to the original	
	equation,	x = 2 and $x = 5$
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473.	Square both sides of the radical	4
	equation. Transform the equation into a	$4x + 3 = \underline{4x^2}$
	quadratic equation.	$4x^2 - 4x - 3 = 0$
	Factor the result using the trinomial factor form.	$4x^2 - 4x - 3 = (2x + 1)(2x - 3) = 0$
	Let the first factor equal zero and	12 12 5 - (22 + 1)(22 + 5) = 0
	solve for x .	2x + 1 = 0, so $x = -0.5$
	Let the second factor equal zero and solve for <i>x</i> .	2x - 3 = 0, so $x = 1.5$
	When you substitute -0.5 for x in the	
	original equation, the result will be $\sqrt{1} = -1$. That cannot be true for the	
	original equation, so $x \neq -0.5$.	
	Substitute 1.5 for x in the original	
	equation. Simplify the terms on each side of	$\sqrt{4(1.5) + 3} = 2(1.5)$
	the equal sign.	$\sqrt{9} = 3 \text{ or } 3 = 3$
	The only solution for the original equation is $x = 1.5$.	
474.		$2 - \frac{7}{2}x = x^2$
	Subtract $(2 - \frac{7}{2}x)$ from both sides	2
	of the equation.	$0 = x^2 + \frac{7}{2}x - 2$
	Multiply both sides of the equation by 2 to simplify the fraction.	$0 = 2x^2 + 7x - 4$
	Factor using the trinomial factor form.	$2x^2 + 7x - 4 = (2x - 1)(x + 4) = 0$
	Let the first factor equal zero and solve for <i>x</i> .	$2x - 1 = 0$, so $x = \frac{1}{2}$
-33	Let the second factor equal zero and	2x - 1 = 0, 30x - 2
	solve for <i>x</i> .	x + 4 = 0, so $x = -4$
	Check the first possible solution in the original equation.	$\sqrt{2 - \frac{7}{2}(\frac{1}{2})} = (\frac{1}{2})$
	Simplify the expression under the	
	radical sign.	$\sqrt{2 - \frac{7}{4}} = \sqrt{2 - 1\frac{3}{4}} = \sqrt{\frac{1}{4}} = \frac{1}{2}$
		$\frac{1}{2} = \frac{1}{2}$
	So $x = \frac{1}{2}$ is a solution.	2 2
	Check the solution $x = -4$ in the original equation.	$\sqrt{2 - 7(-4)}$ (-4)
		$\sqrt{2 - \frac{7}{2}(-4)} = (-4)$
	Simplify the expression. This is not true. There is one solution	$\sqrt{16} = (-4)$ or $4 = -4$
	for the original equation, $x = \frac{1}{2}$.	

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	475.	Square both sides of the equation. Add $\left(\frac{-3}{2x} - 10\right)$ to both sides of	$x^2 = \frac{3}{2}x + 10$	
		the equation.	$x^2 - \frac{3}{2}x - 10 = 0$	
		Multiply the equation by 2 to eliminate the fraction.	$2x^2 - 3x - 20 = 0$	
		Factor using the trinomial factor form. Letting each factor of the trinomial factors equal zero results in two possible solutions for the original	$2x^2 - 3x - 20 = (x - 4)(2x + 5) = 0$	0
		equation, $x = 4$ and/or $x = -2\frac{1}{2}$. Check the first possible solution in		
		the original equation.	$4 = \sqrt{\frac{3}{2}(4) + 10}$	
		Simplify the radical expression. The solution $x = 4$ checks out as a solution for the original equation.	$4 = \sqrt{16} \text{ or } 4 = 4$	
		Check the second possible solution in the original equation. A negative number cannot be equal to	$-2\frac{1}{2} = \sqrt{\frac{3}{2}(-2\frac{1}{2}) + 10}$	
	9	a positive square root as the radical sign in the original expression calls for Therefore, $x = {}^{-}2\frac{1}{2}$ is not a solution to the original equation. The only		
		solution for this equation is $x = 4$.		
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Solving Equations with the Quadratic Formula



In this chapter, you will have the opportunity to practice solving equations using the quadratic formula. In Chapter 17, you practiced using factoring to solve quadratic equations, but factoring is useful only for those equations that can easily be factored. The quadratic formula will allow you to find solutions for any quadratic equation that can be put in the form $ax^2 + bx + c = 0$, where *a*, *b*, and *c* are numbers.

The quadratic formula tells you that for any equation in the form $ax^2 + bx + c = 0$, the solution will be $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$. The solutions found using the quadratic formula are also called the roots of the equation. Some solutions will be in the form of whole numbers or fractions. Some will be in the form of a radical. Some will be undefined, as when the radicand is equal to a negative number. The \pm in the quadratic equation tells you that there will be two solutions, one when you add the radical and one when you subtract it.

Tips for Solving Equations with the Quadratic Formula

- Transform the equation into the form ax² + bx + c = 0. Use the values for a, b, and c in the quadratic equation to determine the solution for the original equation.
- For solutions that contain a radical, be sure to simplify the radical as you practiced in Chapter 18.
- When you are asked to find the solution to the nearest hundredth, you can use a calculator to find the value of the radical.

Solve the following equations using the quadratic formula. Reduce answers to their simplest form or to the simplest radical form. Use of a calculator is recommended.

476. $x^2 + 2x - 8 = 0$ **477.** $2x^2 - 7x - 30 = 0$ **478.** $6x^2 + 13x - 28 = 0$ **479.** $18x^2 + 9x + 1 = 0$ **480.** $6x^2 + 17x = 28$ **481.** $14x^2 = 12x + 32$ **482.** $4x^2 + 5x = 0$ **483.** $5x^2 = 27$ **484.** $5x^2 = 18x - 17$ **485.** $3x^2 + 11x - 7 = 0$ **486.** $5x^2 + 52x + 20 = 0$ **487.** $x^2 = \frac{-5x-2}{2}$ **488.** $x^2 + 8x = 5$ **489.** $x^2 = 20x - 19$ **490.** $23x^2 = 2(8x - 1)$ **491.** $x^2 + 10x + 11 = 0$ **492.** $24x^2 + 18x - 6 = 0$ **493.** $7x^2 = 4(3x + 1)$ **494.** $\frac{1}{3}x^2 + \frac{3}{4}x - 3 = 0$ **495.** $5x^2 - 12x + 1 = 0$

Find the solution to the following equations to the nearest hundredth.

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496. $11r^2 - 4r - 7 = 0$ **497.** $3m^2 + 21m - 8 = 0$ **498.** $4y^2 = 16y - 5$ **499.** $5s^2 + 12s - 1 = 0$ **500.** $4c^2 - 11c + 2 = 0$ **501.** $11k^2 - 32k + 10 = 0$

Answers

Numerical expressions in parentheses like this [] are operations performed on only part of the original expression. The operations performed within these symbols are intended to show how to evaluate the various terms that make up the entire expression.

Expressions with parentheses that look like this () contain either numerical substitutions or expressions that are part of a numerical expression. Once a single number appears within these parentheses, the parentheses are no longer needed and need not be used the next time the entire expression is written.

When two pair of parentheses appear side by side like this ()(), it means that the expressions within are to be multiplied.

Sometimes parentheses appear within other parentheses in numerical or algebraic expressions. Regardless of what symbol is used, (), {}, or [], perform operations in the innermost parentheses first and work outward.

The solutions are underlined.

476. The equation is in the proper form. First, list the values for *a*, *b*, and *c*. Substitute the values into the quadratic equation.

Simplify the expression under the radical sign. $x = \frac{-2 \pm \sqrt{4 - 32}}{2} = \frac{-2 \pm \sqrt{36}}{2}$

Evaluate the square root of 36.Find the two solutions for *x* by simplifying terms. First add the terms in the numerator, and then subtract them.

The two solutions for the variable x are x = 2and x = -4.

477. The equation is in the proper form. First, list the values for *a*, *b*, and *c*. Substitute the values into the quadratic equation.

Simplify the expression. Find the two solutions for *x* by adding and then subtracting in the numerator.

The two solutions for the variable *x* are $\underline{x} = \underline{6}$ and $\underline{x} = -2.5$.

$$a = 2 \quad b = -7 \quad c = -30$$
$$x = \frac{-(-7) \pm \sqrt{(-7)^2 - 4(2)(-30)}}{2(2)}$$
$$x = \frac{7 \pm \sqrt{49 - (-240)}}{4} = \frac{7 \pm \sqrt{289}}{4} = \frac{7 \pm 17}{4}$$

a = 1 b = 2 $c = -\frac{1}{2}$

 $x = \frac{-2 \pm 6}{2}$

 $x = \frac{-2 \pm \sqrt{(2)^2 - 4(1)(-8)}}{2}$

 $x = \frac{-2+6}{2} = \frac{4}{2} = 2$ and

 $x = \frac{-2-6}{2} = \frac{-8}{2} = -4$

$$x = \frac{7+17}{4} = \frac{24}{4} = 6 \text{ and}$$
$$x = \frac{7-17}{4} = \frac{-10}{4} = -2.5$$

478. The equation is in the proper form. First, list the values for *a*, *b*, a = 6 b = 13 c = -28and *c*. Substitute the values into the $x = \frac{-(13) \pm \sqrt{(13)^2 - 4(6)(-28)}}{2(6)}$ quadratic equation. $x = \frac{-13 \pm \sqrt{169 + 672}}{12} = \frac{-13 \pm \sqrt{841}}{12} = \frac{-13 \pm 29}{12}$ Simplify the expression. Find the two solutions for *x* by adding and then subtracting $x = \frac{-13 + 29}{12} = \frac{16}{12} = 1\frac{1}{3}$ and in the numerator. $x = \frac{-13 - 29}{12} = \frac{-42}{12} = -3\frac{1}{2}$ The two solutions for the variable x are $x = 1\frac{1}{3}$ and $x = -3\frac{1}{2}$. The equation is in the proper form. 479. a = 18 b = 9 c = 1First, list the values for *a*, *b*, and *c*. Substitute the values into the $x = \frac{-(9) \pm \sqrt{(9)^2 - 4(18)(1)}}{2(18)}$ quadratic equation. $x = \frac{-9 \pm \sqrt{81 - 72}}{36} = \frac{-9 \pm \sqrt{9}}{36} =$ Simplify the expression. Find the two solutions for x by adding and then subtracting in the $x = \frac{-9+3}{36} = \frac{-6}{36} = \frac{-1}{6}$ and numerator. $x = \frac{-12}{36} = \frac{-1}{3}$ The two solutions for the variable xare $x = \frac{-1}{6}$ and $x = \frac{-1}{3}$. **480.** First transform the equation into the proper form. Subtract 28 from $6x^2 + 17x - 28 = 28 - 28$ both sides of the equation. Combine like terms on both $6x^2 + 17x - 28 = 0$ sides. Now list the values for *a*, *b*, a = 6 b = 17 c = -28and c. Substitute the values into the $x = \frac{-(17) \pm \sqrt{(17)^2 - 4(6)(-28)}}{2(6)}$ quadratic equation. $x = \frac{-17 \pm \sqrt{289 \pm 672}}{12} = \frac{-17 \pm \sqrt{961}}{12} = \frac{-17 \pm 31}{12}$ Simplify the expression. Find the two solutions for *x* by adding and then subtracting $x = \frac{-17 + 31}{12} = \frac{14}{12} = 1\frac{1}{6}$ and in the numerator. $x = \frac{-17 - 31}{12} = \frac{-48}{12} = -4$ The two solutions for the variable *x* are $x = 1\frac{1}{6}$ and x = -4.

	First transform the equation into the proper form. Add $(-12x - 32)$ to both sides of the equation. $14x^2 - 12x - 32 = 12x + 32 - 12x - 32$ Combine like terms. $14x^2 - 12x - 32 = 0$ Now list the values for a, b , and c . $a = 14$ $b = -12$ $c = -32$ Substitute the values into the quadratic equation. $x = \frac{-(-12) \pm \sqrt{(-12)^2 - 4(14)(-32)}}{2(14)}$ mplify the expression. $x = \frac{12 \pm \sqrt{144 + 1,792}}{28} = \frac{12 \pm \sqrt{1,936}}{28} = \frac{12 \pm 44}{28}$ mplify the two solutions for x by adding and then subtracting in the numerator. $x = \frac{12 - 44}{28} = \frac{56}{28} = 2$ and $x = \frac{12 - 44}{28} = \frac{-32}{28} = -1\frac{1}{7}$	
	The two solutions for the variable x are $x = 2$ and $x = -1\frac{1}{7}$. Yes, you could have divided both sides of the equation by 2 before listing your <i>a</i> , <i>b</i> , and <i>c</i> values. However, the solution would have been the same. Try it yourself.	
482.	The equation may not appear to be in proper form because there is no value for <i>c</i> . But you could write it as $4x^2 + 5x + 0 = 0$, and then your values would be $a = 4, b = 5$, and $c = 0$. Substitute the values into the quadratic equation. $x = \frac{-(5) \pm \sqrt{(5)^2 - 4(4)(0)}}{2(4)}$	
匑	Simplify the expression. Find the two solutions for x by adding and then subtracting in the numerator. $x = -\frac{5 \pm \sqrt{25 - 0}}{8} = \frac{-5 \pm 5}{8}$ $x = \frac{-5 + 5}{8} = \frac{0}{8} = 0 \text{ and}$ $x = \frac{-5 - 5}{8} = \frac{-10}{8} = -1\frac{1}{4}$	
	The two solutions for the variable x are $x = 0$ and $x = -1\frac{1}{4}$.	
483.	Subtract 27 from both sides of the equation. $5x^2 - 27 = 27 - 27$ or $5x^2 - 27 = 0$ In this equation, there appears to be no coefficient for the <i>x</i> term unless you realize that $0x = 0$. So you could write the equation in the proper form like this: $5x^2 + 0x - 27 = 0$ Now list the values for <i>a</i> , <i>b</i> , and <i>c</i> . $a = 5$ $b = 0$ $c = -27$ Substitute the values into the quadratic equation. $x = \frac{-(0) \pm \sqrt{(0)^2 - 4(5)(-27)}}{2(5)}$	
	Simplify the expression. $x = \frac{\pm\sqrt{4.5.27}}{10} = \frac{\pm\sqrt{4.9.5.3}}{10} = \frac{\pm2.3\sqrt{5.3}}{10} = \pm \frac{6\sqrt{15}}{10} \pm \frac{3\sqrt{15}}{5}$	

 $\frac{\pm 3\sqrt{6}}{2} = \pm 1\frac{1}{2}\sqrt{6}$ Simplify the radical. The two solutions for the variable *x* are $x = \pm 1\frac{1}{2}\sqrt{6}$. **484.** Transform the equation into the desired form. Subtract 18x and $5x^2 - 18x + 17 = 18x - 18x - 17 + 17$ add 17 to both sides. $5x^2 - 18x + 17 = 0$ Combine like terms on both sides. a = 5 b = -18 c = 17Now list the values for *a*, *b*, and *c*. Substitute the values into the $x = \frac{-(-18) \pm \sqrt{(-18)^2 - 4(5)(17)}}{2(5)}$ quadratic equation. $x = \frac{18 \pm \sqrt{324 - 340}}{10} = \frac{18 \pm \sqrt{-16}}{10}$ Simplify the expression. Since there is no rational number equal to the square root of a negative number, there are no solutions for this equation. **485.** List the values of *a*, *b*, and *c*. a = 3 b = 11 c = -7Substitute the values into $x = \frac{-(11) \pm \sqrt{(11)^2 - 4(3)(-7)}}{2(3)}$ the quadratic equation. $x = \frac{-11 \pm \sqrt{121 + 84}}{6} = \frac{-11 \pm \sqrt{205}}{6} = -1\frac{5}{6} \pm \frac{1}{6}\sqrt{205}$ Simplify the expression. The solutions for the variable x are $x = -1\frac{5}{6} \pm \frac{1}{6}\sqrt{205}$. a = 5 b = 52 c = 20**486.** List the values of *a*, *b*, and *c*. Substitute the values into the $x = \frac{-(52) \pm \sqrt{(52)^2 - 4(5)(20)}}{2(5)}$ quadratic equation. $x = \frac{-52 \pm \sqrt{2,704 - 400}}{10} = \frac{-52 \pm \sqrt{2,304}}{10} = \frac{-52 \pm 48}{10}$ Simplify the expression. Find the two solutions for *x* by adding and then subtracting $x = \frac{-52 + 48}{10} = \frac{-4}{10} = -0.4$ and in the numerator. $x = \frac{-52 - 48}{10} = \frac{-100}{10} = -10$ The two solutions for the variable x are x = -0.4 and x = -10.

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487.	First, multiply both sides of the equation by 2. Then add $5x + 2$ to both sides of the equation. List the values of $a, b,$ and c . Substitute the values into the quadratic equation. Find the two solutions for x by adding and then sub- tracting in the numerator. $2x^2 + 5x + 2 = 0$ $a = 2 b = 5 c = 2$ $x = \frac{-(5) \pm \sqrt{(5)^2 - 4(2)(2)}}{2(2)} = \frac{-5 \pm \sqrt{25 - 16}}{2(2)} = \frac{-5 \pm 3}{4} = \frac{-5 \pm 3}{4}$ $x = \frac{-5 \pm 3}{4} = \frac{-2}{4} = \frac{-1}{2} \text{ and } x = \frac{-5 - 3}{4} = \frac{-8}{4} = -2$		
	The two solutions for the variable <i>x</i> are $x = \frac{-1}{2}$ and $x = -2$.		
488.	Transform the equation by subtracting 5 from both sides. $x^2 + 8x - 5 = 0$ List the values of a, b, and c. Substitute the values into the quadratic equation. $a = 1$ $b = 8$ $c = -5$ Simplify the expression. $x = \frac{-8 \pm \sqrt{82} - 4(1)(-5)}{2(1)}$		
t na s	$x = \frac{-8 \pm \sqrt{4 \cdot 21}}{2} = \frac{-8 \pm 2\sqrt{21}}{2} = -4 \pm \sqrt{21}$		
489.	The solution for the variable x is $x = -4 \pm \sqrt{21}$. 489. Transform the equation by subtracting 20x and adding 19 to both sides of the equation. List the values of a, b, and c. Substitute the values into the quadratic equation. $x^2 - 20x + 19 = 0$ a = 1 $b = -20$ $c = 19x = \frac{-(-20) \pm \sqrt{(-20)^2 - 4(1)(19)}}{2(1)}$		
	Simplify the expression. Find the two solutions for x by adding and then subtracting in the numerator. $x = \frac{20 \pm \sqrt{400 - 76}}{2} = \frac{20 \pm \sqrt{324}}{2} = \frac{20 \pm 18}{2}$ $x = \frac{20 + 18}{2} = \frac{38}{2} = 19 \text{ and}$ $x = \frac{20 - 18}{2} = \frac{2}{2} = 1$		
The two solutions for the variable x are $x = 19$ and $x = 1$.			
490.	Transform the equation into proper form. Use the distributive property of multiplica- tion on the right side of the equation. $23x^2 = 16x - 2$ $23x^2 - 16x + 2 = 0$ $a = 23$ Subtract 16x and add 2 to both sides. List the values of a, b, and c. Substitute the values into the quadratic equation. $23x^2 - 16x + 2 = 0$ $a = 23$ $b = -16$ $c = 2$ Substitute the values into the quadratic equation. $x = \frac{-(-16) \pm \sqrt{(-16)^2 - 4(23)(2)}}{2(23)}$		
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		$x = \frac{16 \pm \sqrt{256 - 184}}{2(23)} = \frac{16 \pm \sqrt{72}}{2(23)} = \frac{16 \pm \sqrt{4 \cdot 9 \cdot 2}}{2(23)} = \frac{2 \cdot 8 \pm 2 \cdot 3 \sqrt{2}}{2(23)} = \frac{8 \pm 3 \sqrt{2}}{23} = \frac{8}{23} \pm \frac{3}{23}\sqrt{2}$			
		The solution for the variable x is $x = \frac{8}{23} \pm \frac{3}{23}\sqrt{2}$.			
	491.	List the values of <i>a</i> , <i>b</i> , and <i>c</i> . Substitute the values into the quadratic equation. Simplify the expression. $x = \frac{-10 \pm \sqrt{100 - 44}}{2} = \frac{-10 \pm \sqrt{56}}{2} = \frac{-10 \pm \sqrt{4 \cdot 14}}{2} = \frac{-10 \pm 2\sqrt{14}}{2} = -5 \pm \sqrt{14}$			
		The two solutions for the variable x are $x = -5 + \sqrt{14}$ and $x = -5 - \sqrt{14}$.			
	492.	List the values of <i>a</i> , <i>b</i> , and <i>c</i> . Substitute the values into the quadratic equation. $a = 24 b = 18 c = -6$ $x = \frac{-(18) \pm \sqrt{(18)^2 - 4(24)(-6)}}{2(24)}$			
	_	Simplify the expression. Find the two solutions for x by adding and then subtracting in the numerator. $x = \frac{-18 \pm \sqrt{324 \pm 576}}{48} = \frac{-18 \pm \sqrt{900}}{48} = \frac{-18 \pm 30}{48}$ $x = \frac{-18 \pm 30}{48} = \frac{12}{48} = \frac{1}{4}$ and $x = \frac{-18 - 30}{48} = \frac{-18}{48} = -1$			
I.		The two solutions for the variable x are $x = \frac{1}{4}$ and $x = \frac{-1}{4}$.			
	493.	Transform the equation into the proper form. First use the distributive property of multiplication. $7x^2 = 4(3x) + 4(1) = 12x + 4$ Then subtract $(12x + 4)$ from both sides. $7x^2 - 12x - 4 = 0$ List the values of a, b, and c. Substitute the values into the $a = 7$ $b = -12$ $c = -4$			
		quadratic equation. $x = \frac{-(-12) \pm \sqrt{(-12)^2 - 4(7)(-4)}}{2(7)}$			
		Simplify the expression. $x = \frac{12 \pm \sqrt{144 + 112}}{14} = \frac{12 \pm \sqrt{256}}{14} = \frac{12 \pm 16}{14}$			
		Find the two solutions for x by adding and then subtracting in the numerator. $x = \frac{12 + 16}{14} = \frac{28}{14} = 2 \text{ and}$ $x = \frac{12 - 16}{14} = \frac{-4}{14} = \frac{-2}{7}$			
		The two solutions for the variable <i>x</i> are $x = 2$ and $x = \frac{-2}{7}$.			

494.	 You could use the fractions as values for <i>a</i> and <i>b</i>, but it might be easier to first transform the equation by multiplying it by 12. Using the distributive property, you get Simplify the terms. List the values of <i>a</i>, <i>b</i>, and <i>c</i>. Substitute the values into the quadratic equation. Simplify the expression. 	$12(\frac{1}{3}x^{2} + \frac{3}{4}x - 3 = 0)$ $12(13x^{2}) + 12(\frac{3}{4}x) - 12(3) = 12(0).$ $4x^{2} + 9x - 36 = 0$ $a = 4 b = 9 c = -36$ $x = \frac{-(9) \pm \sqrt{(9)^{2} - 4(4)(-36)}}{2(4)}$ $x = \frac{-9 \pm \sqrt{81 + 576}}{8} = \frac{-9 \pm \sqrt{657}}{8}$
495.	The two solutions for the variable x are $\frac{1}{2}$.	$= \frac{-9 \pm \sqrt{9 \cdot 73}}{8} = \frac{-9 \pm 3\sqrt{73}}{8}$ $x = \frac{-9 \pm 3\sqrt{73}}{8} \text{ and } x = \frac{-9 - 3\sqrt{73}}{8}.$ a = 5 b = -12 c = 1
	Substitute the values into the quadratic equation. Simplify the expression. $x = \frac{12 \pm \sqrt{144 - 20}}{2(5)} = \frac{12 \pm 20}{2}$	$x = \frac{-(-12) \pm \sqrt{(-12)^2 - 4(5)(1)}}{2(5)}$ $\frac{\sqrt{124}}{5(5)} = \frac{12 \pm \sqrt{4 \cdot 31}}{2(5)} = \frac{12 \pm 2\sqrt{31}}{2(5)} = \frac{6 \pm \sqrt{31}}{5}$
496.	The two solutions for the variable <i>x</i> are . List the values of <i>a</i> , <i>b</i> , and <i>c</i> . Substitute the values into the	a = 11 $b = -4$ $c = -7$
匑	quadratic equation. Simplify the expression. Find the two solutions for <i>r</i> by adding and then subtracting in the numerator	$x = \frac{-(-4) \pm \sqrt{(-4)^2 - 4(11)(-7)}}{2(11)}$ $r = \frac{4 \pm \sqrt{16 + 308}}{22} = \frac{4 \pm \sqrt{324}}{22} = \frac{4 \pm 18}{22}$ $r. r = \frac{4 + 18}{22} = \frac{22}{22} = 1 \text{ and}$
	The two solutions for the variable r are r	$r = \frac{4 - 18}{22} = \frac{-14}{22} = -0.64$
497.	List the values of <i>a</i> , <i>b</i> , and <i>c</i> . Substitute the values into the quadratic equation.	$a = 3 b = 21 c = -8$ $m = \frac{-(21) \pm \sqrt{(21)^2 - 4(3)(-8)}}{2(3)}$
	Simplify the expression. The square root of 537 rounded to the nearest hundredth is 23.17. Substitute into the expression and simplify.	$m = \frac{-21 \pm \sqrt{441 \pm 96}}{6} = \frac{-21 \pm \sqrt{537}}{6}$ $m = \frac{-21 \pm 23.17}{6} = \frac{2.17}{6} = 0.36 \text{ and}$ $m = \frac{-21 - 23.17}{6} = \frac{-44.17}{6} = -7.36$
1	The two solutions for the variable m are	0 0

	501 Algebra Questions
498.	Transform the equation by subtracting 16y from and adding 5 to both sides. Combine like terms. List the values of <i>a</i> , <i>b</i> , and <i>c</i> . Substitute the values into the quadratic equation. $y = \frac{16 \pm \sqrt{256 - 80}}{8} = \frac{16 \pm \sqrt{176}}{8} = \frac{16 \pm \sqrt{16 \cdot 11}}{8} = \frac{16 \pm 4\sqrt{11}}{8}$ The square root of 11 rounded to the nearest hundredth is 3.32. Substitute into the expression and simplify. $y = \frac{16 - 4(3.32)}{8} = \frac{29.28}{8} = 0.34$
	The two solutions for the variable <i>y</i> are $y = 3.66$ and $y = 0.34$.
499.	List the values of <i>a</i> , <i>b</i> , and <i>c</i> . Substitute the values into the quadratic equation. $a = 5 b = 12 c = -1$ $s = \frac{-(12) \pm \sqrt{(12)^2 - 4(5)(-1)}}{2(5)}$
Ta	Simplify the expression. $s = \frac{-12 \pm \sqrt{144 + 20}}{10} = \frac{-12 \pm \sqrt{164}}{10}$ The square root of 164 rounded to the nearest hundredth is 12.81. Substitute into the expression and simplify. $s = \frac{-12 \pm \sqrt{144 + 20}}{10} = \frac{0.81}{10} = 0.081$
	and $s = \frac{-12 - 12.81}{10} = \frac{-24.81}{10} = -2.48$
	The two solutions for the variable <i>s</i> are $\underline{s} = 0.08$ and $\underline{s} = -2.48$.
500.	List the values of <i>a</i> , <i>b</i> , and <i>c</i> . Substitute the values into the quadratic equation. $a = 4 b = -11 c = 2$ $c = \frac{-(-11) \pm \sqrt{(-11)^2 - 4(4)(2)}}{2(4)}$
	Simplify the expression. $c = \frac{11 \pm \sqrt{121 - 32}}{8} = \frac{11 \pm \sqrt{89}}{8} = \frac{11 \pm 9.43}{8}$ $c = \frac{11 + 9.43}{8} = \frac{20.43}{8} = 2.55 \text{ and}$ $c = \frac{11 - 9.43}{8} = \frac{1.57}{8} = 0.20$
	The two solutions for the variable <i>c</i> are $\underline{c = 2.55}$ and $\underline{c = 0.20}$.
501.	List the values of <i>a</i> , <i>b</i> , and <i>c</i> . Substitute the values into the quadratic equation. $a = 11 b = -32 c = 10$ $k = \frac{-(-32) \pm \sqrt{(-32)^2 - 4(11)(10)}}{2(11)}$
	Simplify the expression. $k = \frac{32 \pm \sqrt{1,024 - 440}}{22} = \frac{32 \pm \sqrt{584}}{22} = \frac{32 \pm 24.17}{22}$ $k = \frac{32 \pm 24.17}{22} = \frac{56.17}{22} = 2.55 \text{ and}$
	$k = \frac{32 - 24.17}{22} = 7.8322 = 0.36$
	The two solutions for the variable <i>k</i> are $k = 2.55$ and $k = 0.36$.

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