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## The CENTRE for EDUCATION in MATHEMATICS and COMPUTING

cemc.uwaterloo.ca

### Pascal Contest

(Grade 9)

Tuesday, February 27, 2018
(in North America and South America)

Wednesday, February 28, 2018 (outside of North America and South America)



Time: 60 minutes

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Calculating devices are allowed, provided that they do not have any of the following features: (i) internet access, (ii) the ability to communicate with other devices, (iii) previously stored information such as formulas, programs, notes, etc., (iv) a computer algebra system, (v) dynamic geometry software.

#### Instructions

- 1. Do not open the Contest booklet until you are told to do so.
- 2. You may use rulers, compasses and paper for rough work.
- 3. Be sure that you understand the coding system for your response form. If you are not sure, ask your teacher to clarify it. All coding must be done with a pencil, preferably HB. Fill in circles completely.
- On your response form, print your school name and city/town in the box in the upper right corner.
- 5. Be certain that you code your name, age, grade, and the Contest you are writing in the response form. Only those who do so can be counted as eligible students.
- 6. This is a multiple-choice test. Each question is followed by five possible answers marked **A**, **B**, **C**, **D**, and **E**. Only one of these is correct. After making your choice, fill in the appropriate circle on the response form.
- 7. Scoring: Each correct answer is worth 5 in Part A, 6 in Part B, and 8 in Part C. There is no penalty for an incorrect answer.

Each unanswered question is worth 2, to a maximum of 10 unanswered questions.

- 8. Diagrams are *not* drawn to scale. They are intended as aids only.
- 9. When your supervisor tells you to begin, you will have sixty minutes of working time.
- 10. You may not write more than one of the Pascal, Cayley and Fermat Contests in any given year.

Do not discuss the problems or solutions from this contest online for the next 48 hours.

The name, grade, school and location, and score range of some top-scoring students will be published on our website, cemc.uwaterloo.ca. In addition, the name, grade, school and location, and score of some top-scoring students may be shared with other mathematical organizations for other recognition opportunities.

Each unanswered question is worth 2, to a maximum of 10 unanswered questions.

#### Part A: Each correct answer is worth 5.

- Which of the following is the smallest number?
  - $(\mathbf{A})$  1.4

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- **(B)** 1.2
- **(D)**  $1.5_{\text{M}}$

- The value of  $\frac{2018 18 + 20}{2}$ 
  - (A) 1010
- **(B)** 2020
- **(C)** 1008
- **(D)** 2017
- **(E)** 1011

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- July 3, 2030 is a Wednesday. What day of the week is July 14, 2030?
  - (A) Wednesday
- (B) Saturday

(C) Sunday

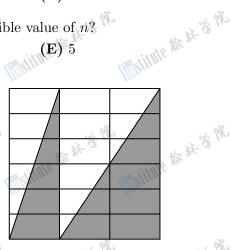
(**D**) Monday

- (E) Tuesday
- An electric car is charged 3 times per week for 52 weeks. The cost to charge the car each time is \$0.78. What is the total cost to charge the car over these 52 weeks?
  - (A) \$104.00
- **(B)** \$81.12
- **(C)** \$202.80
- **(D)** \$162.24
- **(E)** \$121.68
- If  $3 \times 3 \times 5 \times 5 \times 7 \times 9 = 3 \times 3 \times 7 \times n \times n$ , what is a possible value of n?
  - **(A)** 15

- In the diagram, 18 identical  $1 \times 2$  rectangles are put together to form a  $6 \times 6$  square. Part of the square is shaded, as shown. What percentage of the area of the  $6 \times 6$  square is shaded?



- **(E)** 25%



- 7. A box contains 5 black ties, 7 gold ties, and 8 pink ties. Stephen randomly chooses a tie from the box. Each tie is equally likely to be chosen. The probability that Stephen chooses a pink tie is equivalent to
  - (A)  $\frac{1}{4}$
- (B)  $\frac{7}{20}$
- (C)  $\frac{2}{5}$
- (D)  $\frac{3}{5}$
- (E)  $\frac{3}{4}$
- **对抗**机性 教育 技术 资 序彩 In the diagram, the number line between 0 and 5 is divided into 20 equal parts. The numbers S and T are marked on the line. What is the value of S + T?



- (A) 5.25

- The symbols  $\heartsuit$  and  $\nabla$  represent different positive integers less than 20. If  $\heartsuit \times \heartsuit \times \heartsuit = \nabla$ , what is the value of  $\nabla \times \nabla$ ?
  - (A) 12
- **(B)** 16
- (C) 36
- **(D)** 64
- **(E)** 81

 $(\mathbf{A})$  (0,0)

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- **(C)** (0,3)
- **(D)** (0,4)
- **(E)** (0,5)

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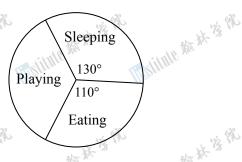
Part B: Each correct answer is worth 6.

11. In the diagram, the circle graph shows how a baby polar bear spent 24 hours. How many hours did it spend playing?



- **(B)** 7

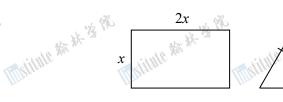
- **(D)** 9
- **(E)** 10



111112. C Glenda, Helga, Ioana, Julia, Karl, and Liu participated in the 2017 Canadian Team Mathematics Contest. On their team uniforms, each had a different number chosen from the list 11, 12, 13, 14, 15, 16. Helga's and Julia's numbers were even. Karl's and Liu's numbers were prime numbers. Glenda's number was a perfect square. What was Ioana's number?

- **(B)** 13
- (C) 14
- **(D)** 15
- **(E)** 12

(A) 11 13. A rectangle with height x and width 2x has the same perimeter as an equilateral triangle with side length 10. What is the area of the rectangle?



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- **(B)** 50
- (C) 25
- **(D)** 200

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**(E)** 100

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(**A**) 18 In the list 7,9,10,11,18, which number is the average (mean) of the other four numbers?

- (A) 9
- **(B)** 18
- (C) 7
- **(D)** 11
- **(E)** 10

shows a time in which all of the digits are consecutive and are in increasing order?

(A) 458 (B) 587 (C) 376 (D) 215 15. A digital clock shows the time 4:56. How many minutes will pass until the clock next

16. Reading from left to right, a sequence consists of 6 X's, followed by 24 Y's, followed twice as many times as the other letter. The sum of the four possible values of n is

(A) 72 (B) 54 litulu the the little l by 96 X's. After the first n letters, reading from left to right, one letter has occurred

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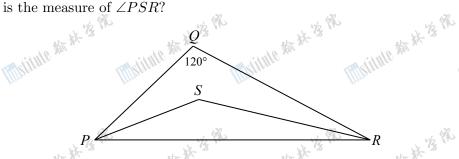
Y.

Y.

- **(B)** 6
- **(D)** 8
- **(E)** 7

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Also,  $\angle QPS = \angle RPS$  and 18. In the diagram,  $\triangle PQR$  has  $\angle PQR = 120^{\circ}$ .  $\angle QRS = \angle PRS$ . (In other words, SP and SR bisect  $\angle QPR$  and  $\angle QRP$ , respectively.) Mytithe My 14 13 1980 What is the measure of  $\angle PSR$ ? Maritute 紫 林·溪



- Marithte Mar # 13 198 **(A)** 130°
- **(B)** 120°
- **(C)** 140°
- **(D)** 160°
- **(E)** 150°

19. On Monday, Mukesh travelled x km at a constant speed of 90 km/h. On Tuesday, Matinta 教育社·漢序 he travelled on the same route at a constant speed of 120 km/h. His trip on Tuesday took 16 minutes less than his trip on Monday. The value of x is

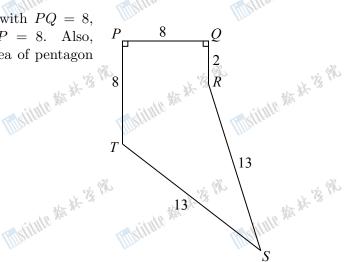
- (A) 90
- **(B)** 112
- (C) 100
- **(D)** 96
- **(E)** 92

20. In the diagram, PQRST is a pentagon with PQ = 8, QR = 2, RS = 13, ST = 13, and TP = 8. Also,  $\angle TPQ = \angle PQR = 90^{\circ}$ . What is the area of pentagon PQRST?  $(\mathbf{A}) 76$ 

- (B) 84
- (C) 92

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- **(D)** 100
- **(E)** 108



#### Part C: Each correct answer is worth 8.

21. A coin travels along a path that starts in an unshaded square in the top row of the figure, that uses only diagonal moves, and that ends in an unshaded square in the bottom row. A diagonal move takes the coin either one square down and one square left, or one square down and one square right. How many different paths from the top row to the bottom row are possible?

- (A) 16
- **(B)** 20
- (C) 32

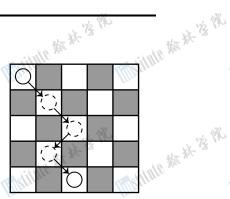
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(D) 24

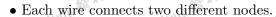
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**(E)** 28

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- There is at most one wire between each pair of nodes.
- Exactly three wires are connected to each node.

circuit has 13 788 wires, how many nodes does it have? An example of a Miniou circuit is shown. If a Miniou



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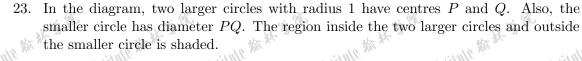
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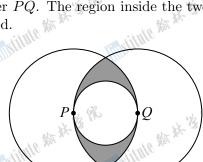
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The area of the shaded region is closest to

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wire node

In Mrs. Warner's class, there are 30 students. Strangely, 15 of the students have a height of 1.60 m and 15 of the students have a height of 1.22 m. Mrs. Warner lines up n students so that the average height of any four consecutive students is greater than 1.50 m and the average height of any seven consecutive students is less than 1.50 m. What is the largest possible value of n?

25. P.J. starts with m = 500 and chooses a positive integer n with  $1 \le n \le 499$ . He applies the following algorithm to m and n:

• P.J. sets r equal to the remainder when m is divided by n.

• If r = 0, P.J. sets s = 0.

If r > 0, P.J. sets s equal to the remainder when n is divided by r.

• If s = 0, P.J. sets t = 0.

If s > 0, P.J. sets t equal to the remainder when r is divided by s.

For example, when n = 8, P.J. obtains r = 4, s = 0, and t = 0. For how many of the positive integers n with  $1 \le n \le 499$  does P.J.'s algorithm give  $1 \le r \le 15$  and  $2 \le s \le 9 \text{ and } t = 0$ ?

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#### For students...

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Thank you for writing the 2018 Pascal Contest! Each year, more than 240 000 students from more than 75 countries register to write the CEMC's Contests.

Encourage your teacher to register you for the Fryer Contest which will be written in April.

Visit our website cemc.uwaterloo.ca to find

- More information about the Fryer Contest
- Free copies of past contests
- Math Circles videos and handouts that will help you learn more mathematics and prepare for future contests
- Information about careers in and applications of mathematics and computer science

#### For teachers...

Visit our website cemc.uwaterloo.ca to

- Register your students for the Fryer, Galois and Hypatia Contests which will be written in April
- Look at our free online courseware for senior high school students

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- Learn about our face-to-face workshops and our web resources
- Subscribe to our free Problem of the Week
- Investigate our online Master of Mathematics for Teachers

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• Find your school's contest results

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